

**King Saud University  
College of Science  
Physics & Astronomy Dept.**

**PHYS 111 (GENERAL PHYSICS 2)**

**CHAPTER 3: Vectors**

**LECTURE NO. 1**

**Presented by Nouf Saad Alkathran**

## 3.2 Vector and Scalar Quantities

**Scalar quantity:** is completely specified by a single value with an appropriate unit and has no direction. Such as volume, mass, speed, and time intervals.

**Vector quantity** is completely specified by a number and appropriate units plus a direction. Such as displacement, velocity, and forces.

➤ a vector quantity can be presented as  $A$ ,  $\vec{A}$ ,  $|\mathbf{A}|$ ,  $\vec{\mathbf{A}}$ .

**Quick Quiz 3.1** Which of the following are vector quantities and which are scalar quantities? (a) your age (b) acceleration (c) velocity (d) speed (e) mass

## 3.3 Some Properties of Vectors

- **Equality of Two Vectors**

if they have the same magnitude and point in the same direction.  $A = B$

- **Adding Vectors**

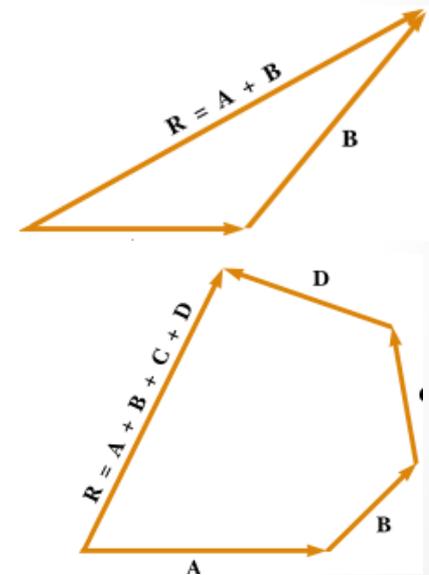
- Graphical methods

$$A+B=R$$

- Geometric construction

$$A+B+C+D= R$$

$R$  is the vector drawn from the tail of the first vector to the tip of the last vector.



## 3.3 Some Properties of Vectors

- Commutative law of addition:

$$\mathbf{A} + \mathbf{B} = \mathbf{B} + \mathbf{A}$$

- Associative law of addition:

$$\mathbf{A} + (\mathbf{B} + \mathbf{C}) = (\mathbf{A} + \mathbf{B}) + \mathbf{C}$$

### Negative of a Vector

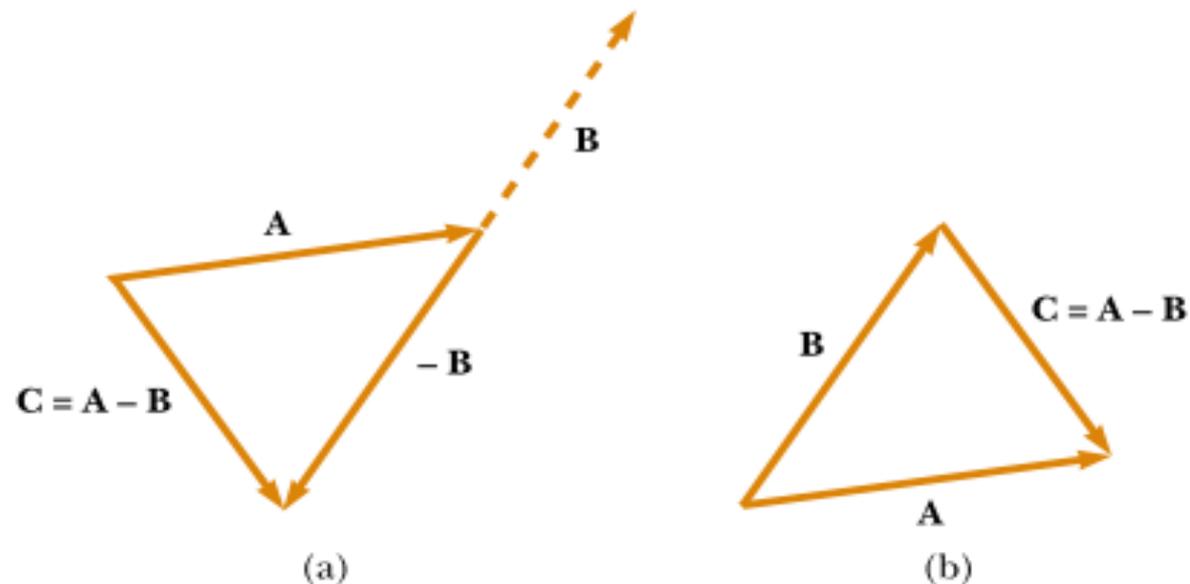
The negative of the vector  $A$  is defined as the vector that when added to  $A$  gives zero for the vector sum. That is,  $A + (-A) = 0$ .

