

King Saud University
Department of Mathematics

2 Mid Term Exam

205-Math

2 Semester (1439/1440)

Question1 (4). Find the local extreme values of the function $f(x, y) = \frac{x^3}{3} - x + xy^2$

Question2 (4). Find the maximum and minimum values of the function $f(x, y) = x^2 + y$
on the circle $x^2 + y^2 = 9$.

Question3 (4). Evaluate the integral $\iint_R \frac{y}{1+x^2} dA$ over the region R bounded by the graphs:
 $y = 0$, $x = 1$ and $y = x$.

Question4 (3). Sketch the region of integration for the integral $\int_0^{\pi} \int_y^{\pi} y^2 \sin x^2 dx dy$
and write an equivalent integral with the order of integration reversed.

Question5 (4). Find the area of the plane region that is outside the curve $r = a$ and inside the
curve $r = 2a \cos \theta$ where $0 < a \in \mathfrak{R}$.

Question6 (3). Find the volume of the solid bounded by the surfaces:

$$z = \sqrt{25 - x^2 - y^2}, \quad z = 0 \quad \text{and} \quad x^2 + y^2 = 9$$

Question7 (3). Find the surface area of the surface $z = \sqrt{x^2 + y^2}$ that lies above the region R in
 xy -plane bounded by the circle $x^2 + y^2 = 9$.