

$$\begin{aligned} & (x^3 - 4x)^3 - 4(x^3 - 4x) \\ & f(x) = x^3 - 4x \\ & f \circ f = f(f(x)) = (f(x))^3 - 4f(x) \\ & = (x^3 - 4x)^3 - 4(x^3 - 4x) \end{aligned}$$

م 3-12:32 ناضم

$$g(x) = \frac{1}{x^2+1}$$

$$\frac{1}{(g(x))^2+1} = \frac{1}{\left(\frac{1}{x^2+1}\right)^2+1}$$

م 3-12:49 ناضم

$$\begin{aligned} & f(x) = x^3 - 4x, g(x) = \frac{1}{x^2+1}, h(x) = x^4 \\ & \text{c) } f \circ g \circ h \\ & f(g(h(x))) : \\ & g(h(x)) = \frac{1}{(x^4)^2+1} \\ & f(g(h(x))) = \left(\frac{1}{(x^4)^2+1}\right)^3 - 4\left(\frac{1}{(x^4)^2+1}\right) \end{aligned}$$

م 3-12:57 ناضم

$$\begin{aligned} & f \circ h \circ g \\ & f(x) = x^3 - 4x, g(x) = \frac{1}{x^2+1}, h(x) = x^4 \\ & f(h \circ g) \\ & h(g(x)) = (g(x))^4 = \left(\frac{1}{x^2+1}\right)^4 \\ & f(h(g(x))) = \left(\frac{1}{(x^2+1)^4}\right)^3 - 4\left(\frac{1}{(x^2+1)^4}\right) \end{aligned}$$

م 3-01:12 ناضم

$p \rightarrow q$
 Contrapositive:
 $\neg q \rightarrow \neg p$
 1) If you don't get F
 you will take an examination.

م 3-01:22 ناضم

Ex 3
 Every integer greater than 1
 has a unique prime
 factorization
 $\forall x \in \mathbb{Z} : x > 1 \rightarrow x \text{ unique} \dots$

م 3-01:30 ناضم

converse /
 $p \rightarrow q$
 $q \rightarrow p$ [converse]
 $\forall x: p \rightarrow q$
 $\forall x: q \rightarrow p$ [converse]
 $\forall x \in \mathbb{Z}: x \text{ has unique } \dots \rightarrow$
 Every integer $x > 1$ that has unique \dots is greater than one

م 3-01:33 ناضم

p
 $\neg p$ (Inverse)
 $\forall x: p$
 $\forall x: \neg p$ (Inverse)
 $a \rightarrow b \equiv \neg a \vee b$
 \vdots

م 3-01:36 ناضم

$\forall x \in \mathbb{Z}: [(x > 1 \rightarrow x \text{ is prime}) \rightarrow \exists x \in \mathbb{Z}: (x < 1 \rightarrow x \text{ is prime})]$
 $a \rightarrow b \equiv \neg a \vee b$
 $\neg(a \rightarrow b) \equiv \neg(\neg a \vee b)$
 $\forall x \in \mathbb{Z}: x \leq 1 \text{ and } x \text{ is prime} \dots$

م 3-01:39 ناضم

$\forall x: p \rightarrow q$
 $\forall x: \neg q \rightarrow \neg p$ (contrapositive)
 $\forall x \in \mathbb{Z}: x \text{ is not prime} \rightarrow x \leq 1$

م 3-01:42 ناضم

p
 $\neg p$ (Inverse, negation)
 $\forall x: p$
 $\forall x: \neg p$ (Inverse)
 $\neg(\forall x: p)$ (Negation): $\exists x: \neg p$
 $\neg(\exists x: p) \equiv \forall x: \neg p$
 $\exists x \in \mathbb{Z}, \neg(x > 1 \rightarrow x \text{ is prime} \dots)$

م 3-01:44 ناضم

$(\overline{p \rightarrow q}) \vee (q \rightarrow \overline{p})$

	\overline{a}	b			
	p	q	$p \rightarrow q$	$q \rightarrow p$	$a \vee b$
F	F	F	T	T	T
F	F	T	T	F	T
T	F	F	F	T	T
T	F	T	T	T	T

م 3-01:51 ناضم

$(p \vee \neg q) \rightarrow (q \wedge \neg p)$

p	q	$\neg p$	$\neg q$	$p \vee \neg q$	$q \wedge \neg p$	Result
F	F	T	T	T	F	F
F	T	T	F	F	T	T
T	F	F	T	T	F	F
T	T	F	F	T	F	F

م 3-01:56 ناضم

$A = \{d, i, v, s, c\}, B = \{r, e, t\}$

$A \times B = \{(d, r), (d, e), (d, t), \dots\}$

Find the power set of B

$B = \{\emptyset, \{r\}, \{e\}, \{t\}, \{r, e\}, \{r, t\}, \{e, t\}, \{r, e, t\}\}$

م 3-02:04 ناضم

$(A \cup B)^c = A^c \cap B^c$

$= \{d, i, v, s, c, r, e, t\}^c$

$= \{a, h, m\}$

م 3-02:09 ناضم

$A = \{a, e, h, m, r, t\}$

$B = \{a, c, d, i, m, s, h\}$

$A^c \cap B^c = \{a, m, h\}$

$=$

م 3-02:13 ناضم