## 3.3 Some Properties of Vectors

### Subtracting Vectors

**A - B** as vector **- B** added to vector **A**

$$\mathbf{A} - \mathbf{B} = \mathbf{A} + (-\mathbf{B})$$



**Figure 3.11** (a) This construction shows how to subtract vector **B** from vector **A**. The vector **- B** is equal in magnitude to vector **B** and points in the opposite direction. To subtract **B** from **A**, apply the rule of vector addition to the combination of **A** and **- B**: Draw **A** along some convenient axis, place the tail of **- B** at the tip of **A**, and **C** is the difference **A - B**. (b) A second way of looking at vector subtraction. The difference vector **C = A - B** is the vector that we must add to **B** to obtain **A**.

## 3.3 Some Properties of Vectors

- To find resultant ( $R$ ) resulting from two vectors  $A$ ,  $B$ , we use this equation:

$$R = \sqrt{A^2 + B^2 - 2AB \cos \theta}$$

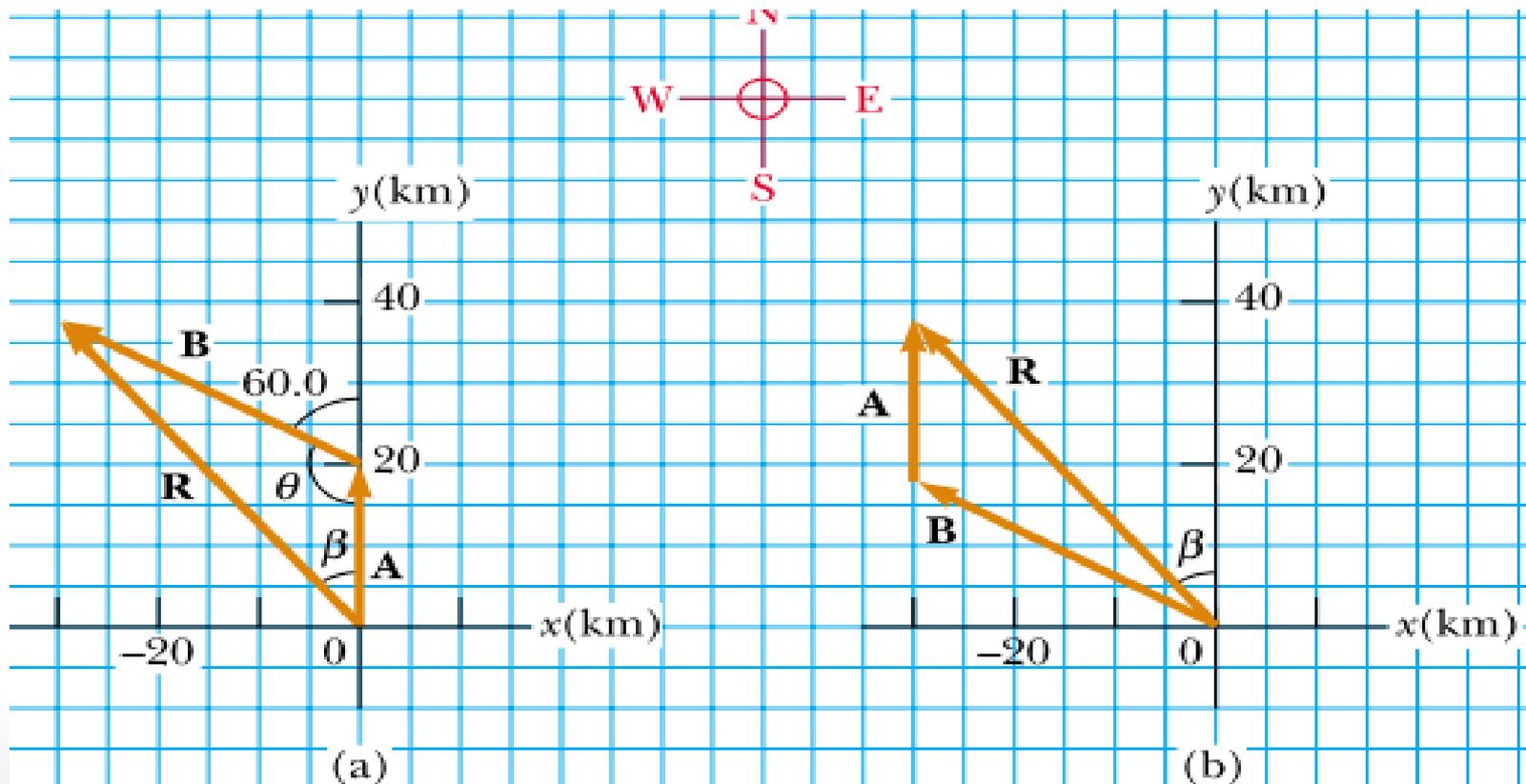
Where  $\theta$  is the angle between  $A$  and  $B$ .

