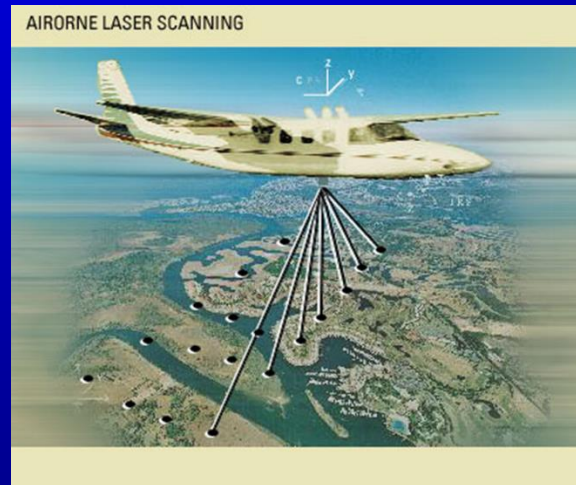


# Photogrammetry



# Photogrammetry SE 321

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  - Office: 2A - 44
- Surveying Engineering Program
- Introduction-Measurement on Single Photos-Stereo Viewing and Parallax



# Photogrammetry SE 321

- Instructor: Prof. Ismat Elhassan
- Office: 2A 44
- E-mail: [ismat@ksu.edu.sa](mailto:ismat@ksu.edu.sa)
- Textbook: Wolf, Dewitt & Wilkinson. 2014.  
“Elements of Photogrammetry with Applications in GIS”, 4<sup>th</sup> edition
- Evaluation:
  - Two tests:       2x15       = 30
  - Tutorials, HWs and Lab = 30
  - Final Exam       = 40



## Course Objective and Learning Outcomes

- At the end of the course student will be able to:
  - - Extract surveying information from single aerial photos;
  - - Extract surveying information from stereo aerial photos;
  - - Design aerial survey project



# Course Contents

- Definition, Types and Importance of Photogrammetry
- Image Acquisition (Cameras)
- Survey Data from Measurements on Single (Vertical and Tilted) Aerial Photograph
- Stereo Viewing and Extraction of survey data from stereo photographs
- Stereo Plotters: Components, Types, Orientation and operation to provide survey data
- Flight planning

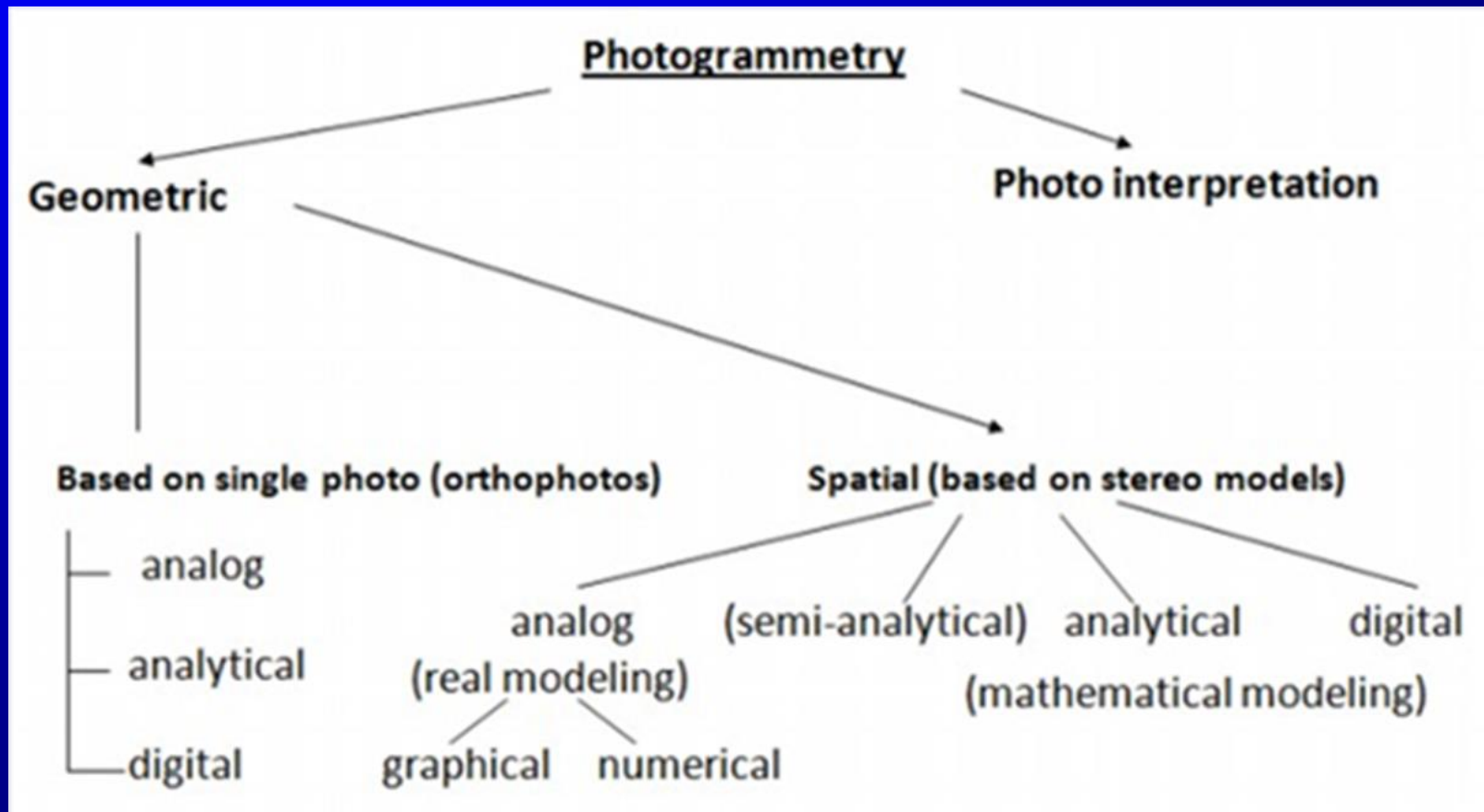


# Introduction

- Photogrammetry is the science, art, and technology of obtaining reliable information from photographs.
- Two major areas: metric, and interpretative.
- Terrestrial, aerial and Space Photogrammetry.
- Uses of Photogrammetry: survey data (distances, angles, elevations), topographic mapping, determine precise point coordinates, cross sections, deflection monitoring, and many other engineering applications.
- Types of Photogrammetry:

# Types of Photogrammetry

- The following chart summarize types of photogrammetry:



# Advantages of Photogrammetry

- Some advantages of photogrammetry over conventional surveying and mapping methods are:
- It provides a **permanent photographic record** of conditions that existed at the time the aerial photographs were taken.
- Since this record has metric characteristics, it is not only a pictorial record but also an **accurate measurable** record.
- If information has to be re-surveyed or re-evaluated, it is not necessary to perform **expensive field work**. The same photographs can be measured again and new information can be compiled easily. **Continue:**





# Advantages of Photogrammetry

- It can provide a large mapped area more **efficiently and economically** than other conventional methods.
- It provides a broad **detailed view** of the project area, identifying both topographic and cultural features.
- It can be used in locations that are difficult, unsafe, or **impossible to access**,
- Road surveys can be done **without closing lanes**, disturbing traffic. Once a road is photographed, measurement of road features, including elevation data, is done in the office, not in the field. This applies for all construction projects.



# Disadvantages of Photogrammetry

- **Disadvantages:**
- 1. **Seasonal conditions**, including weather, vegetation, and shadows can affect both the taking of photographs and the resulting measurement quality.
- 2. Overall **accuracy depends on camera quality** and flying height (photo scale).
- 3. Identification of **planimetric features** can be **difficult** or impossible (*e.g.* type of curb, size of culverts, type of fences, and **information on signs**).
- 4. **Underground utilities cannot be located**, measured, or identified.
- 5. Features **under clouds and bridges** are affected.



# Image Acquisition

- Image can be acquired using cameras.
- Classification of cameras:
- According to platform: **Terrestrial, Aerial and Space.**
- According to function: **Metric** for measurements and Reconnaissance (**non-metric**) for interpretation.
- According to design: **Optical, film** (single or multi-lens) and **Digital.**
- Aerial Metric cameras are mostly used for survey data production.



# Aerial Cameras

- For precise results, cameras must be geometrically stable, fast, have efficient shutters, sharp lenses
- Single-lens frame cameras: figure 27-2
  - most used format size is 23cm, focal length 150mm
  - components: lens, shutter, diaphragm, filter, focal plane, fiducial marks.
  - shutters can be operated manually or automatically.
  - The camera could be leveled regardless of the plane orientation (vertical optical axis).
  - Exposure station and principal point.
  - Camera calibration.

