Department of Statistics \& Operations Research College of Science, King Saud University

## STAT 145

Final Examination
Second Semester 1431 - 1432 H


|  |  | \|سم الطالب |
| :---: | :---: | :---: |
|  | رقم التّضير | الرقّ الجامعى |
|  | اسم الاكتور | رقم الشعبة |

- Mobile Telephones are not allowed in the classrooms.
- Time allowed is $\mathbf{3}$ Hours.
- Answer all questions.
- Choose the nearest number to your answer.
- For each question, put the code (Capital Letters) of the correct answer in the following table beneath the question number. Do not use pencil or red pens.

| $\mathbf{1}$ | $\mathbf{2}$ | $\mathbf{3}$ | $\mathbf{4}$ | $\mathbf{5}$ | $\mathbf{6}$ | $\mathbf{7}$ | $\mathbf{8}$ | $\mathbf{9}$ | $\mathbf{1 0}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| A | D | A | C | A | C | B | C | B | D |
| $\mathbf{1 1}$ | $\mathbf{1 2}$ | $\mathbf{1 3}$ | $\mathbf{1 4}$ | $\mathbf{1 5}$ | $\mathbf{1 6}$ | $\mathbf{1 7}$ | $\mathbf{1 8}$ | $\mathbf{1 9}$ | $\mathbf{2 0}$ |
| B | D | B | A | B | A | A | B | C | A |
| 21 | $\mathbf{2 2}$ | $\mathbf{2 3}$ | $\mathbf{2 4}$ | $\mathbf{2 5}$ | $\mathbf{2 6}$ | $\mathbf{2 7}$ | $\mathbf{2 8}$ | $\mathbf{2 9}$ | $\mathbf{3 0}$ |
| C | D | B | C | A | B | B | A | D | D |
| $\mathbf{3 1}$ | $\mathbf{3 2}$ | $\mathbf{3 3}$ | $\mathbf{3 4}$ | $\mathbf{3 5}$ | $\mathbf{3 6}$ | $\mathbf{3 7}$ | $\mathbf{3 8}$ | $\mathbf{3 9}$ | 40 |
| A | C | C | B | A | D | D | C | B | A |
| 41 | $\mathbf{4 2}$ | $\mathbf{4 3}$ | $\mathbf{4 4}$ | $\mathbf{4 5}$ | $\mathbf{4 6}$ | $\mathbf{4 7}$ | $\mathbf{4 8}$ | 49 | $\mathbf{5 0}$ |
| B | C | C | B | B | B | B | B | C | A |


| Term Marks | Final Exam. Marks | Total Marks |
| :--- | :--- | :--- |
|  |  |  |

## >>>

Following are the weights (in kg ) for a sample of 6 children. $13,20,18,12,15$, and 12.
(1) The mean of the data is:

| A) 12 | B) | 15 | C) | 10 | D) | 18 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(2) The median of the data is:

| A) | 17 | B) | 12 | C) | 10 | D) | $\underline{14}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(3) The mode of the data is:
A) $\underline{12}$
B) 20
C) 15
D) 2
(4) The variance of the data is:

| A) | 3.347 | B) | 3.055 | C) | $\underline{11.200}$ | D) | 9.333 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(5) The coefficient of variation (C.V.) of the data is:

| A) $22.3 \%$ | B) | $17.4 \%$ | C) | $74.7 \%$ | D) | $62.22 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

>>>
Temperatures recorded at 2 pm for 5 days of a year, for a city are:

$$
7, \quad 4, \quad 0, \quad-5, \quad \text { and } \quad 40 .
$$

(6) The range of temperatures is:
A) 33
B) 40
C) $\underline{\underline{45}}$
D) 5
(7) The most suitable measure of centre for the data is:

| A) | Mean | B) | Median | C) | Mode | D) | Range |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

