King Saud University Department of Mathematics Semester II: 1436-1437 <u>COURSE OUTLINE FOR</u> MATH 5701: TOPOLOGY and GEOMETRY 4(3+1)credit-hours

Reference Books:

1. Topology by James R. Munkres

2. Calculus on Manifolds by M. Spivak

3. An Introduction to Differentiable Manifolds and Riemannian Geometry by W. M. Boothby

Prerequisite: Math 375: Introduction to Topology(3+1) credit-hours **A. TOPOLOGY**

*REVIEW:(Munkres, Chapter 2; Sections: 2.1-2.10)

1. Separation axioms: Hausdorff, regular and normal spaces

2. Quotient spaces (Munkres, Chapter 2, pp.134)

a) Quotient map, quotient topology

b) Quotient topology by equivalence relation; various examples, such as, Torus,

Möbius strip, Klein bottle, *n*-dimensional real projective spaces \mathbf{RP}_n

3. Connectedness (Munkres, Chapter 3)

a) Connected spaces

b) Path connected spaces

c) Components, path components, relation between path *components* and *components*

d) Locally connected spaces, locally path connected spaces

4. Locally compact spaces, and the one-point compactification

5. Complete metric spaces and examples

B. DIFFERENTIABLE MANIFOLDS

Definition of smooth manifolds with related basic notions and various examples