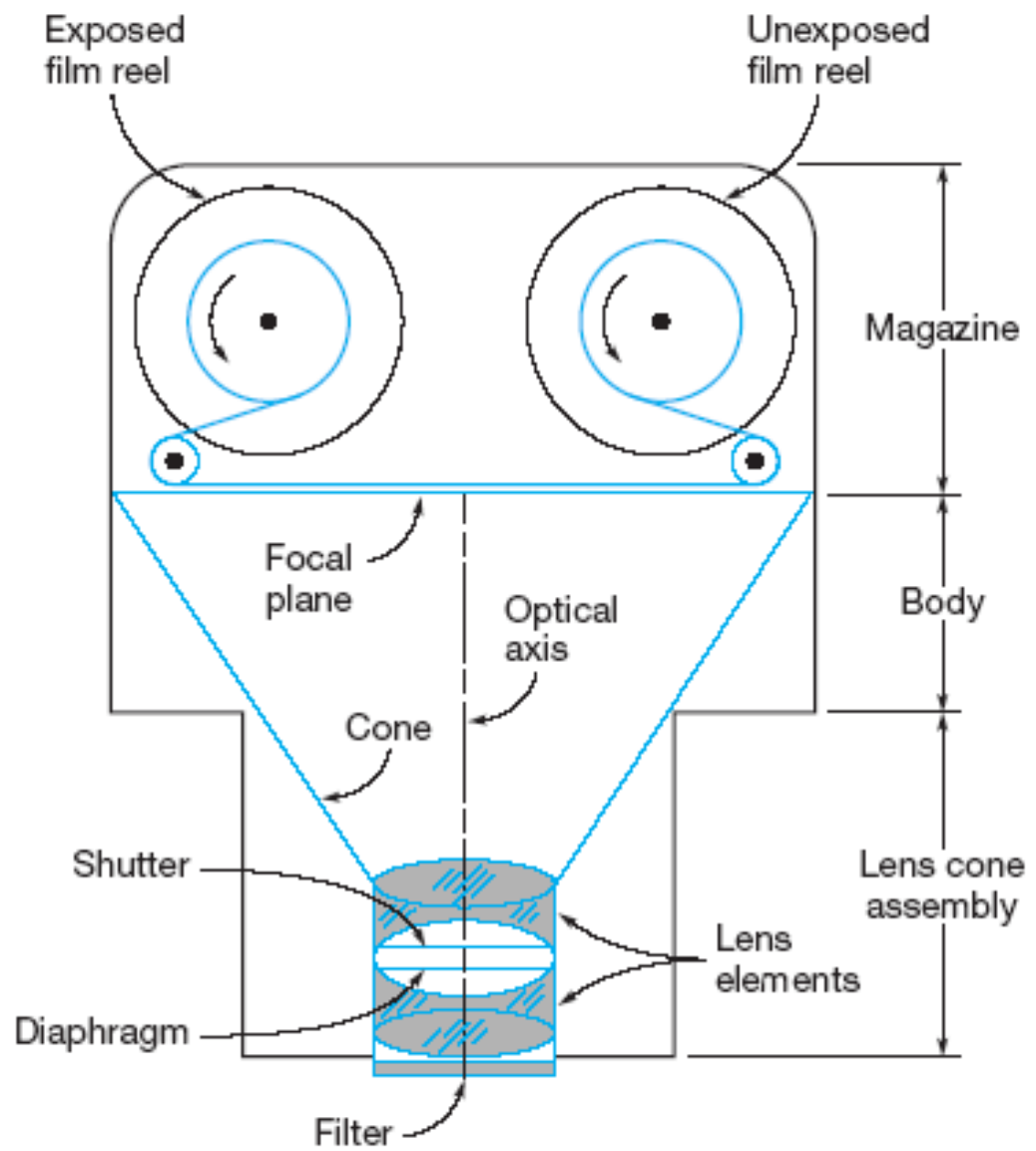


Figure 27-2 Principal components of a single lens frame aerial camera.

# Aerial Photographs

- Aerial Photographs can be classified according to optical axis attitude:
  - - **True Vertical**: if the camera axis is exactly vertical, (normal to horizontal) or near vertical.
  - - **Tilted Photographs**, if optical axis is tilted to vertical within 3degrees.
  - - **Oblique photographs**: **high** where horizon appears on photo and **low oblique** (horizon does not appear)
- Vertical or near Vertical Photos are the most used type for surveying applications



**Figure 27-4** Vertical aerial photograph. (Courtesy Pennsylvania Department of Transportation.)



**Figure 27-5** Low oblique aerial photograph showing state capital and downtown Madison, Wisconsin. (Courtesy State of Wisconsin, Department of Transportation.)



# High Oblique Photo

- Horizon appears on photo



# Color Vertical Aerial Photo

See Fiducial Marks (side and corner)



# Geometry of Vertical Photographs

- Definitions:
- **Principal point:** geometric center of photo, which can be located by joining opposite Fiducial Marks.
- **Exposure station:** position of lens center at time of exposure
- **Principal distance** (focal length:  $f$  or  $c$ ): distance from lens center to principal point
- **Image (photo) coordinate system** (right handed), principal point, exposure station as origin, x-axis along flight line, y-axis perpendicular to x-axis
- Measurements could be done on negative or positive, same geometry.

# Negative and Positive Film

- Film received from flight is **negative**. After processing and contact prints it is provided as **positive** where measurement will be done (They are geometrically identical):



Negative Film



Positive Film

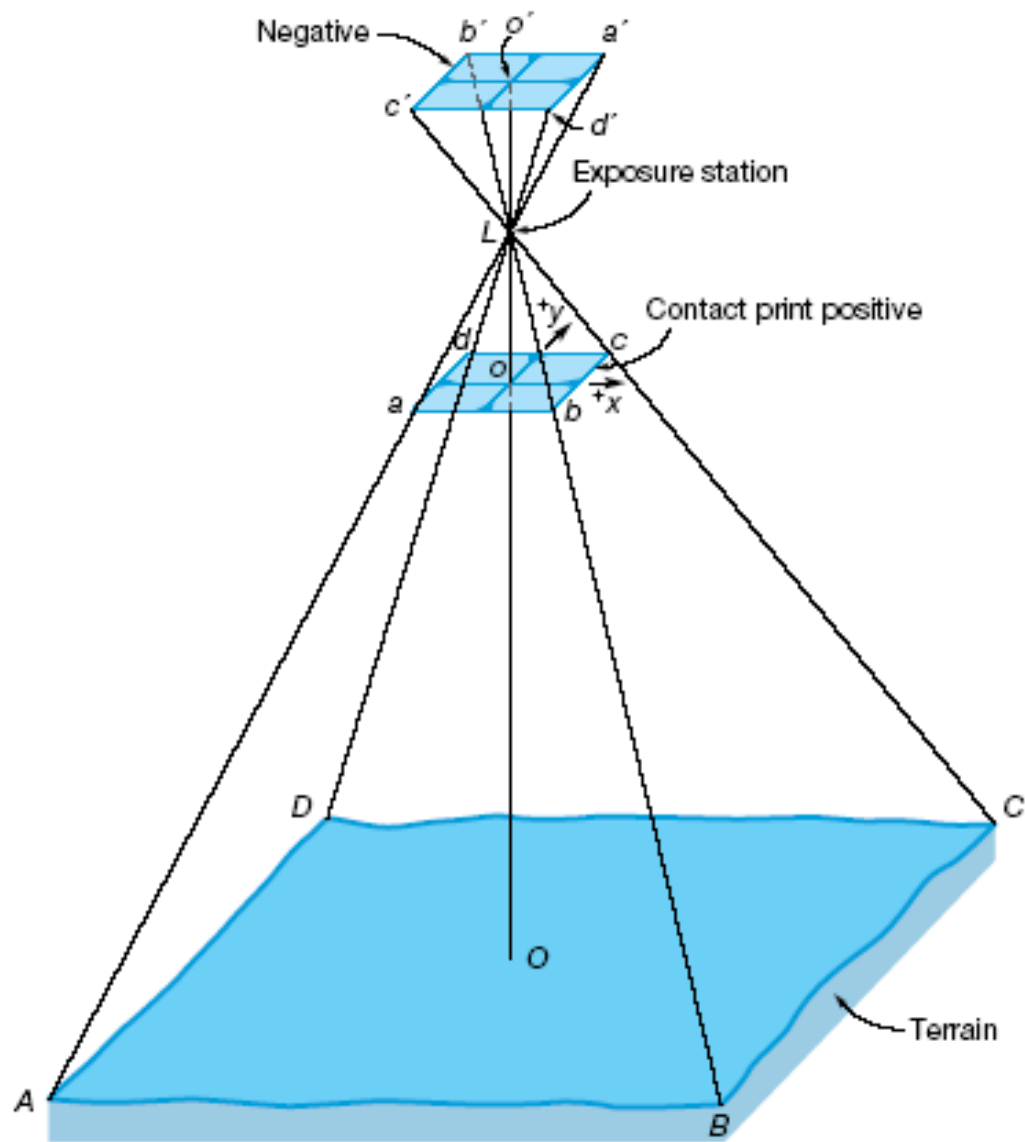
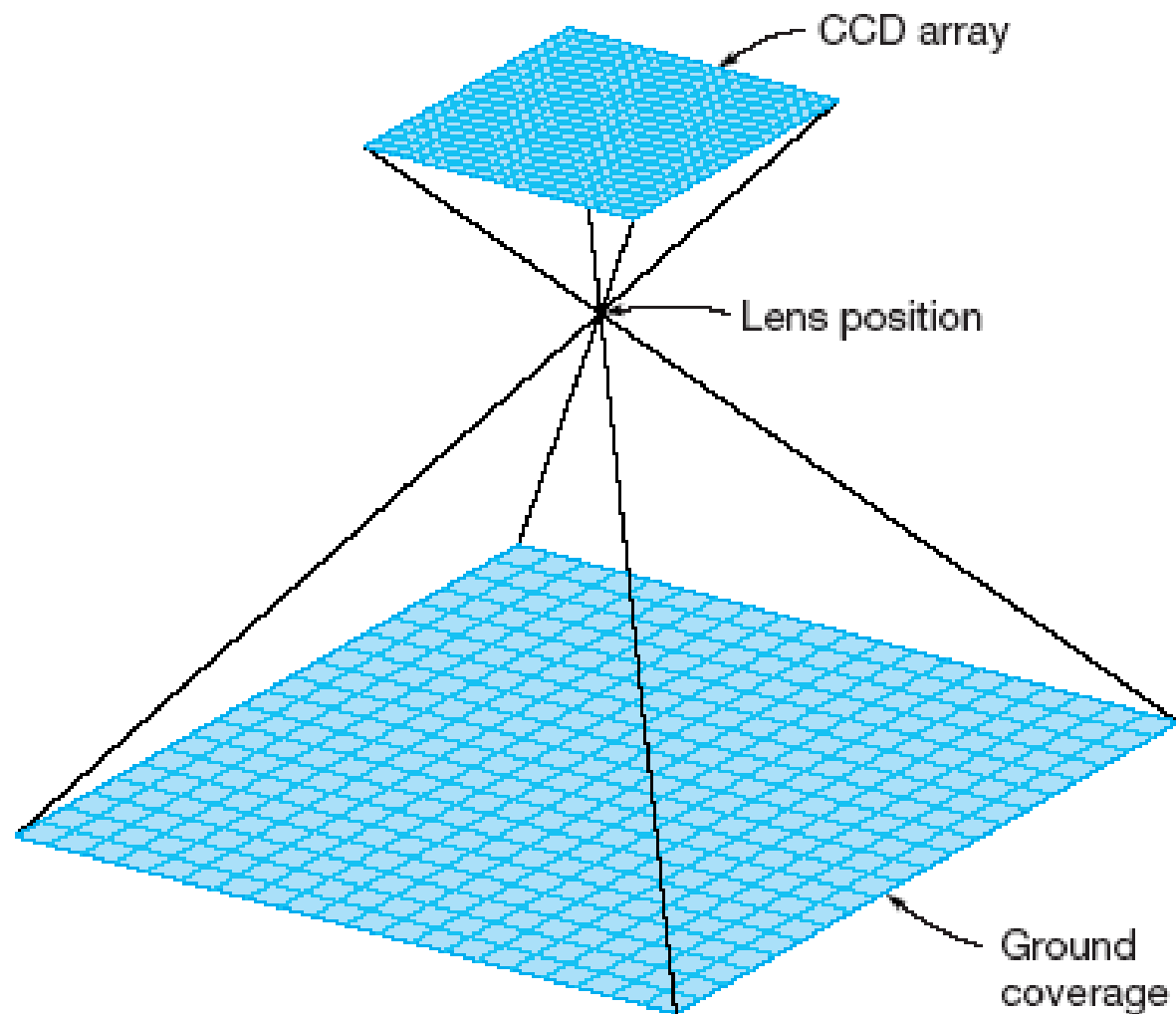