"»>
Let $A$ and $B$ denote two events defined on the same sample space with $P(A)=0.6, P(B)=$ 0.4 , and $P(A \cup B)=0.74$, then:
(8) The events A and B are:

| A) | independent | B) | mutually <br> exclusive | C) | dependent | D) | impossible |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(9) The $P(\bar{A} \cup \bar{B})$ is:

| A) | 0.18 |
| :--- | :--- |

B) $\underline{0.26}$
C) 0.50
(D) 1.00

## »»

Consider the following cumulative frequency distribution table for the ages of all workers in a certain factory.

| Age | Cumulative frequency |
| :--- | :---: |
| $26-35$ | 10 |
| $36-45$ | 40 |
| $46-55$ | 50 |

(10) Percentage of workers in the age group 36-45 is:

| A) | $40 \%$ | B) | $80 \%$ | C) | $30 \%$ | D) | $60 \%$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(11) Number of workers having age 36 or more is:

| A) | 90 | B) | $\underline{40}$ | C) | 10 | D) | 50 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(12) The true class limits for the first class are:

| A) | $26-35$ | B) | $21.5-35.5$ | C) | $25.5-34.5$ | D) | $\underline{25.5-35.5}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

>>>
Let $A$ and $B$ be two independent events. Suppose that $P(A)=0.6$ and $P(B)=0.3$ then
(13) $P(\bar{A} \cap B)$ equals:

| A) | 0.08 | B) | $\underline{0.12}$ | C) | 0.20 | D) | 0.42 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(14) $P(A \cup B)$ equals:
A) $\underline{0.72}$
B) 0.90
C) 0.10
D) 0.7
>>>
Suppose that a town has $20 \%$ of men known to have a certain disease. A certain medical test is applied to randomly selected 500 men. The following data is obtained.

|  | Disease |  |  |
| :--- | :---: | :---: | :---: |
| Test | Present | Absent | Total |
| Positive | $\mathbf{8 2}$ | $\mathbf{8 0}$ | $\mathbf{1 6 2}$ |
| Negative | $\mathbf{3 8}$ | $\mathbf{3 0 0}$ | $\mathbf{3 3 8}$ |
| Total | $\mathbf{1 2 0}$ | $\mathbf{3 8 0}$ | $\mathbf{5 0 0}$ |

Let an individual be selected at random from the sample.
(15) The probability that the selected person has the disease is:
A) 0.20
B) $\underline{0.24}$
C) 0.68
D) 0.32
(16) The probability that the test gives a false negative result is:

| A) | $\underline{0.32}$ | B) | 0.68 | C) | 0.21 | D) | 0.79 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(17) The sensitivity of the test is:

| A) | $\underline{0.68}$ | B) | 0.16 | C) | 0.51 | D) | 0.79 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(18) Suppose that $20 \%$ of men in the town have the disease, the predictive probability negative for the test is:

| A) | 0.37 | B) | $\underline{0.62}$ | C) | 0.09 | D) | 0.89 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

»"»
In a large population of people, $34 \%$ have blood type A+. If we randomly choose 8 persons from this population and let $X=$ the number in the $\mathbf{8}$ chosen that with blood type A+.
(19) The values of the parameters of the distribution are:
A) 3 and 0.34
B) 8 , and 0.66
C) 8 and 0.34
D) 8 and 34
(20) The probability that there is exactly one person with blood type A+:
A) $\underline{0.1484}$
B) 0.0028
C) 0.3400
D) 0.0185
(21) The probability that there is at least one person with blood type A+:

| A) | 0.1484 | B) | 0.1844 | C) | $\underline{0.9640}$ | D) | 0.0360 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

>>>
The number of serious surgical operations that are performed in a hospital during a day follows a Poisson distribution with an average of 5 persons per day, then:
(22) The probability that no operations is performed in the next day is:

| A) | 0.99996 | B) | $\underline{0.0067}$ | C) | 0.54210 | D) | 0.08972 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(23) The probability that 5 operations are performed in the next day is:

| A) | 0.2145 | B) | 0.8521 | C) | $\underline{0.175}$ | D) | 0.5124 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(24) The average number of operations that are performed in two days is:

| A) 20 | B) | $\underline{10}$ | C) | 5 | D) | 30 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |

