



King Saud University  
 College of Business Administration  
 Quantitative Analysis Department (QUA)

## Quantitative Methods for Decision Making

QUA 553

**MIDTERM EXAM**

**Duration: 90 min.**

**Name:**

**Student ID:**

|        |    |    |    |    |    |    |    |    |    |    |    |     |
|--------|----|----|----|----|----|----|----|----|----|----|----|-----|
| Q#     | 1  | 2  | 3  | 4  | 5  | 6  | 7  | 8  | 9  | 10 | 11 | 12  |
| Answer |    |    |    |    |    |    |    |    |    |    |    |     |
| Q#     | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | --- |
| Answer |    |    |    |    |    |    |    |    |    |    |    |     |

**Note:**

- THE EXAM CONSISTS OF 23 QUESTIONS AND 12 PAGES.
- ANSWER ALL THE QUESTIONS AND PLACE THEM IN THE TABLE ABOVE.
- CIRCLE ONE ANSWER FOR EACH QUESTION.
- SHOW ALL YOUR CALCULATIONS.
- USE THE EXAM PAGES TO SOLVE THE QUESTIONS.
- YOU CAN'T BORROW ANYTHING FROM ANY STUDENT.

1. The main purpose of descriptive statistics is to:
  - A) Summarize data in a useful and informative manner.
  - B) Make inferences about a population.
  - C) Determine if the data adequately represents the population.
  - D) Gather or collect data
  
2. Which of the following is an example of a continuous variable?
  - A) Family income
  - B) Number of students in a statistics class
  - C) Zip codes of shoppers
  - D) Rankings of baseball teams in a league
  
3. The incomes of a group of 50 loan applicants are obtained. Which level of measurement is income?
  - A) Nominal
  - B) Ordinal
  - C) Interval
  - D) Ratio
  
4. A questionnaire contained a question regarding marital status. The respondent checked either single, married, divorced, separated or widowed. What is the scale of measurement for this question?
  - A) Ratio
  - B) Interval
  - C) Ordinal
  - D) Nominal

**Use the following to answer questions 5-7:**

Refer to the following distribution of ages:

| Ages        | Number |
|-------------|--------|
| 40 up to 50 | 10     |
| 50 up to 60 | 28     |
| 60 up to 70 | 12     |

5. For the distribution of ages above, what is the relative class frequency for the lowest class?

- A) 50%
- B) 18%
- C) 20%**
- D) 10%

6. What is the class interval?

- A) 9
- B) 10**
- C) 10.5
- D) 11

7. What is the class midpoint of the highest class?

- A) 54
- B) 55**
- C) 64
- D) 65

8. A sample of 9 companies revenue in billion riyals is given by:

|     |     |     |     |     |     |     |     |     |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|
| 8.3 | 5.9 | 4.8 | 4.1 | 3.4 | 3.6 | 2.5 | 2.7 | 6.7 |
|-----|-----|-----|-----|-----|-----|-----|-----|-----|

The mean and standard deviation of the companies revenue are:

- (a)  $\bar{X} = 2.50$ ,  $s = 3.82$
- (b)  $\bar{X} = 3.82$ ,  $s = 4.67$
- (c)  $\bar{X} = 4.67$ ,  $s = 1.95$**
- (d)  $\bar{X} = 42.0$ ,  $s = 2.54$

9. The net annual sales of a sample of small retail clothing stores were organized into the following relative frequency distribution.

| Net Sales (in \$ millions) | Percent of Total |
|----------------------------|------------------|
| 1 up to 4                  | 13               |
| 4 up to 7                  | 14               |
| 7 up to 10                 | 40               |
| 10 up to 13                | 23               |
| 13 or more                 | 10               |

What is the mean net sales (in \$ millions)?

- A) \$7.09
  - B) \$10.09
  - C) \$8.59
  - D) \$8.325
10. In a scatter diagram, we describe the relationship between
- A) two variables measured at the ordinal level
  - B) two variables, one measured as an ordinal variable and the other as a ratio variable
  - C) two variables measured at the interval or ratio level
  - D) a variable measure on the interval or ratio level and time
11. What statistics are needed to draw a box plot?
- A) Minimum, maximum, median, first and third quartiles
  - B) Median, mean and standard deviation
  - C) A median and an interquartile range
  - D) A mean and a standard deviation
12. When are two events mutually exclusive?
- A) They overlap on a Venn diagram
  - B) If one event occurs, then the other cannot
  - C) Probability of one affects the probability of the other
  - D) Both (a) and (b)