Figure 27-6 Geometry of a vertical aerial photograph.



**Figure 27-3** Geometry of a digital frame camera. (From *Elements of Photogrammetry, With Applications in GIS*, 3rd Ed., Wolf & Dewitt, 2000; Courtesy McGraw-Hill Book Co., Inc.)

# Scale of a Vertical Photograph

- Figure 27-7
- Scale of a photograph is the ratio of a distance on a photo to the same distance on the ground.
- Geometrically it is the focal length/flying height =  $f/H$
- For a point of level  $h$  above sea level:
- Scale ( $s$ ) at the point:  $f / (H - h)$

•Average scale of a photograph: 
$$S_{\text{avg}} = \frac{f}{H - h_{\text{avg}}}$$

If the  $f$ ,  $H$ , and  $h$  are not available, but a map is available then:

$$\text{Photo Scale} = \frac{\text{photo distance}}{\text{map distance}} \times \text{map scale}$$

## Example

- If a 1 km stretch of highway covers 4 cm on an air photo, the scale is calculated as follows:

$$\frac{\text{PHOTO DISTANCE}}{\text{GROUND DISTANCE}} = \frac{4 \text{ cm}}{1 \text{ km}} = \frac{4 \text{ cm}}{100\,000 \text{ cm}} = \frac{1}{25\,000} \quad \text{SCALE: } 1/25\,000$$

- If vertical photo scale is 1:20000 and image distance  $ab = 3 \text{ cm}$ , Ground distance  $AB = 3/(1/20000) = 3\text{cm} \times 20000 = 600\text{m}$
- If ground distance  $AB = 400\text{m}$  and photo scale is 1:5000, image distance  $ab = 400\text{m} \times (1/5000) = 8\text{cm}$





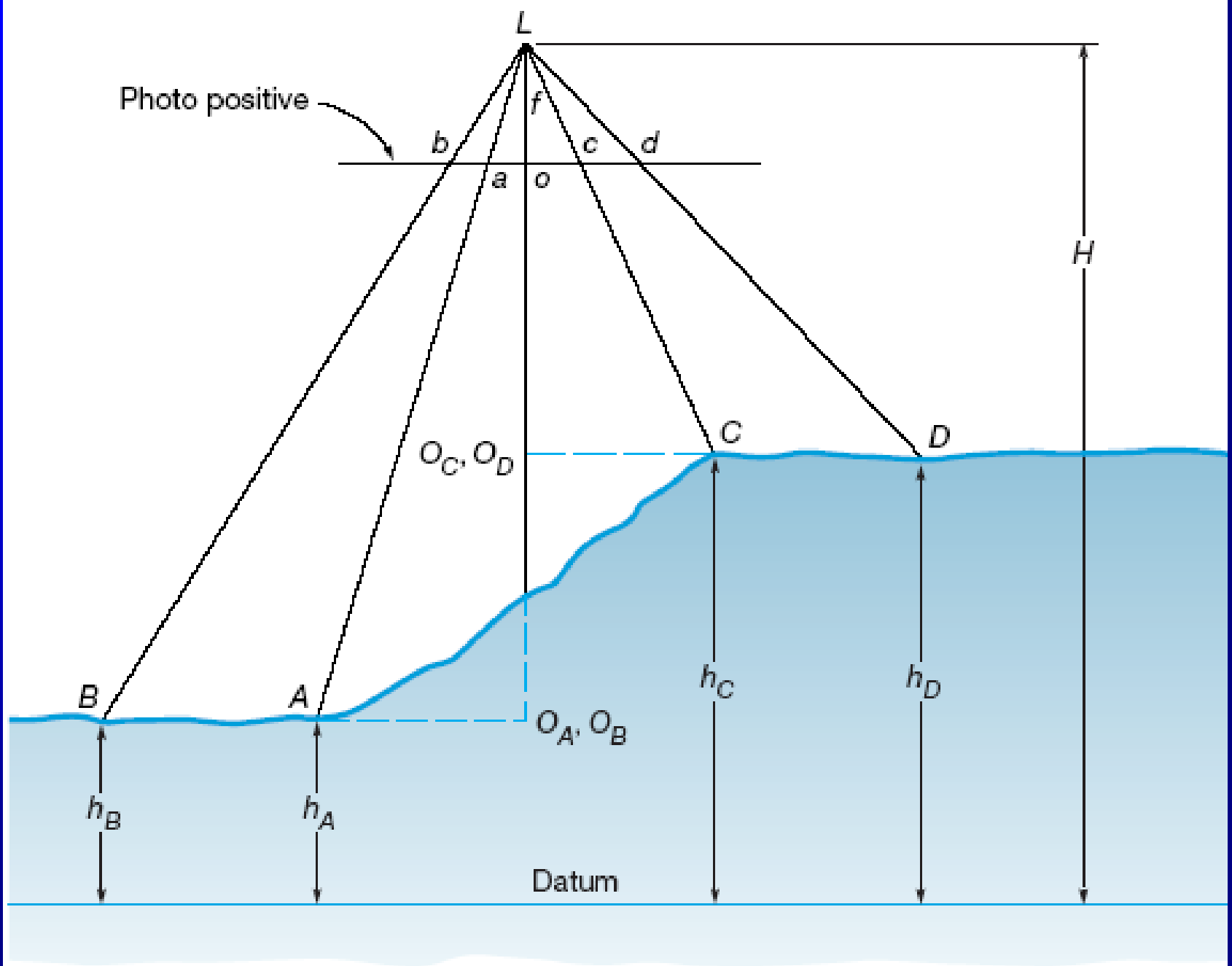


Figure 27-7 Scale of a vertical photograph.

# Undulating Ground

- For undulating ground with points of different elevations above datum (Fig. 27-7)
  - Scale at each point will be different:
  - Scales at a and b will be:
- Scale at a =  $S_A = f/(H - h_A)$
- Scale at b =  $S_B = f/(H - h_B)$ 
  - If given elevations of A, B, C and D, average ground elevation above datum will be
- $h_{av} = (h_A + h_B + h_C + h_D) / 4$
- Average photo scale =  $f/(H - h_{av})$
- Approximate distance AB =  $ab \times (H - h_{av}) / f$

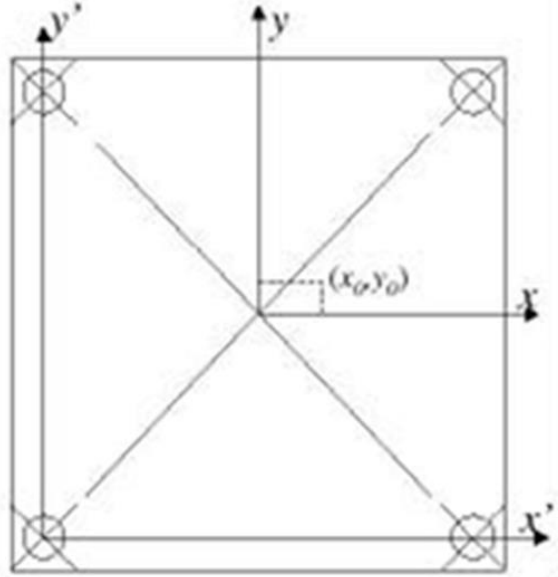


# Photo Coordinates System

- x-axis along flight line, y-axis perpendicular to it at principal point (ppt.) origin of the system and located by joining opposite fiducial marks.