>>>
In a population of people, $X=$ the body mass index (in $\mathrm{kg} / \mathrm{m}^{2}$ ) is normally distributed with mean $\mu=25$ and standard deviation $\sigma=2$. For a randomly chosen person,
(25) $\mathrm{P}(24<\mathrm{X}<26)=$
A) 0.6915
B) $\underline{\underline{0.3830}}$
C) 0.2085
D) 1 1
(26) $\mathrm{P}(\mathrm{X}>21)=$

| A) $\underline{0.9772}$ B) 0.0228 C) 1 D) (27) $\mathrm{P}(\mathrm{X}=21)=$ <br> A) 0.9772$\quad$ B) 00.0228 |
| :--- |

B) 0.0228
C) 1
D) $\underline{0}$
(28) Find the value of k such that $\mathrm{P}(\mathrm{X}>\mathrm{k})=0.2578$.

| A) | 0.257 | B) | 25 | C) | -0.65 | D) | 26.3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

## >>

A sample of size 100 is taken from a population having a proportion $p_{1}=0.8$. Another independent sample of size 400 is taken from a population having a proportion $p_{2}=0.5$.
(29) The sampling distribution for the difference in sample proportions has a mean equals:
A) $\underline{0.3}$
B) 1.3
C) 0
D) 0.8
(30) The sampling distribution for the difference in sample proportions has a standard error equals:

| A) 0.015 | B) |
| :--- | :--- | :--- |
| (31) $\mathrm{P}\left(\hat{p}_{1}-\hat{p}_{2}<0.2\right)=$ : |  |
| A) 0.4423 | B |


| A) | 0.4423 | B) | 0.993 | C) | $\underline{0.0166}$ | D) | 0.2415 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

## "»»

Suppose it has been established that for a certain type of client the average length of a home visit by a public health nurse is $\mathbf{4 5}$ minutes with a standard deviation of $\mathbf{1 5}$ minutes, and that for a second type of client the average home visit is 30 minutes with a standard deviation of $\mathbf{2 0}$ minutes. If a nurse randomly visits $\mathbf{3 5}$ clients from the first population and 40 from the second population, then
(32) The mean of the difference between two sample means is:

| A) 5 | B) | 15 | C) | 20 | D) | 35 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(33) The standard deviation of the difference between two sample means is:

| A) | 4.0532 | B) | 16.4286 | C) | 8.2143 | D) | 0.5241 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(34) The probability that the average length of home visit will differ between the two groups by 20 or more is:

| A) | 0.8907 | B) | 0.4215 | C) | 0.5 | D) | $\underline{0.1093}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

## »»

A researcher wishes to determine if vitamin $E$ supplements could increase cognitive ability among elderly women. In 1999 the researcher recruits a sample of elderly women age 7580. At the time of the enrollment into the study, the women were randomized to either take Vitamin $E$, or a placebo for six months. At the end of the six month period, the women were given a cognition test. Higher scores on this test indicate better cognition. The mean of the test scores of 81 women who took vitamin $E$ supplements was $\bar{X}_{1}=27$, while the mean of the test scores of the 90 women who took placebo supplements was $\bar{X}_{2}=24$ Assuming the two populations follow approximately two different normal distributions with standard deviations, $\sigma_{1}=6.9$ and , $\sigma_{2}=6.2$, respectively.
(35) The point estimate for the difference between the two population means $\left(\mu_{1}-\mu_{2}\right)$ :

| A) 27 | B) | 24 | C) | 6.2 | D) | $\underline{3}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(36) The standard error for the difference between the two sample means $\left(\bar{X}_{1}-\bar{X}_{2}\right)$ :

| A) | 6.9 | B) | 6.2 | C) | $\underline{1.007}$ | D) | 3 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(37) A lower limit of a $95 \%$ C.I. for the difference between the two population means $\left(\mu_{1}-\mu_{2}\right):$

| A) | $\underline{1.0263}$ | B) | 4.9745 | C) | 5.9120 | D) |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |

