**10.1. Single Mean:**

Q1. A machine is producing metal pieces that are cylindrical in shape. A random sample of size 5 is taken and the diameters are 1.70, 2.11, 2.20, 2.31 and 2.28 centimeters. Then,

1) The sample mean is:

(A) 2.12 (B) 2.32 (C) 2.90 (D) 2.20 (E) 2.22

2) The sample variance is:

(A) 0.59757 (B) 0.28555 (C) 0.35633 (D) 0.06115 (E) 0.53400

Q2. The average life of a certain battery is 5 years, with a standard deviation of 1 year. Assume that the live of the battery approximately follows a normal distribution.

1. The sample mean X of a random sample of 5 batteries selected from this product has a mean equal to:

(A) 0.2 (B) 5 (C) 3 (D) None of these

2) The variance of the sample mean X of a random sample of 5 batteries

selected from this product is equal to:

(A) 0.2 (B) 5 (C) 3 (D) None of these

3) The probability that the average life of a random sample of size 16 of such batteries will be between 4.5 and 5.4 years is:

(A) 0.1039 (B) 0.2135 (C) 0.7865 (D) 0.9224

4) The probability that the average life of a random sample of size 16 of such batteries will be

less than 5.5 years is:

(A) 0.9772 (B) 0.0228 (C) 0.9223 (D) None of these

5) The probability that the average life of a random sample of size 16 of such batteries will be more than 4.75 years is:

1. 0.8413 (B) 0.1587 (C) 0.9452 (D) None of these

 6) If where X represents the sample mean for a random sample of size

9 of such batteries, then the numerical value of a is:

 (A) 4.653 (B) 6.5 (C) 5.347 (D) None of these

Q4. Suppose that you take a random sample of size n=64 from a distribution with mean =55 and standard deviation =10. Let be the sample mean.

1. What is the approximated sampling distribution of ?
2. What is the mean of ?

 (c) What is the standard error (standard deviation) of ?

(d) Find the probability that the sample mean exceeds 52.

(A) 0.7745 (B) 0.2784 (C) 0.9973 (D) 0.0236



8.22 The heights of 1000 students are approximately normally distributed with a mean of 174.5 centimeters and a standard deviation of 6.9 centimeters. Suppose 200 random samples of size 25 are drawn from this population and the means recorded to the nearest tenth of a centimeter. Determine

1. the mean and standard deviation of the sampling distribution of ;
2. the number of sample means that fall between 172.5 and 175.8 centimeters inclusive;

Then the number of sample means that fall between 172.5 and 175.8 centimeters is

0.7529 \* 1000 ≈ 753

(c) the number of sample means falling below 172.0 centimeters.

the number of sample means falling below 172.0 centimeters is

**10.2. Two Means:**

if we have and which are independent then

Q1. A random sample of size n1 = 36 is taken from a normal population with a mean 1 = 70 and a standard deviation 1 = 4. A second independent random sample of size n2 = 49 is taken from a normal population with a mean 2 = 85 and a standard deviation 2 = 5. Let X1 and X2 be the averages of the first and second samples, respectively.

1. Find E() and Var().

 b) Find E() and Var().

1. Find P( 70 < < 71).

d) Find P( > 16).

Q2. A random sample of size 25 is taken from a normal population (first population) having a mean of 100 and a standard deviation of 6. A second random sample of size 36 is taken from a different normal population (second population) having a mean of 97 and a standard deviation of 5. Assume that these two samples are independent.

1. the probability that the sample mean of the first sample will exceed the sample mean of the second sample by at least 6 is

(A) 0.0013 (B) 0.9147 (C) 0.0202 (D) 0.9832

(2)  the probability that the difference between the two sample means will be less than 2 is

(A) 0.099 (B) 0.2480 (C) 0.8499 (D) 0.9499

**10.3. Single Proportion:**

Q1. Suppose that 20% of the students in a certain university smoke cigarettes. A random sample of **5** students is taken from this university. Let be the proportion of smokers in the sample.

 (1) Find E()  , the mean .

1. Find Var() 2 , the variance of .
2. Find an approximate distribution of .

we can’t find it because n <30

1. Find P() >0.25). we can’t find it because n <30

**10.4. Two Proportions:**

Q1. Suppose that 25% of the male students and 20% of the female students in a certain university smoke cigarettes. A random sample of 5 male students is taken. Another random sample of 10 female students is independently taken from this university. Let pˆ1 and pˆ2 be the proportions of smokers in the two samples, respectively.

(1) Find E(  ) , the mean of

(2) Find Var() 2 pˆ 1 pˆ 2 , the variance of .

(3) Find an approximate distribution of

(4) Find P(0.10< <0.20).

**10.5 t-distribution:**

Q1. Using t-table with degrees of freedom df=14, find

Q2. From the table of t-distribution with degrees of freedom 15 , the value of t0.025 equals to

(A) 2.131 (B) 1.753 (C) 3.268 (D) 0.0

**H.W**

Q3. The random variable X, representing the lifespan of a certain light bulb, is distributed normally with a mean of 400 hours and a standard deviation of 10 hours.

1. What is the probability that a particular light bulb will last for more than 380 hours?

1. Light bulbs with lifespan less than 380 hours are rejected. Find the percentage of light bulbs that will be  rejected.
2. If 9 light bulbs are selected randomly, find the probability that their average lifespan will be less than  405.

Q5. The amount of time that customers using ATM (Automatic Teller Machine) is a random variable with the mean 3.0 minutes and the standard deviation of 1.4 minutes. If a random sample of 49 customers is observed, then X: The amount of time that customers using ATM

1. the probability that their mean time will be at least 2.8 minutes is

(A) 1.0 (B) 0.8413 (C) 0.3274 (D) 0.4468

(2)  the probability that their mean time will be between 2.7 and 3.2 minutes is

8.28 A random sample of size 25 is taken from a normal population having a mean of 80 and a standard deviation of 5. A second random sample of size 36 is taken from a different normal population having a mean of 75 and a standard deviation of 3. Find the probability that the sample mean computed from the 25 measurements will exceed the sample mean computed from the 36 measurements by at least 3.4 but less than 5.9. Assume the difference of the means to be measured to the nearest tenth.

8.29 The distribution of heights of a certain breed of terrier has a mean of 72 centimeters and a standard deviation of 10 centimeters, whereas the distribution of heights of a certain breed of poodle has a mean of 28 centimeters with a standard deviation of 5 centimeters. Assuming that the sample means can be measured to any degree of accuracy, find the probability that the sample mean for a random sample of heights of 64 terriers exceeds the sample mean for a random sample of heights of 100 poodles by at most 44.2 centimeter

Q2: Suppose that you take a random sample of size n=100 from a binomial population with parameter p=0.25 (proportion of successes). Let X / n be the sample proportion of successes, where X is the number of successes in the sample.

n=100 , p=0.25

1. What is the approximated sampling distribution of ?

1. What is the mean of ?

 (c) What is the standard error (standard deviation) of ?

 (d) Find the probability that the sample proportion is less than 0.2.