**Photo Coordinate System**

- A Photo coordinate system is defined in reference to the fiducial marks, and the position of the PP given in the defined coordinate system, as  $(x_0, y_0)$ .
- Positive  $x$  is defined as the direction of flight



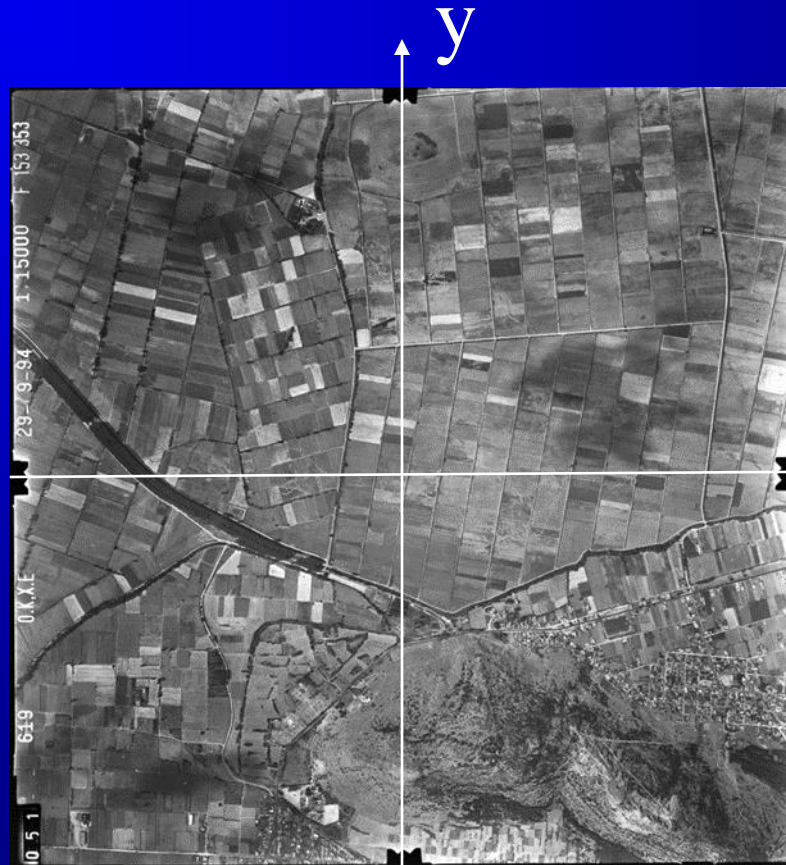
The diagram illustrates a photo coordinate system within a rectangular frame. At the center of the frame is the principal point (PP). Two coordinate axes are shown: a horizontal x-axis and a vertical y-axis, both originating from the PP. The x-axis is labeled 'x' and the y-axis is labeled 'y'. The origin of the system is marked as  $(x_0, y_0)$ . Four fiducial marks, represented by circles with an 'X' inside, are located at the corners of the frame. The top-left mark is labeled  $x', y'$ , the top-right mark is labeled  $x'', y''$ , the bottom-left mark is labeled  $x', y''$ , and the bottom-right mark is labeled  $x'', y'$ . Dashed lines indicate the coordinates of the PP relative to the frame's edges.



# Photo coordinates measurement

- This can be done manually or indirectly by measurement of coordinates on a mono comparator.

□



□



# Mono comparator

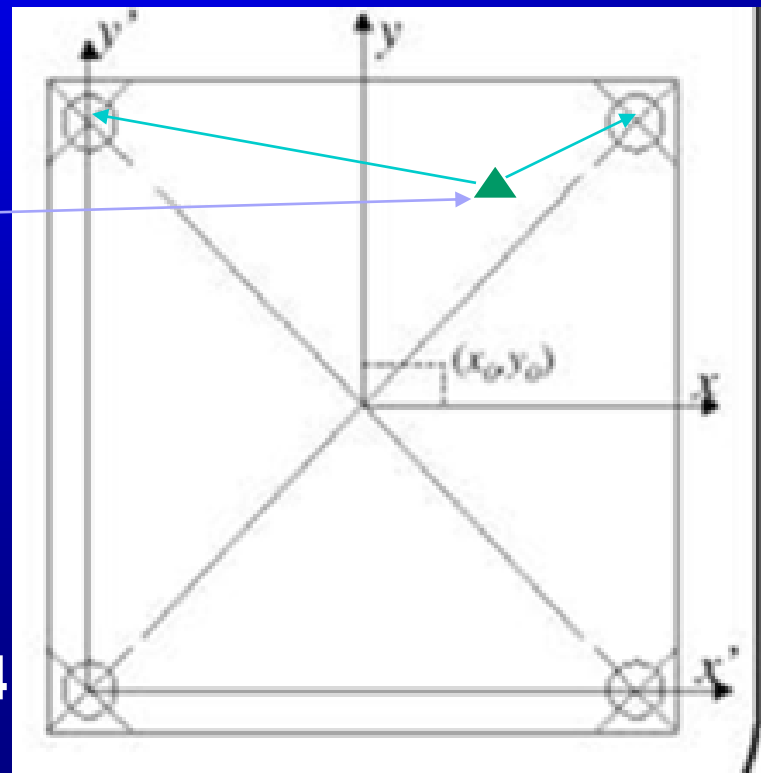
- Coordinates of ppt. and of other image points are measured on mono comparator coordinates and then reduced to ppt. as origin, a flat plate with flat glass, optical projector, hand wheels and coordinate system.



# Indirect Measurement of Photo coordinates

- Another method is to measure distances from image point to two of the **fiducial marks whose coordinates are given** in calibration and use intersection method to calculate position of image point.

- 
- 
- Measure  $a$ -F1
- and  $a$ -F2
- Compute
- F1-F2 from
- Compute  $a$  F4
- Coordinates!



F2

F3



## Example

- Coordinates of fiducial points F1 and F2 as measured on the photo coordinate system are: F1(-110.015; 110.002)mm and F2(110.005; 110.006)mm. Measured distances F1-a = 130.000mm and F2-a = 60.000mm. Compute coordinates of image point a:
- Solution steps:
- From given coordinates of F1 and F2 compute distance F1-F2; In  $\Delta$  F1-F2-a compute angles of the triangle using cosine rule first. Using coordinates of F1 and F2 and angles a-F1-F2 and F1-F2-a use intersection method to calculate coordinates of point a.



# Ground Coordinates from a Single Aerial Vertical Photograph

- Figure 27-8
- With phot coordinate system defined, we define an arbitrary ground coordinate system.
- That ground system could be used to compute distances and azimuths. Coordinates can also be transformed to any system
- In that ground system: Scale at a =  $S_A = f/(H - h_A)$

$$X_A = x_a * (\text{photograph scale at a})$$

$$Y_A = y_a * (\text{photograph scale at a})$$

Horizontal Ground Distance AB =

$$[(X_A - X_B)^2 + (Y_A - Y_B)^2]^{1/2}$$



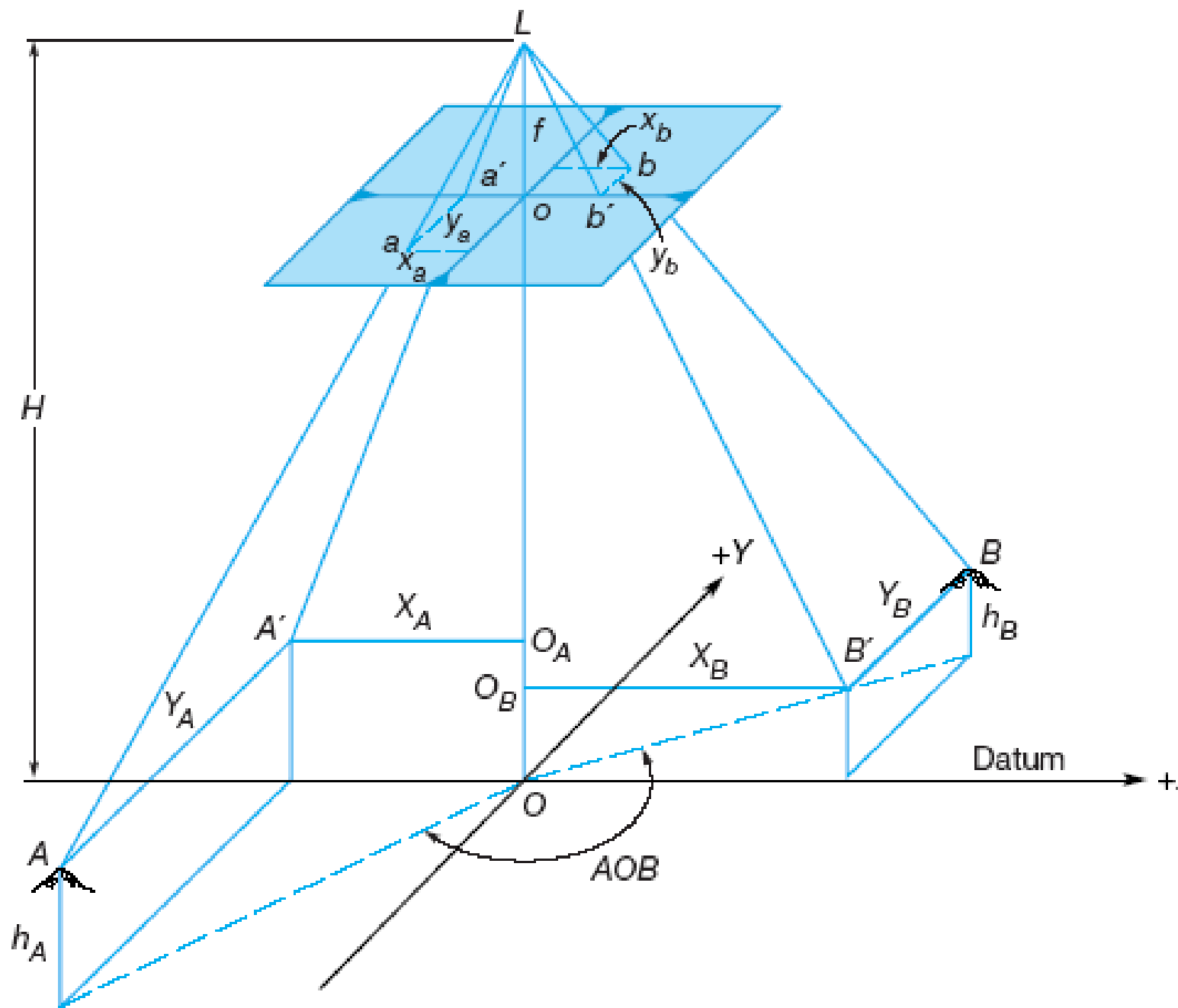


Figure 27-8 Ground coordinates from a vertical photograph.