">>
Six healthy three year old female sheep were injected with the antibiotic Gentamicin, at a dosage of $10 \mathrm{mg} / \mathrm{kg}$ body weight. Their blood serum concentrations ( $\mathrm{mg} / \mathrm{ml}$ ) of Gentamicin after injection were $33 ; 26 ; 34 ; 31 ; 23 ; 25$, the summary statistics for these data are

| $n$ | mean | Standard <br> deviation | SE(mean) |
| :---: | :---: | :---: | :---: |
| 6 | 28.67 | 4.59 | 1.87 |

Assuming the data follows approximately a normal distribution,
(38) The standard error of the sample mean is equal to:

| A) | 0.25 | B) | 1.87 | C) | 4.59 | D) | 28.67 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(39) At the $90 \%$, the ratability coefficient is equal to:

| A) | 2.33 | B) | $\underline{2.015}$ | C) | 3.215 | D) | 1.96 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(40) The $90 \%$ confidence interval for the population mean score on this test is:

| A) | $(27.412,30.145)$ | B) | $(24.48,29.10)$ | C) | $(24.902,32.438)$ | D) | $(32.48,39.55)$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(41) The test statistic for testing the hypotheses $H_{0}: \mu=30 v s H_{1}: \mu<30$ is equal to:

| A) | -2.2587 | B) | 2.5812 | C) | $\underline{-0.7112}$ | D) | 3.3412 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(42) At the 5\% significance level the critical region is :
A) $(-\infty,-2.015)$
B) $(-2.015,2.015)$
C) $(2.015, \infty)$
D) $(2.58, \infty)$
(43) At the 5\% significance level we are able to :

| A) | Reject $H_{0}$ | B) | Not to reject |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $H_{0}$ | C) | Decision is not possible |  |

>>>
A biostatistician , found that among 2000 boys ages 7 to 12 years. 400 were overweight. On the basis of this study:
(44) The standard error of the sample proportion of the overweight boys ages 7 to 12 years is:

| A) | 0.0500 | B) | $\underline{0.0089}$ | C) | 0.6587 | D) | 0.0221 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(45) The $99 \%$ upper confidence limit for the population proportion of the overweight boys ages 7 to12 years is:

| A) | 0.5000 | B) | $\underline{0.223}$ | C) | 0.6587 | D) | 0.0221 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(46) The test statistic for testing the hypotheses the proportion of boys ages 7 to 12 year does not equal 18 is:

| A) | -2.2587 | B) | $\underline{2.33}$ | C) | -0.7112 | D) | 3.3412 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(47) At the $5 \%$ significance level, can we conclude that more than $18 \%$ of boys ages 7 to 12 years are overweight:

| A) Yes | B) | No | C) | Decision is not possible |
| :--- | :--- | :--- | :--- | :--- |

>>>
A sample of 25 freshman nursing students made a mean score of $77.0 n$ a test designed to measure the attitude toward the dying patient. The sample standard deviation was 10. Assuming the data comes from a normal population,
(48) The statistical hypothesis for testing the hypothesis that the mean score is different than 80 is:

| A) | $H_{0}: \mu=80$ vs $H_{1}: \mu \neq 80$ | B) | $H_{0}: \mu=80$ vs $H_{1}: \mu<80$ |
| :--- | :--- | :--- | :--- |
| C) | $H_{0}: \mu=80$ vs $H_{1}: \mu>80$ | D) | $H_{0}: \mu=77$ vs $H_{1}: \mu<77$ |

(49) The test statistic for these statistical hypothesis is:

| A) -1.500 | B) | -2.025 | C) | 3.258 | D) | 0 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

(50) At the 5\% significance level we are able to :

| A) | Reject $H_{0}$ | B) | Not to reject $H_{0}$ | C) | Decision is not possible |
| :--- | :--- | :--- | :--- | :--- | :--- |