- To find the angle  $\beta$  of the resultant  $R$ , we use this equation:

$$\frac{\sin \beta}{B} = \frac{\sin \theta}{R}$$

## Example 3.2

- A car travels 20.0 km due north and then 35.0 km in a direction  $60.0^\circ$  west of north, as shown in Figure 3.12a. Find the magnitude and direction of the car's resultant displacement.



## Solution 3.2

$$R = \sqrt{A^2 + B^2 - 2AB \cos \theta}$$

$$\text{With } \theta = 180^\circ - 60^\circ = 120^\circ$$

$$= \sqrt{(20.0 \text{ km})^2 + (35.0 \text{ km})^2 - 2(20.0 \text{ km})(35.0 \text{ km}) \cos 120^\circ}$$

$$= 48.2 \text{ km}$$

$$\frac{\sin \beta}{B} = \frac{\sin \theta}{R}$$

$$\sin \beta = \frac{B}{R} \sin \theta = \frac{35.0 \text{ km}}{48.2 \text{ km}} \sin 120^\circ = 0.629$$

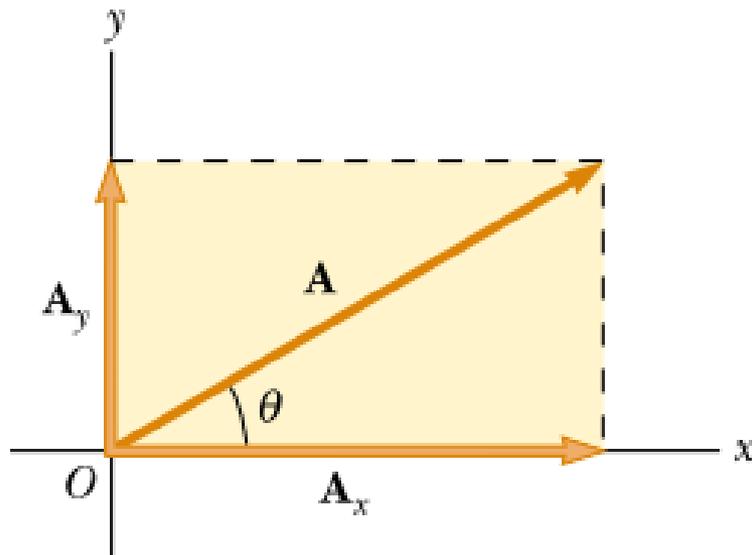
$$\beta = 39.0^\circ$$

# Quick Quiz

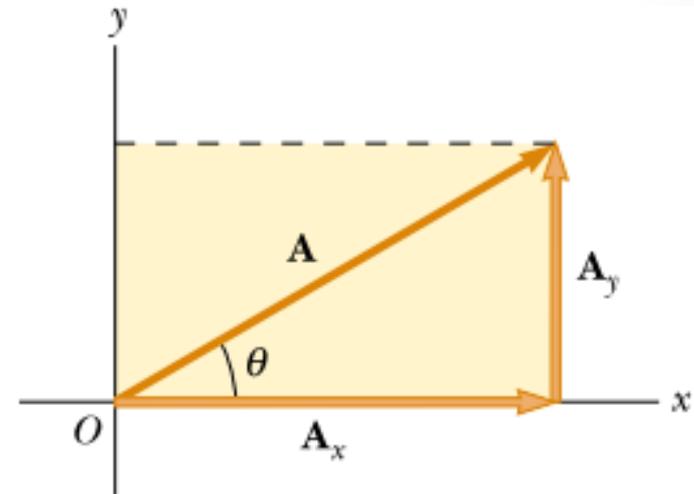