# Flying Height of Vertical Photo

□ Flying height (**H**) can be determined by:

- Direct readings on the photo
- Applying scale equation, if scale could be computed

- Example: what is the flying height above datum if  $f=150\text{mm}$ , average elevation of ground is  $600\text{m}$ , scale is  $1:4000$ ?

- Or, if two control points of ground distance,  $L$  appear in the photograph, solve the equation:  $L^2 = (X_B - X_A)^2 + (Y_B - Y_A)^2$

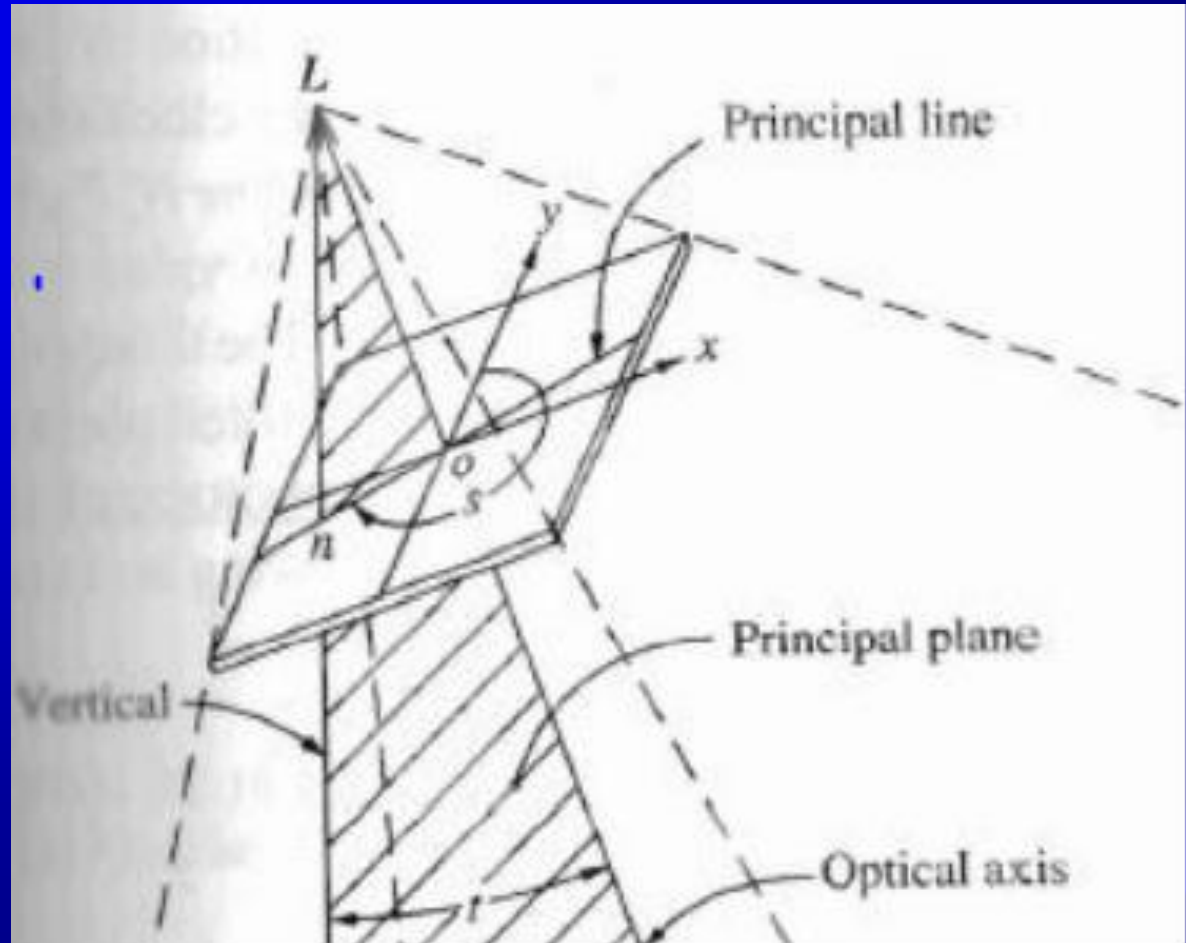
replacing the ground coordinates with the photo coordinates:  $X_A = x_a * (\text{photograph scale at } a)$

where photo scale at  $a = f/(H - h_A)$



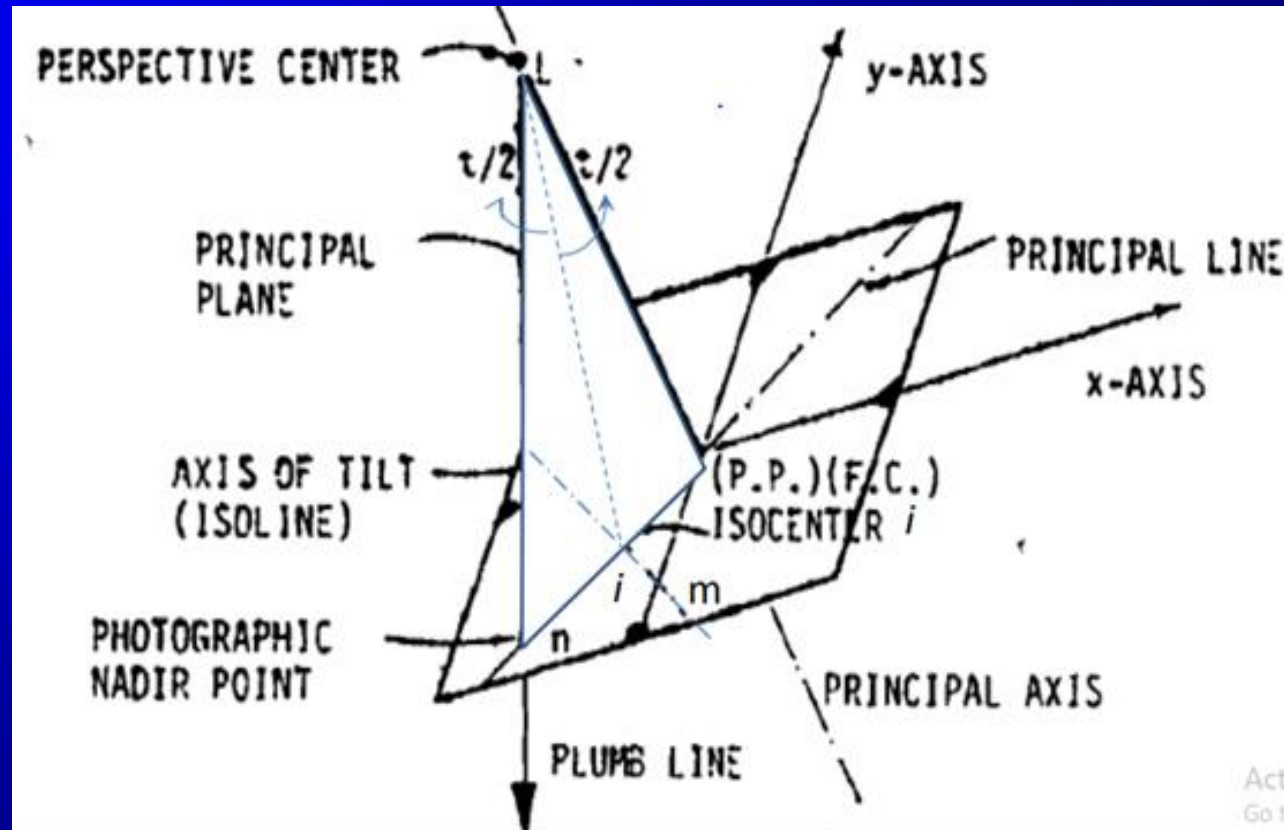
# Tilted Aerial Photos

- ❑ Camera axis cannot always be vertical. An angle from the vertical is called tilt angle.
- ❑ Nadir point,  $n$
- ❑ is intersection
- ❑ of vertical and
- ❑ Photo plane;
- ❑ Principal Line is
- ❑ line joining  $n$
- ❑ with principal
- ❑ point  $O$  or  $P$ ;
- ❑ Tilt angle,  $t$  is
- ❑ Angle between
- ❑ Vertical and optical axis



