King Saud University College of Applied Studies and Community Service Department of Natural Sciences



Quantum Theory of Light

General Physics II PHYS 111

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- In the Compton experiment, the wavelength of the scattered light is ______ the wavelength of the incident light.
- (A) longer than
- (B) the same as
- (C) shorter than

• Suppose visible light of wavelength = 5 x 10 m is used to determine the position of an electron to within the wavelength of the light. What is the minimum uncertainty in the electron's speed?

$$\Delta x \Delta p = \frac{h}{4\pi}.$$

With p = mv, and assuming negligible uncertainty in the mass of the electron, we find

$$\Delta v = \begin{vmatrix} h \\ 4\pi m \Delta x \end{vmatrix} = \frac{6.63 \times 10^{-34} \text{ J} \cdot \text{s}}{4\pi \cdot 9.11 \times 10^{-31} \text{ kg} \cdot 5 \times 10^{-7} \text{ m}} = 115.8 \frac{\text{m}}{\text{s}}.$$

Thus, the minimum uncertainty in the electron's speed is 115.8 m/s.

(a)Calculate the wavelength in meters of an electron traveling at 1.24 x10⁷ m/s. The mass of an electron is 9.11x 10⁻²⁸g.

(a)
$$m = 9.11 \times 10^{-28} \text{ g} \times \frac{1 \text{ kg}}{1000 \text{ g}} = 9.11 \times 10^{-31} \text{ kg}$$

Substituting into the de Broglie equation,

$$\lambda = \frac{h}{mv} = \frac{6.626 \times 10^{-34} \,\frac{\text{kg} \cdot \text{m}^2}{\text{s}}}{(9.11 \times 10^{-31} \,\text{kg}) \left(1.24 \times 10^7 \,\frac{\text{m}}{\text{s}}\right)} = 5.87 \times 10^{-11} \,\text{m}$$

• A green line of wavelength 4.86x10⁻¹⁹ m is observed in the emission spectrum of hydrogen. Calculate the energy of one photon of this green light.

$$E = \frac{bc}{\lambda} = \frac{(6.626 \times 10^{-34} \,\mathrm{J \cdot s})(3.00 \times 10^8 \,\mathrm{m/s})}{(4.86 \times 10^{-7} \,\mathrm{m})} = \frac{4.09 \times 10^{-19} \,\mathrm{J/photon}}{4.09 \times 10^{-19} \,\mathrm{J/photon}}$$

Planck's constant.....

- A) remains unknown to this day.
- **B**) is the inverse of Einstein's constant.
- C) is used to find the quantum energy associated with a certain frequency of light.

D) is not really constant since it varies from one part of the universe to another.

A light source of wavelength λ illuminates a metal and ejects photoelectrons with a maximum kinetic energy of 1.00 eV. A second light source with half the wavelength of the first ejects photoelectrons with a maximum kinetic energy of 4.00 eV.
Determine the work function of the metal.

$$K_1 = \frac{hc}{\lambda_1} - \phi$$

$$K_2 = \frac{hc}{\lambda_2} - \phi$$

where $\lambda_2 = 0.5 \lambda_1$, so
$$K_2 - 2K_1 = \phi$$

and therefore $\phi = 2 \text{ eV}$ when $K_1 = 1 \text{ eV}$ and $K_2 = 4 \text{ eV}$.

Which statement is TRUE?

- A) Light always behaves like a wave and electrons always behave like particles.
- B) Light always behaves like a particle and electrons always behave like waves.
- C) <u>Both light and electrons behave sometimes like</u> waves and sometimes like particles.
- D) Light and electrons never behave like waves or particles.

How many Joules of energy are contained in a photon with $\lambda = 550$ nm?

- Use $f = c / \lambda$ to get the frequency: $f = (3.00 \text{ x } 10^8 \text{ m/s}) / (550 \text{ x } 10^{-9} \text{ m}) = 5.4508 \text{ x } 10^{14} \text{ s}^{-1}$.
- Now use E = hv to get the energy: $E = (6.6260755 \text{ x } 10^{-34} \text{ J s}) (5.4508 \text{ x } 10^{14} \text{ s}^{-1})$ $= 3.612 \text{ x} 10^{-19} \text{ J}.$

What is the energy of a quantum of light with a frequency of 3.87×10^{19} Hz?

 $E = hf = (6.6260755 \text{ x } 10^{-34} \text{ J s}) (3.87 \text{ x } 10^{19} \text{ s}^{-1})$ = 2.56 x10⁻¹⁴J