**Use the following to answer questions 13-15:**

Each salesperson in a large department store chain is rated on their sales ability and their potential for advancement. The data for the 500 sampled salespeople are summarized in the following table.

|               |               | Potential for Advancement |      |           |
|---------------|---------------|---------------------------|------|-----------|
|               |               | Fair                      | Good | Excellent |
| Sales Ability | Below Average | 16                        | 12   | 22        |
|               | Average       | 45                        | 60   | 45        |
|               | Above Average | 93                        | 72   | 135       |

13. What is the probability that a salesperson selected at random has above average sales ability and is an excellent potential for advancement?
- A) 0.20  
B) 0.50  
C) 0.27  
D) 0.75
14. What is the probability that a salesperson selected at random will have average sales ability and good potential for advancement?
- A) 0.09  
B) 0.12  
C) 0.30  
D) 0.525
15. What is the probability that a salesperson selected at random will have below average sales ability and fair potential for advancement?
- A) 0.032  
B) 0.10  
C) 0.16  
D) 0.32
16. In a large metropolitan area, past records revealed that 30 percent of all the high school graduates go to college. From 20 graduates selected at random, what is the probability that exactly 8 will go to college?
- A) 0.114  
B) 0.887  
C) 0.400  
D) 0.231

**Use the following to answer questions 17-19:**

A statistics professor receives an average of five e-mail messages per day from students. Assume the number of messages approximates a Poisson distribution.

17. What is the probability that on a randomly selected day she will have no messages?

- A) 0.0067
- B) zero
- C) 0.0335
- D) Impossible to have no messages

18. What is the probability that on a randomly selected day she will have five messages?

- A) 0.0067
- B) 0.875
- C) 0.175
- D) 1.0

19. What is the probability that on a randomly selected day she will have two messages?

- A) 0.0067
- B) 0.0014
- C) 0.420
- D) 0.084

**use the following to answer 20-23:**

Married men were asked to specify which type of saving they used. The following table shows the 100 responses cross-classified by educational level of the respondent.

| saving method | Educational Level  |                |                        | Total |
|---------------|--------------------|----------------|------------------------|-------|
|               | High School<br>(A) | College<br>(B) | Graduate School<br>(C) |       |
| S             | 15                 | 8              | 7                      | 30    |
| T             | 3                  | 7              | 20                     | 30    |
| V             | 5                  | 5              | 15                     | 25    |
| W             | 10                 | 3              | 2                      | 15    |
| Total         | 33                 | 23             | 44                     | 100   |

20. The probability that a randomly selected man will be using saving method V :

- (a) 0.05      (b) 0.25      (c) 0.33      (d) 0.20      (e) 0.15

21. The probability that a randomly selected man will have College :

- (a) 0.08      (b) 0.07      (c) 0.23      (d) 0.05      (e) 0.03

22. The probability that a randomly selected man will be using saving method T or have High School is:

- (a) 0.30      (b) 0.33      (c) 0.09      (d) 0.60      (e) 0.10

23. The probability that a randomly selected man will be using saving method **W** and have Graduate School is:

- (a) 0.02      (b) 0.10      (c) 0.44      (d) 0.13      (e) 0.05

With my best wishes.

## Formulae

$$\text{SAMPLE MEAN} \quad \bar{X} = \frac{\sum X}{n} \quad [3-2]$$

$$\text{GEOMETRIC MEAN} \quad GM = \sqrt[n]{(X_1)(X_2) \cdots (X_n)} \quad [3-4]$$

$$\text{MEAN DEVIATION} \quad MD = \frac{\sum |X - \bar{X}|}{n} \quad [3-7]$$

$$\text{SAMPLE STANDARD DEVIATION} \quad s = \sqrt{\frac{\sum (X - \bar{X})^2}{n - 1}} \quad [3-11]$$

**CHEBYSHEV'S THEOREM** For any set of observations (sample or population), the proportion of the values that lie within  $k$  standard deviations of the mean is at least  $1 - 1/k^2$ , where  $k$  is any constant greater than 1.

$$1 - \frac{1}{k^2} = 1 - \frac{1}{(3.5)^2} = 1 - \frac{1}{12.25} = 0.92$$

$$\text{ARITHMETIC MEAN OF GROUPED DATA} \quad \bar{X} = \frac{\sum fM}{n} \quad [3-12]$$

where:

- $\bar{X}$  is the designation for the sample mean.
- $M$  is the midpoint of each class.
- $f$  is the frequency in each class.
- $fM$  is the frequency in each class times the midpoint of the class.
- $\sum fM$  is the sum of these products.
- $n$  is the total number of frequencies.

$$\text{STANDARD DEVIATION, GROUPED DATA} \quad s = \sqrt{\frac{\sum f(M - \bar{X})^2}{n - 1}} \quad [3-13]$$

where:

- $s$  is the symbol for the sample standard deviation.
- $M$  is the midpoint of the class.
- $f$  is the class frequency.
- $n$  is the number of observations in the sample.
- $\bar{X}$  is the designation for the sample mean.

$$\text{LOCATION OF A PERCENTILE} \quad L_p = (n + 1) \frac{P}{100} \quad [4-1]$$

$$\text{PEARSON'S COEFFICIENT OF SKEWNESS} \quad sk = \frac{3(\bar{X} - \text{Median})}{s} \quad [4-2]$$

$$\text{CLASSICAL PROBABILITY} \quad \text{Probability of an event} = \frac{\text{Number of favorable outcomes}}{\text{Total number of possible outcomes}} \quad [5-1]$$

**GENERAL RULE OF MULTIPLICATION**

$$P(A \text{ and } B) = P(A)P(B|A)$$

[5-6]

$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$

$$P(A) = 1 - P(\sim A).$$

**BAYES' THEOREM**

$$P(A_i|B) = \frac{P(A_i)P(B|A_i)}{P(A_1)P(B|A_1) + P(A_2)P(B|A_2)}$$

[5-7]

**PERMUTATION FORMULA**

$${}_n P_r = \frac{n!}{(n-r)!}$$

[5-9]

**COMBINATION FORMULA**

$${}_n C_r = \frac{n!}{r!(n-r)!}$$

[5-10]

**MEAN OF A PROBABILITY DISTRIBUTION**

$$\mu = \sum[xP(x)]$$

[6-1]

**VARIANCE OF A PROBABILITY DISTRIBUTION**

$$\sigma^2 = \sum[(x - \mu)^2 P(x)]$$

[6-2]

**BINOMIAL PROBABILITY FORMULA**

$$P(x) = {}_n C_x \pi^x (1 - \pi)^{n-x}$$

$$P(x) = \frac{{}_s C_x (W-s) C_{n-x}}{{}_N C_n}$$

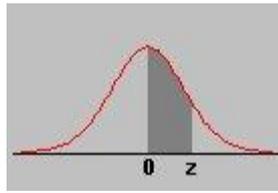
**POISSON DISTRIBUTION**

$$P(x) = \frac{\mu^x e^{-\mu}}{x!}$$

[6-7]

