

PHYS 500-FALL 2019
Homework 3

1. In an experiment to study the behaviour of silicon diodes when they are cooled, the voltage across a diode was measured as a function of the diode temperature. We got the following data after 8 measurements.

| Recordings | Temperature (K) | Voltage (V) |
|------------|-----------------|-------------|
| 1 | 300 | 0.630 |
| 2 | 290 | 0.653 |
| 3 | 280 | 0.670 |
| 4 | 270 | 0.678 |
| 5 | 260 | 0.695 |
| 6 | 250 | 0.705 |
| 7 | 240 | 0.735 |
| 8 | 230 | 0.748 |

Apply the method of least squares to determine the best fit line $V=BT+A$. This is to determine A and B and their errors. V is for voltage and T for temperature. (15 marks)

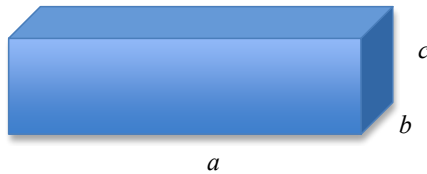
2. We measure the sides of the slab, shown in figure below and we found:

$$a = (9.0 \pm 0.3) \text{ mm}, \quad b = (3.0 \pm 0.3) \text{ mm}, \quad c = (2.0 \pm 0.3) \text{ mm}.$$

a) Calculate the volume of the slab (1 marks).

b) Calculate the error of the volume (2 marks).

c) Quote the final result (volume \pm error) after making all the necessary roundings (2 marks).



ANSWERS:

1)

$$y = Bx + A$$

by applying the method we get:

$$A = 1.117666667, \quad B = -0.001616666667 \text{ and}$$

$$\delta A = 0.02577008348, \quad \delta B = 0.00009191884367$$

So we write:

$$A = (1.12 \pm 0.03)V \text{ and } B = (-0.00162 \pm 0.00009)VK^{-1}$$

Vasileios Lembessis 9/11/2019 09:19

Comment [1]: Some of you calculated average values and made plots. I did not ask for it.

2) (a) The volume is given by $V = abc$

$$a = (9.0 \pm 0.3)mm, \quad b = (3.0 \pm 0.3)mm, \quad c = (2.0 \pm 0.3)mm$$

$$V = abc = 3 \times 9 \times 2 \text{ mm}^3 = 54 \text{ mm}^3$$

(b) The error of the volume is given by

$$\begin{aligned} \delta V &= \sqrt{\left(\frac{\partial V}{\partial a} \delta a\right)^2 + \left(\frac{\partial V}{\partial b} \delta b\right)^2 + \left(\frac{\partial V}{\partial c} \delta c\right)^2} = \\ &= \sqrt{[bc\delta a]^2 + [ac\delta b]^2 + [ab\delta c]^2} = \\ &= 9.9 \text{ mm}^3 \end{aligned}$$

Thus to correct number of significant figure it becomes $\delta V = 10 \text{ mm}^3$

(c) $V = (54 \pm 10) \text{ mm}^3$

Vasileios Lembessis 9/11/2019 09:20

Comment [2]: Some of you wrote or send me by email correction to 50 ± 10 . This is a mistake.