**Quick Quiz 3.2** The magnitudes of two vectors **A** and **B** are  $A = 12$  units and  $B = 8$  units. Which of the following pairs of numbers represents the *largest* and *smallest* possible values for the magnitude of the resultant vector  $\mathbf{R} = \mathbf{A} + \mathbf{B}$ ? (a) 14.4 units, 4 units (b) 12 units, 8 units (c) 20 units, 4 units (d) none of these answers.

**Quick Quiz 3.4** If vector **B** is added to vector **A**, which *two* of the following choices must be true in order for the resultant vector to be equal to zero? (a) **A** and **B** are parallel and in the same direction. (b) **A** and **B** are parallel and in opposite directions. (c) **A** and **B** have the same magnitude. (d) **A** and **B** are perpendicular.

## 3.4 Components of a Vector and Unit Vectors



(a)



(b)

$$\mathbf{A} = \mathbf{\hat{A}}_x + \mathbf{A}_y \quad A_x = A \cos \theta$$

$$A_y = A \sin \theta$$

$$A = \sqrt{A_x^2 + A_y^2}$$

$$\theta = \tan^{-1} \left( \frac{A_y}{A_x} \right)$$

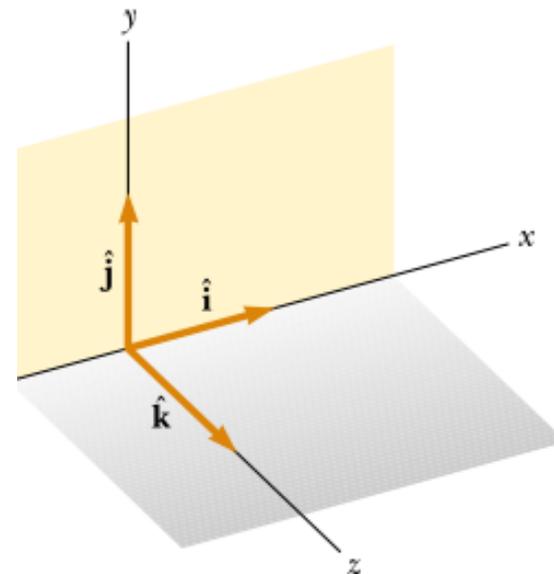
## 3.4 Components of a Vector and Unit Vectors