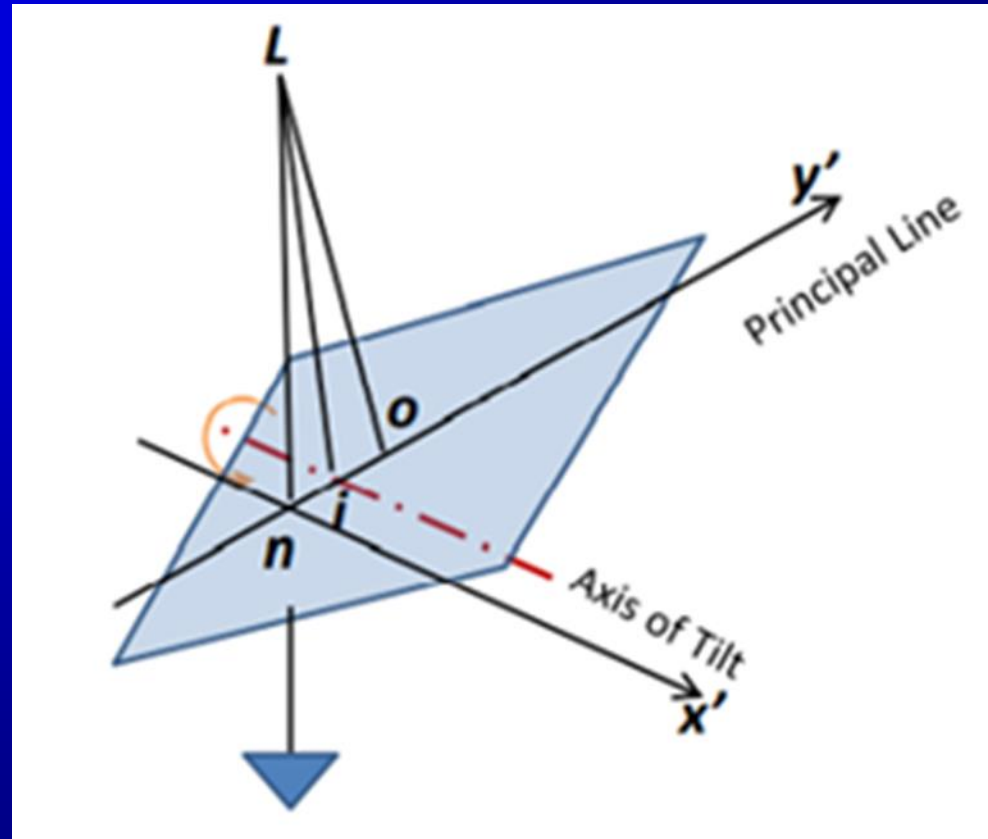
# Tilted Aerial Photo

- Definition:
- Isocenter,  $i$
- on bisector
- of tilt angle
- and principal
- Line;  $n$ ,  $i$  and
- $P$  are on
- Principal
- line



# Coordinates system of tilted photo

- Nadir point,  $n$  is the origin of the system;
- $Y'$  axis along the principal line;
- $X'$  perpendicular
- to  $y'$  at  $n$ .
- The tilt of photo
- is around the axis
- of tilt along the
- Principal line



# Tilted Aerial Photo

□ Coordinates on tilted photo in relation with vertical photo:

□  $y'$ -axis along

□ Principal line

□  $n$  is the origin

□  $t$  = tilt angle

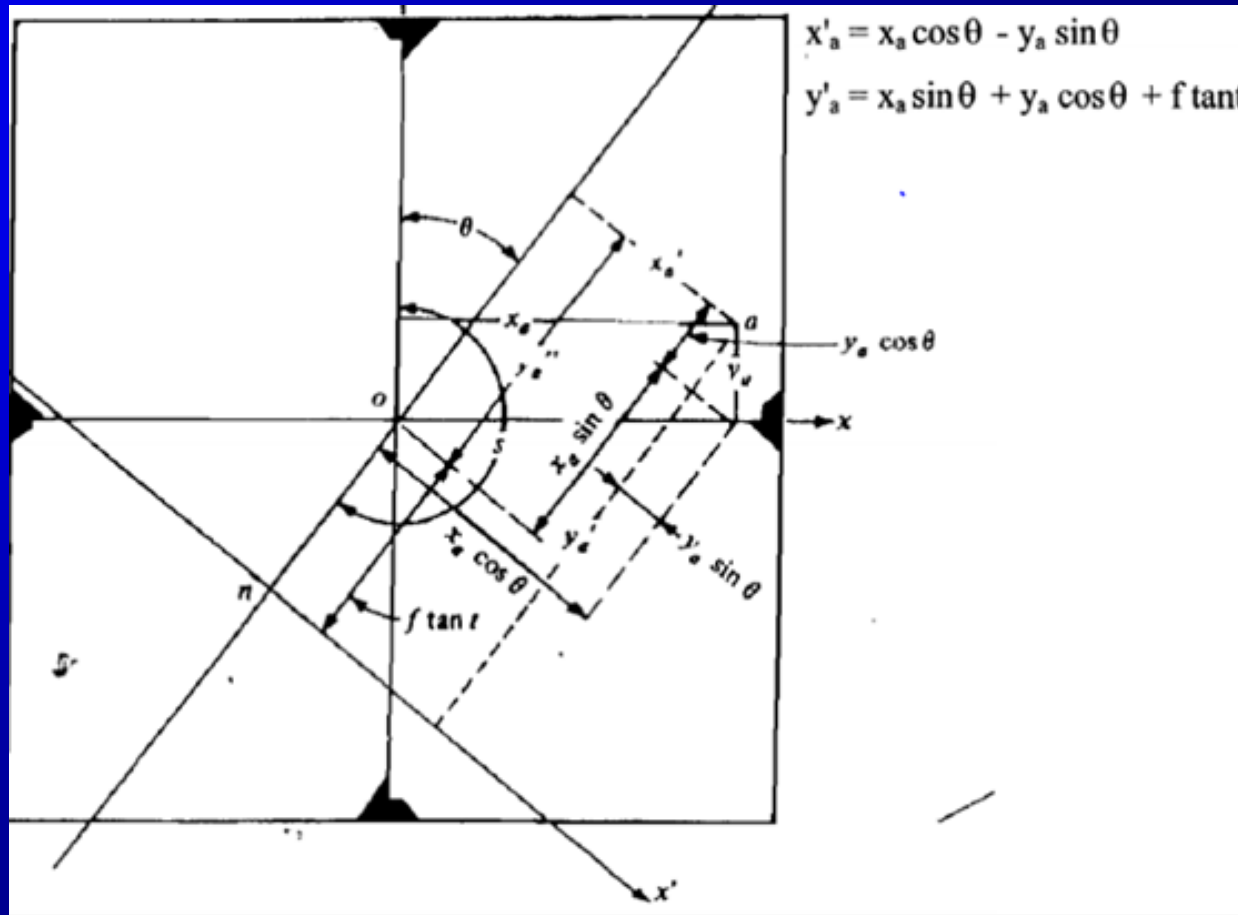
□  $\Theta$  = Azimuth

□ or swing

□ Angle measured

□ Clockwise from

□  $y$ -axis to principal line, on (Pn)



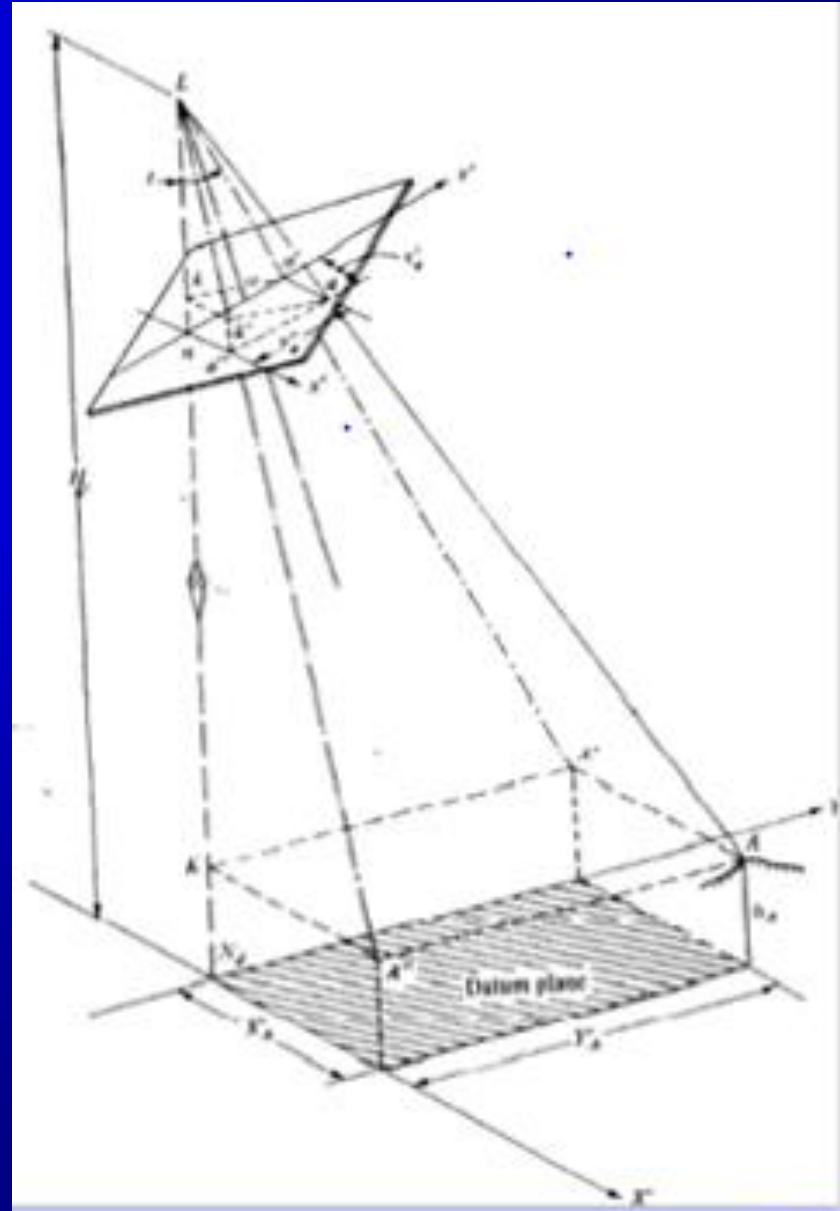
## Tilted Photo Coordinates

- Relation between vertical photo system and tilted photo system.
- Rotate vertical system an angle  $\Theta$  c.w. and shift origin from ppt. to nadir point, n.
- Tilted photo coordinates for any point are:
  - $x' = x \cos \Theta - y \sin \Theta$
  - $y' = x \sin \Theta + y \cos \Theta + f \tan t$



