## Net Present Value \& Other Investment Criteria CHAPTER 9

## Key Concepts and Skills

- Compute payback \& discounted payback and understand their shortcomings
- Understand accounting rates of return and their shortcomings
- Be able to compute internal rates of return (standard and modified) and understand their strengths and weaknesses
- Be able to compute the net present value and understand why it is the best decision criterion
- Be able to compute the profitability index and understand its relation to net present value


## Chapter Outline

- Net Present Value
- The Payback Rule
- The Discounted Payback
- The Average Accounting Return
- The Internal Rate of Return
- The Profitability Index
- The Practice of Capital Budgeting


## Good Decision Criteria

- We need to ask ourselves the following questions when evaluating capital budgeting decision rules:
- Does the decision rule adjust for the time value of money?
- Does the decision rule adjust for risk?
- Does the decision rule provide information on whether we are creating value for the firm?


## Net Present Value

- The difference between the market value of a project and its cost
- How much value is created from undertaking an investment?
- Step 1: estimate the expected future cash flows.
- Step 2: estimate the required return for projects of this risk level.
- Step 3: find the present value of the cash flows and subtract the initial investment.


## NPV - Decision Rule

- If the NPV is positive, accept the project
- A positive NPV means that the project is expected to add value to the firm and will therefore increase the wealth of the owners.
- Since our goal is to increase owner wealth, NPV is a direct measure of how well this project will meet our goal.


## Project Example Information

- You are reviewing a new project and have estimated the following cash flows:
- Year 0: $\quad C F=-165,000$
- Year 1: $\quad \mathrm{CF}=63,120 ; \mathrm{NI}=13,620$
- Year 2: $\quad \mathrm{CF}=70,800 ; \mathrm{NI}=3,300$
- Year 3: $\quad \mathrm{CF}=91,080 ; \mathrm{NI}=29,100$
- Average Book Value $=72,000$
- Your required return for assets of this risk level is $12 \%$.


## Computing NPV for the Project

- Using the formulas:
- NPV $=-165,000+63,120 /(1.12)+70,800 /(1.12)^{2}+$ $91,080 /(1.12)^{3}=12,627.41$
- Using the calculator:
- $\mathrm{CF}_{\mathrm{o}}=-165,000 ; \mathrm{Co1}=63,120 ; \mathrm{FO}=1 ; \mathrm{Co2}=70,800$; $\mathrm{FO} 2=1 ; \mathrm{Co} 3=91,080 ; \mathrm{FO} 3=1 ; \mathrm{NPV} ; \mathrm{I}=12 ; \mathrm{CPT} \mathrm{NPV}=$ 12,627.41
- Do we accept or reject the project?


## Decision Criteria Test - NPV

- Does the NPV rule account for the time value of money?
- Does the NPV rule account for the risk of the cash flows?
- Does the NPV rule provide an indication about the increase in value?
- Should we consider the NPV rule for our primary decision rule?


## Example 9.1

Suppose we are asked to decide whether a new consumer product should be launched. Based on projected sales and costs, we expect that the cash flows over the fiveyear life of the project will be $\$ 2000$ in the first two years, $\$ 4000$ in the next two and $\$ 5000$ in the last year. It will cost about $\$ 10000$ to begin production. We use a 10 percent discount rate to evaluate new products. What should we do here?

## Example 9.1

- Present Value of the expected cash flows $=$ $(2000 / 1.1)+\left(2000 / 1.1^{2}\right)+\left(4000 / 1.1^{3}\right)+\left(4000 / 1.1^{4}\right)$ $+\left(5000 / 1.1^{5}\right)=\$ 12313$
- $\mathrm{NPV}=-10000+12313=\$ 2313$
- Decision : accept the project because NPV is positive.


## Payback Period

- How long does it take to get the initial cost back in a nominal sense?
- Computation
- Estimate the cash flows
- Subtract the future cash flows from the initial cost until the initial investment has been recovered
- Decision Rule - Accept if the payback period is less than some preset limit


## Computing Payback for the Project

- Assume we will accept the project if it pays back within two years.
- Year 1: 165,000 $-63,120=101,880$ still to recover
- Year 2: 101,880-70,800 $=31,080$ still to recover
- Year 3: 31,080 $-91,080=-60,000$ project pays back in year 3
- Do we accept or reject the project?


## Decision Criteria Test - Payback

- Does the payback rule account for the time value of money?
- Does the payback rule account for the risk of the cash flows?
- Does the payback rule provide an indication about the increase in value?
- Should we consider the payback rule for our primary decision rule?


## Example 9.2

The proposed cash flows for a proposed project that costs $\$ 500$, are as follows:
$\$ 100$ in one year, $\$ 200$ in two years and $\$ 500$ in three years.

Should we accept or reject this project if the payback period in the market is 3 years?

## Example 9.2

$$
\begin{aligned}
& \text { Year 1: } 500-100=\$ 400 \\
& \text { Year 2: } 400-200=\$ 200 \\
& \text { Year 3: } 200-500=(300)
\end{aligned}
$$

- We only need $\$ 200$ from the third year 500 , so we have to wait $200 / 500=0.4$ years
- The payback period is 2.4 years and since it is less than 3 years the market payback period the project should be accepted.


