# Final Exam, M-106, TM I, (2015-16), Department of Mathematics, King Saud University

#### 1. [2+2 Marks]

- 1.1) Find  $\frac{dy(x)}{dx}$  where  $y(x) = (5^x + 5^{-x})^5$ .
- 1.2) Evaluate the indefinite integral  $\int x^2 \sinh(x^3) dx$ .

#### 2. [3+3 Marks]

- 2.1) Determine whether the improper integral  $\int_{1}^{\infty} (1-x)e^{-x} dx$  converges or diverges, and evaluate it if it converges.
- 2.2) Evaluate the indefinite integral  $\int \cos^{11}(x) \sin^3(x) dx$ .

#### 3. [3+3+3 Marks]

- 3.1) Evaluate the indefinite integral  $\int \frac{5x^2+20x+6}{x^3+2x^2+x} dx$ .
- 3.2) Sketch the region bounded by the graphs of the equations  $x = 3 y^2$ , x = y + 1, and find its area.
- 3.3) Evaluate the indefinite integral  $\int \frac{x^2}{(1+x^2)^2} dx$ .

#### 4. [3+3 Marks]

- 4.1) Evaluate the indefinite integral  $\int \frac{x}{\sqrt{6x+1}} dx$ .
- 4.2) Evaluate the indefinite integral  $\int \frac{1}{\sqrt{8+2x-x^2}} dx$ .

### 5. [3+3 Marks]

- 5.1) Sketch the region R bounded by the graphs of the equations  $y = \sqrt{x}$ ,  $y = x^2$ , and find the volume of the solid generated by revolving R about the x -axis.
- 5.2) Find the arc length of the graph of the equation  $y(x) = \ln(\cos(x))$  from x = 0 to  $x = \frac{\pi}{4}$ .

## 6. **[5+4 Marks]**

- 6.1) Sketch the region which is outside the graph of the equation r=3 and inside the graph of the equation  $r=2+2\sin(\theta)$ , and find its area.
- Sketch the graph of the equation  $r=2\cos(\theta)$ , and find the area of the surface generated by revolving it about the line  $\theta=\frac{\pi}{2}$ .