# Tilted Aerial Photo Scale

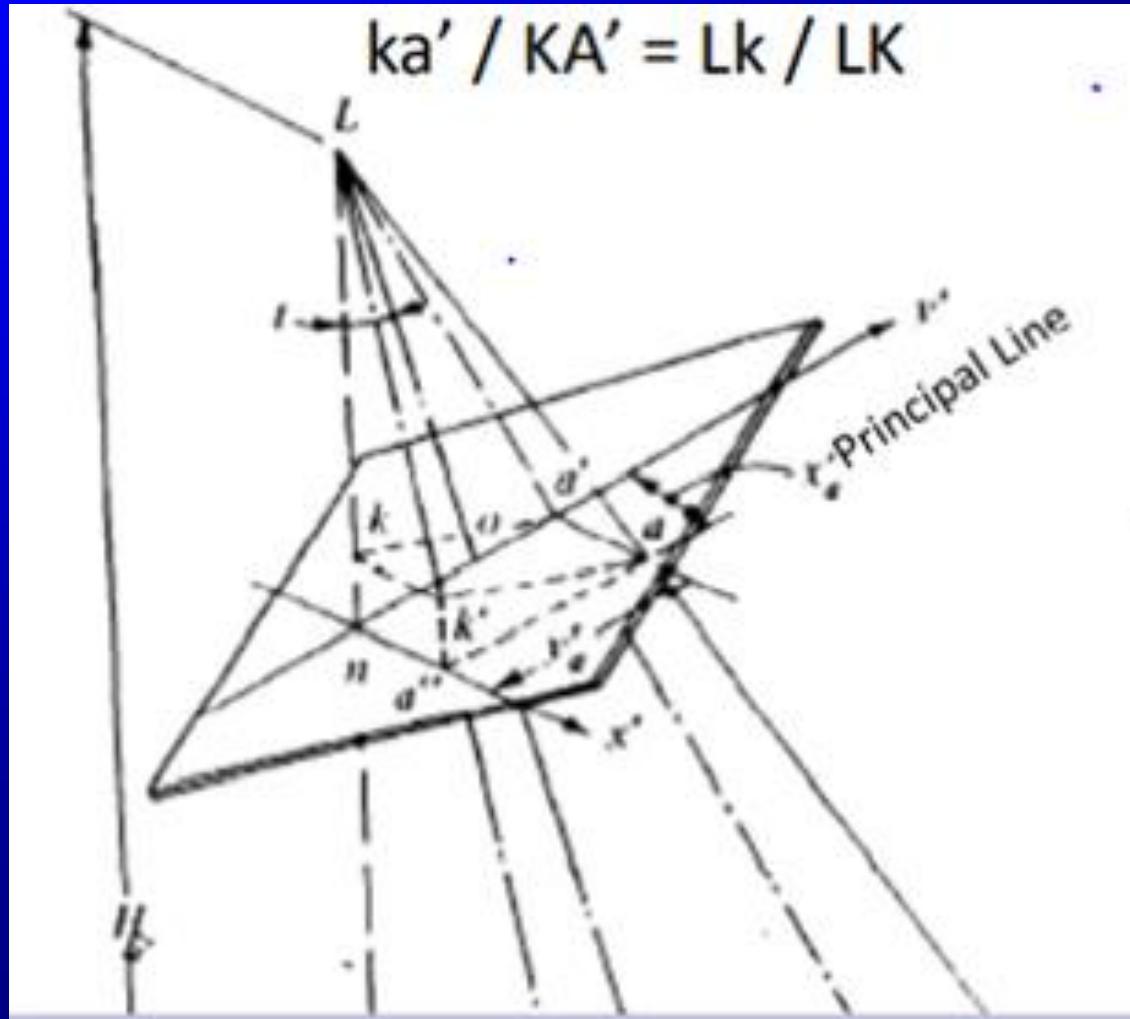
- Tilted photo scale =
- Horizontal distance
- On photo / horizontal
- Distance on ground =
- $Ka' / KA' = Lk / LK$





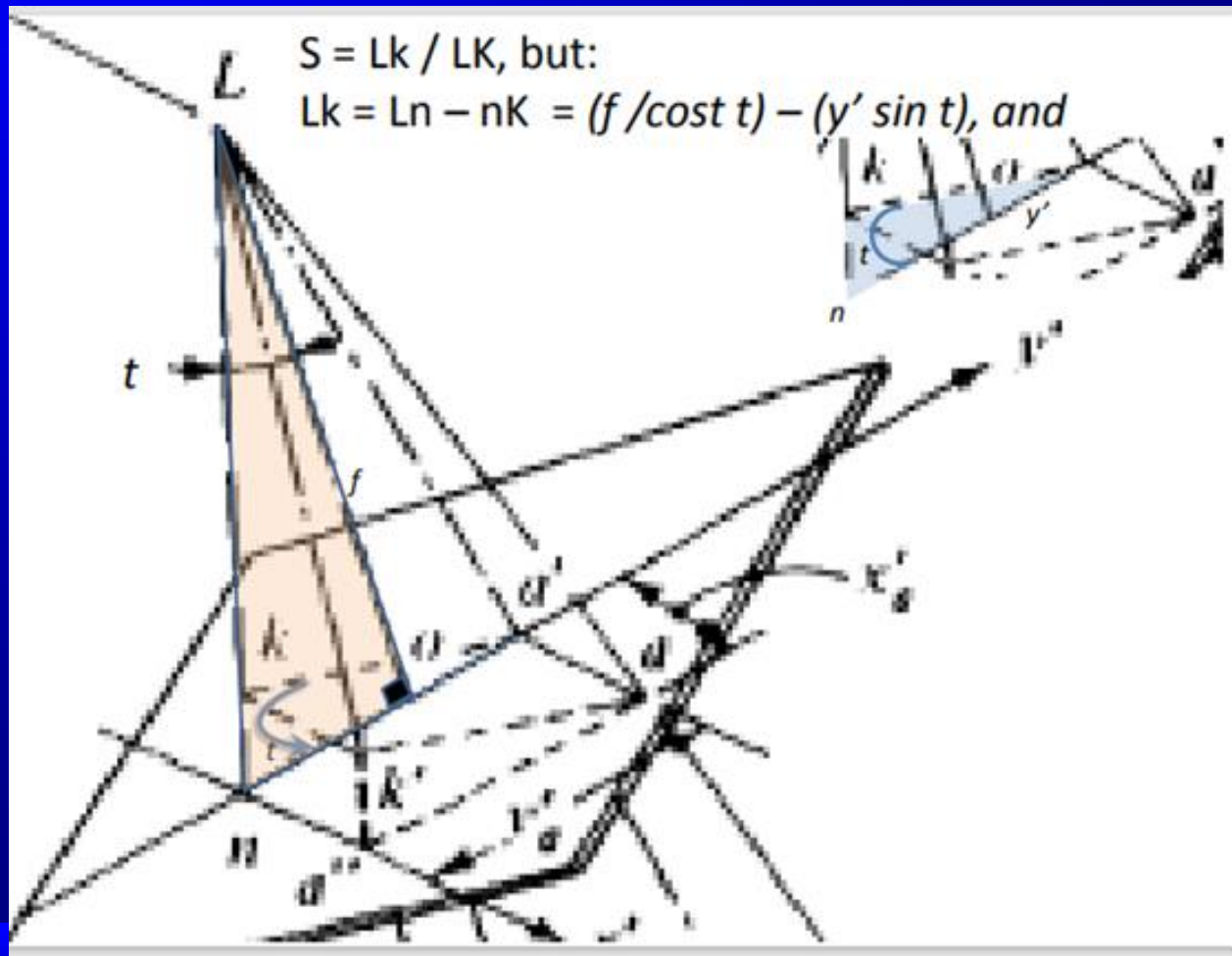
# Tilted Aerial Photo Scale

- Scale of tilted aerial photo =  $Lk/LK$ ;



# Tilted Aerial Photo Scale

- $Lk = Ln - nk$ ;  $Ln = f / \cos t$ ;  $nk = y' \sin t$ ;
- Hence,  $Lk = f / \cos t - y' \sin t$ ;  $LK = H - h$
- **Scale =  $[f / \cos t - y' \sin t] / (H - h)$**



# Tilted Photo Scale

- Example:
- A  $3^\circ$  tilted aerial photo is exposed with a camera of 150mm focal length from a flying altitude 3000m above MSL. Swing angle of photo is  $218^\circ$ .
- Point A with elevation 600m above MSL has image coordinates: -60.00mm and 80.00mm, compute the scale of the photo at point a.



# Ground Coordinates from Tilted photo

## □ X Ground Coordinate

### Ground Coordinates from a tilted photograph

- Coordinates of point A in a ground coordinate system  $X', Y'$  where:
- $X', Y'$  are parallel to  $x'$  and  $y'$  (auxiliary system)
- Ground Nadir N is the origin of the ground system
- Note that in the auxiliary coordinate system, lines parallel to  $x'$  are horizontal, thus  $x'$  on the photo is horizontal and directly related to ground X by the scale, or

$$X'_A = x' / S_A$$

# Ground Coordinates from Tilted Photo

## □ Y Ground Coordinate



- But in the auxiliary system,  $y'$  is in the direction of maximum tilt and not horizontal, the scale is ratio between horizontal projections.
- $K_a$ : Horizontal projection of  $y' = y' \cos t$
- Then,
- $Y' = y' \cos t / S$

# Tilted Photo and Ground Coordinates

## □ Example

- An aerial tilted photo of 150mm focal length and 3000m flying height above MSL has tilt angle  $3^\circ$  and swing angle  $218^\circ$ . Point A has elevation of 600m above MSL and image coordinates -60mm and 80.00mm in x and y respectively.
- Another ground point Q has photo coordinates 75mm and 40mm in x and y respectively and ground elevation 620m above MSL.
- Compute ground distance AQ.