$$Z = \frac{X - \mu}{\sigma}$$

Area between 0 and z



|     | 0      | 0.01   | 0.02   | 0.03   | 0.04   | 0.05   | 0.06   | 0.07   | 0.08   | 0.09   |
|-----|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 0   | 0      | 0.004  | 0.008  | 0.012  | 0.016  | 0.0199 | 0.0239 | 0.0279 | 0.0319 | 0.0359 |
| 0.1 | 0.0398 | 0.0438 | 0.0478 | 0.0517 | 0.0557 | 0.0596 | 0.0636 | 0.0675 | 0.0714 | 0.0753 |
| 0.2 | 0.0793 | 0.0832 | 0.0871 | 0.091  | 0.0948 | 0.0987 | 0.1026 | 0.1064 | 0.1103 | 0.1141 |
| 0.3 | 0.1179 | 0.1217 | 0.1255 | 0.1293 | 0.1331 | 0.1368 | 0.1406 | 0.1443 | 0.148  | 0.1517 |
| 0.4 | 0.1554 | 0.1591 | 0.1628 | 0.1664 | 0.17   | 0.1736 | 0.1772 | 0.1808 | 0.1844 | 0.1879 |
| 0.5 | 0.1915 | 0.195  | 0.1985 | 0.2019 | 0.2054 | 0.2088 | 0.2123 | 0.2157 | 0.219  | 0.2224 |
| 0.6 | 0.2257 | 0.2291 | 0.2324 | 0.2357 | 0.2389 | 0.2422 | 0.2454 | 0.2486 | 0.2517 | 0.2549 |
| 0.7 | 0.258  | 0.2611 | 0.2642 | 0.2673 | 0.2704 | 0.2734 | 0.2764 | 0.2794 | 0.2823 | 0.2852 |
| 0.8 | 0.2881 | 0.291  | 0.2939 | 0.2967 | 0.2995 | 0.3023 | 0.3051 | 0.3078 | 0.3106 | 0.3133 |
| 0.9 | 0.3159 | 0.3186 | 0.3212 | 0.3238 | 0.3264 | 0.3289 | 0.3315 | 0.334  | 0.3365 | 0.3389 |
| 1   | 0.3413 | 0.3438 | 0.3461 | 0.3485 | 0.3508 | 0.3531 | 0.3554 | 0.3577 | 0.3599 | 0.3621 |
| 1.1 | 0.3643 | 0.3665 | 0.3686 | 0.3708 | 0.3729 | 0.3749 | 0.377  | 0.379  | 0.381  | 0.383  |
| 1.2 | 0.3849 | 0.3869 | 0.3888 | 0.3907 | 0.3925 | 0.3944 | 0.3962 | 0.398  | 0.3997 | 0.4015 |
| 1.3 | 0.4032 | 0.4049 | 0.4066 | 0.4082 | 0.4099 | 0.4115 | 0.4131 | 0.4147 | 0.4162 | 0.4177 |
| 1.4 | 0.4192 | 0.4207 | 0.4222 | 0.4236 | 0.4251 | 0.4265 | 0.4279 | 0.4292 | 0.4306 | 0.4319 |
| 1.5 | 0.4332 | 0.4345 | 0.4357 | 0.437  | 0.4382 | 0.4394 | 0.4406 | 0.4418 | 0.4429 | 0.4441 |
| 1.6 | 0.4452 | 0.4463 | 0.4474 | 0.4484 | 0.4495 | 0.4505 | 0.4515 | 0.4525 | 0.4535 | 0.4545 |
| 1.7 | 0.4554 | 0.4564 | 0.4573 | 0.4582 | 0.4591 | 0.4599 | 0.4608 | 0.4616 | 0.4625 | 0.4633 |
| 1.8 | 0.4641 | 0.4649 | 0.4656 | 0.4664 | 0.4671 | 0.4678 | 0.4686 | 0.4693 | 0.4699 | 0.4706 |
| 1.9 | 0.4713 | 0.4719 | 0.4726 | 0.4732 | 0.4738 | 0.4744 | 0.475  | 0.4756 | 0.4761 | 0.4767 |
| 2   | 0.4772 | 0.4778 | 0.4783 | 0.4788 | 0.4793 | 0.4798 | 0.4803 | 0.4808 | 0.4812 | 0.4817 |
| 2.1 | 0.4821 | 0.4826 | 0.483  | 0.4834 | 0.4838 | 0.4842 | 0.4846 | 0.485  | 0.4854 | 0.4857 |
| 2.2 | 0.4861 | 0.4864 | 0.4868 | 0.4871 | 0.4875 | 0.4878 | 0.4881 | 0.4884 | 0.4887 | 0.489  |
| 2.3 | 0.4893 | 0.4896 | 0.4898 | 0.4901 | 0.4904 | 0.4906 | 0.4909 | 0.4911 | 0.4913 | 0.4916 |
| 2.4 | 0.4918 | 0.492  | 0.4922 | 0.4925 | 0.4927 | 0.4929 | 0.4931 | 0.4932 | 0.4934 | 0.4936 |
| 2.5 | 0.4938 | 0.494  | 0.4941 | 0.4943 | 0.4945 | 0.4946 | 0.4948 | 0.4949 | 0.4951 | 0.4952 |
| 2.6 | 0.4953 | 0.4955 | 0.4956 | 0.4957 | 0.4959 | 0.496  | 0.4961 | 0.4962 | 0.4963 | 0.4964 |
| 2.7 | 0.4965 | 0.4966 | 0.4967 | 0.4968 | 0.4969 | 0.497  | 0.4971 | 0.4972 | 0.4973 | 0.4974 |
| 2.8 | 0.4974 | 0.4975 | 0.4976 | 0.4977 | 0.4977 | 0.4978 | 0.4979 | 0.4979 | 0.498  | 0.4981 |
| 2.9 | 0.4981 | 0.4982 | 0.4982 | 0.4983 | 0.4984 | 0.4984 | 0.4985 | 0.4985 | 0.4986 | 0.4986 |
| 3   | 0.4987 | 0.4987 | 0.4987 | 0.4988 | 0.4988 | 0.4989 | 0.4989 | 0.4989 | 0.499  | 0.499  |