$A_x$ negative	$A_x$ positive
$A_y$ positive	$A_y$ positive
$A_x$ negative	$A_x$ positive
$A_y$ negative	$A_y$ negative

### Unit Vectors

$$|\hat{\mathbf{i}}| = |\hat{\mathbf{j}}| = |\hat{\mathbf{k}}| = 1.$$

$$\mathbf{A} = A_x \hat{\mathbf{i}} + A_y \hat{\mathbf{j}}$$



The resultant vector  $\mathbf{R} = \mathbf{A} + \mathbf{B}$  is therefore

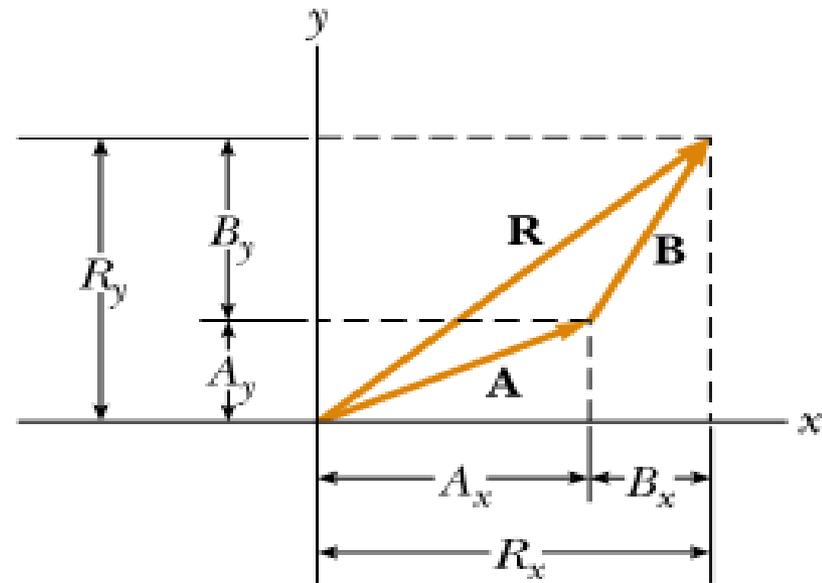
$$\mathbf{R} = (A_x \hat{\mathbf{i}} + A_y \hat{\mathbf{j}}) + (B_x \hat{\mathbf{i}} + B_y \hat{\mathbf{j}})$$

$$\mathbf{R} = (A_x + B_x) \hat{\mathbf{i}} + (A_y + B_y) \hat{\mathbf{j}}$$

$$R_x = A_x + B_x$$

$$R_y = A_y + B_y$$

$$\mathbf{R} = R_x \hat{\mathbf{i}} + R_y \hat{\mathbf{j}},$$



We obtain the magnitude of  $\mathbf{R}$  and the angle

$$R = \sqrt{R_x^2 + R_y^2} = \sqrt{(A_x + B_x)^2 + (A_y + B_y)^2}$$

$$\tan \theta = \frac{R_y}{R_x} = \frac{A_y + B_y}{A_x + B_x}$$

## Example 3.3

Find the sum of two vectors **A** and **B** lying in the *xy* plane and given by

$$\mathbf{A} = (2.0\hat{\mathbf{i}} + 2.0\hat{\mathbf{j}}) \text{ m} \quad \text{and} \quad \mathbf{B} = (2.0\hat{\mathbf{i}} - 4.0\hat{\mathbf{j}}) \text{ m}$$

## Example 3.4

A particle undergoes three consecutive displacements:  $\mathbf{d}_1 = (15\hat{\mathbf{i}} + 30\hat{\mathbf{j}} + 12\hat{\mathbf{k}})$  cm,  $\mathbf{d}_2 = (23\hat{\mathbf{i}} - 14\hat{\mathbf{j}} - 5.0\hat{\mathbf{k}})$  cm and  $\mathbf{d}_3 = (-13\hat{\mathbf{i}} + 15\hat{\mathbf{j}})$  cm. Find the components of the resultant displacement and its magnitude.