

Time: 1h 30 min

Instructions: Calculators are **not** allowed.

Question 1 (3+2 Marks):

1. Use Riemann sum to evaluate the definite integral $\int_{-1}^1 (3x^2 + 2)dx$.
2. Find $F'(0)$, if $F(x) = \int_{\cos(\sqrt{x+1})}^{e^{x^2}} \frac{1}{1-t^2} dt$.

Question 2 (2+2 Marks): Find $\frac{dy}{dx}$ if

1. $y(x) = \cos^{-1}\left(\frac{1}{2^{3^x}}\right) + x^2 \log_2(\sqrt[5]{x^4 + 2})$.
2. $y(x) = (\sin x)^{\sqrt{x}}$.

Question 3: Evaluate the following integrals (2 Marks for each integral)

1. $\int \frac{x^2 + 4}{\sqrt[3]{x}} dx$.
2. $\int \frac{\cos x}{(1 + \sin x)^4} dx$.
3. $\int \frac{\sec(x^{\frac{2}{5}}) \tan(x^{\frac{2}{5}})}{x^{\frac{3}{5}}} dx$.
4. $\int \frac{1}{\sqrt{x}(1 + \sqrt{x})} dx$.
5. $\int_0^1 \frac{x}{x+1} dx$.
6. $\int \ln x e^{-\ln(2x)} dx$.
7. $\int \frac{1}{e^{-x} + e^x} dx$.
8. $\int \frac{2^x}{\sqrt{4^{2^x} - 9}} dx$.