


FIRST MID TERM EXAMINATION, OCTOBER 30, 2017  
DEPARTMENT OF MATHEMATICS  
KING SAUD UNIVERSITY  
MATH - 240 FULL MARK: 25 TIME: 2 HOUR 

1. Let  $A$  be the matrix

$$\mathbf{A} = \begin{pmatrix} 3 & 1 \\ 2 & 1 \end{pmatrix}.$$

If  $f(x) = x^3 - 2x + 4$ , then find  $f(A)$ .

2. What conditions must  $b_1$ ,  $b_2$ , and  $b_3$  satisfy in order for the system of equations

$$\begin{aligned} x_1 + x_2 + 2x_3 &= b_1 \\ x_1 + x_3 &= b_2 \\ 2x_1 + x_2 + 3x_3 &= b_3 \end{aligned}$$

to be consistent.

3. Evaluate the following determinant by reducing to row echelon form.

$$\begin{vmatrix} 2 & 1 & 3 & 1 \\ 1 & 0 & 1 & 1 \\ 0 & 2 & 1 & 0 \\ 0 & 1 & 2 & 3 \end{vmatrix}$$

4. Solve the following system of linear equations by using Cramer's rule

$$\begin{aligned} 4x + 5y &= 2 \\ 11x + y + 2z &= 3 \\ x + 5y + 2z &= 1. \end{aligned}$$

5. Determine whether the vectors  $\mathbf{v}_1 = (2, -1, 3)$ ,  $\mathbf{v}_2 = (4, 1, 2)$ , and  $\mathbf{v}_3 = (8, -1, 8)$  span  $\mathbb{R}^3$ .

6. Determine whether the following vectors in  $\mathbb{R}^3$

$\mathbf{v}_1 = (-3, 0, 4)$ ,  $\mathbf{v}_2 = (5, -1, 2)$ , and  $\mathbf{v}_3 = (1, 1, 3)$  form a linearly independent set or linearly dependent set.