# Relief Displacement on a Vertical Photograph

- Figure 27-9
- The shift of an image from its theoretical datum location caused by the object's relief. Two points on a vertical line will appear as one line on a map, but two points, usually, on a photograph.
- In a vertical photo, the displacement is from the principal point.
- Relief displacement (d) of a point wrt a point on the datum :

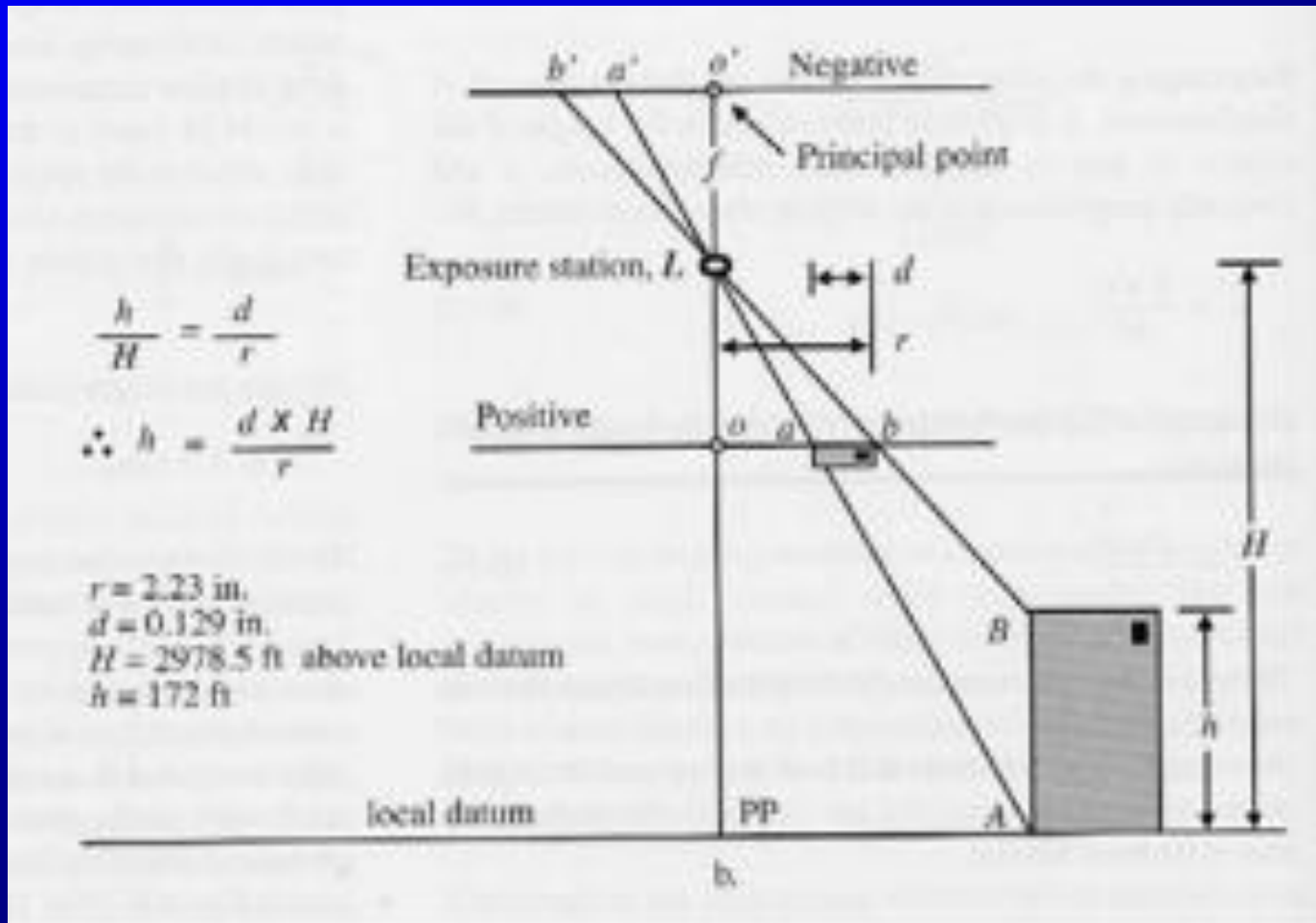
$$d = \frac{r h}{H}$$

where: r is the radial distance on the photo to the high point  
h : elevation of the high point, and H is flying height above datum

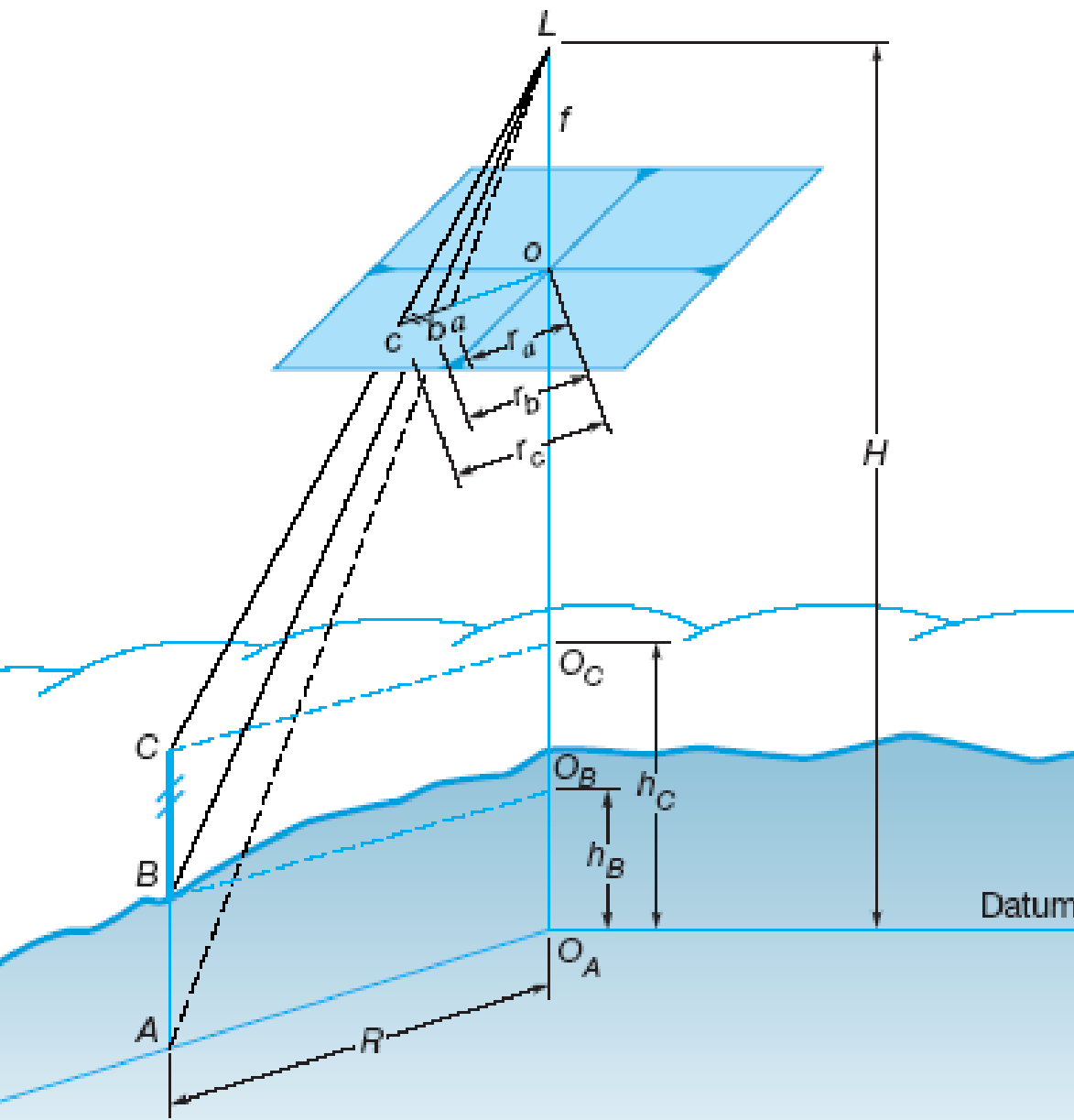
- Assuming that the datum is at the bottom of vertical object, H is the flying height above ground, the value h will compute the object height.

# Relief Displacement

- RD caused by change in ground height
- Object height,  $h = dr \times H / r$  (  $r$  is image distance from p.p. to image of top of object (image of B) )







$$r_a/R = f/H$$

$$\text{Or: } r_a * H = R * f \text{ ----(1)}$$

$$r_b/R = f/(H-h)$$

$$\text{Or: } r_b * (H-h) = R * f \text{ ---(2)}$$

Then from (1) and (2);

$$r_a * H = r_b * (H-h) \text{ then;}$$

$$RD = r_b - r_a = r_b * h_b / H$$

$$RD = r_t - r_b = r_t * h_T / H$$

Figure 27-9 Relief displacement on a vertical photograph.

# Example

- Given:
- Flying height above ground surface = 2000m
  - Readings on the photo:
    - Radial distance to image top=85mm
    - Radial distance to image base= 83mm
    - Solution:
      - Relief displacement  $dr = 85 - 83 = 2\text{mm}$
      - Object height =  $h = [dr / r_t] * H$
      - $= [2/85] * 2000 = 47.06\text{m}$