## Advantages and Disadvantages of Payback

- Advantages
- Easy to understand
- Adjusts for uncertainty of later cash flows
- Biased toward liquidity
- Disadvantages
- Ignores the time value of money
- Requires an arbitrary cutoff point
- Ignores cash flows beyond the cutoff date
- Biased against longterm projects, such as research and development, and new projects


## Discounted Payback Period

- Compute the present value of each cash flow and then determine how long it takes to pay back on a discounted basis
- Compare to a specified required period
- Decision Rule - Accept the project if it pays back on a discounted basis within the specified time


## Computing Discounted Payback for the Project

- Assume we will accept the project if it pays back on a discounted basis in 2 years.
- Compute the PV for each cash flow and determine the payback period using discounted cash flows
- Year 1: 165,000-63,120/1.12 ${ }^{1}=108,643$
- Year 2: $108,643-70,800 / 1.12^{2}=52,202$
- Year 3: 52,202-91,080/1.12 ${ }^{3}=-12,627$ project pays back in year 3
- Do we accept or reject the project?


## Decision Criteria Test - Discounted Payback

- Does the discounted payback rule account for the time value of money?
- Does the discounted payback rule account for the risk of the cash flows?
- Does the discounted payback rule provide an indication about the increase in value?
- Should we consider the discounted payback rule for our primary decision rule?


## Advantages \& Disadvantages of Discounted

## Payback

## - Advantages

- Includes time value of money
- Easy to understand
- Does not accept negative estimated NPV investments when all future cash flows are positive
- Biased towards liquidity
- Disadvantages
- May reject positive NPV investments
- Requires an arbitrary cutoff point
- Ignores cash flows beyond the cutoff point
- Biased against longterm projects, such as
R\&D and new products


## Average Accounting Return

- There are many different definitions for average accounting return
- The one used in the book is:
- Average net income / average book value
- Note that the average book value depends on how the asset is depreciated.
- Need to have a target cutoff rate
- Decision Rule: Accept the project if the AAR is greater than a preset rate


## Computing AAR for the Project

- Assume we require an average accounting return of 25\%
- Average Net Income:
- $(13,620+3,300+29,100) / 3=15,340$
- $\mathrm{AAR}=15,340 / 72,000=.213=21.3 \%$
- Do we accept or reject the project?


## Decision Criteria Test - AAR

- Does the AAR rule account for the time value of money?
- Does the AAR rule account for the risk of the cash flows?
- Does the AAR rule provide an indication about the increase in value?
- Should we consider the AAR rule for our primary decision rule?


## Advantages \& Disadvantages of AAR

- Advantages
- Easy to calculate
- Needed information will usually be available
- Disadvantages
- Not a true rate of return; time value of money is ignored
- Uses an arbitrary benchmark cutoff rate
- Based on accounting net income and book values, not cash flows and market values


## Internal Rate of Return

- This is the most important alternative to NPV
- It is often used in practice and is intuitively appealing
- It is based entirely on the estimated cash flows and is independent of interest rates found elsewhere


## IRR - Definition \& Decision Rule

- Definition: IRR is the return that makes the $\mathrm{NPV}=\mathrm{o}$
- Decision Rule: Accept the project if the IRR is greater than the required return


## Computing IRR for the Project

- If you do not have a financial calculator, then this becomes a trial and error process
- Calculator
- Enter the cash flows as you did with NPV
- Press IRR and then CPT
$\circ \operatorname{IRR}=16.13 \%>12 \%$ required return
- Do we accept or reject the project?


## IRR Example

Consider a project that costs $\$ 100$ today and pays $\$ 110$ in one year. Suppose you were asked, "What is the return on this investment?" What would you say?

- NPV = -\$100 + [\$110/(1+R)]
- $0=-\$ 100+[\$ 110 /(1+\mathrm{R})]$
- $\$ 100=\$ 110 /(1+\mathrm{R})$
- $1+\mathrm{R}=110 / 100=1.1$
- $\mathrm{R}=10 \%$


## Example 9.4

A project has a total up-front cost of $\$ 435.44$. The cash flows are $\$ 100$ in the first year, $\$ 200$ in the second year and $\$ 300$ in the third year. What's the IRR? If we require an 18 percent return, should we take this investment?
$\circ$ The NPV is zero at $15 \% \rightarrow \operatorname{IRR}=15 \%$.

- Decision: reject this investment because its $15 \%$ return is below the required return of $18 \%$.


## Decision Criteria Test - IRR

- Does the IRR rule account for the time value of money?
- Does the IRR rule account for the risk of the cash flows?
- Does the IRR rule provide an indication about the increase in value?
- Should we consider the IRR rule for our primary decision criteria?


## Advantages of IRR

- Knowing a return is intuitively appealing
- It is a simple way to communicate the value of a project to someone who doesn't know all the estimation details
- If the IRR is high enough, you may not need to estimate a required return, which is often a difficult task


## Summary of Decisions for the Project

## Summary

Net Present Value $\quad$ Accept
Payback Period
Discounted Payback Period Reject
Average Accounting Return Reject
Internal Rate of Return Accept

## NPV vs. IRR

- NPV and IRR will generally give us the same decision
- Exceptions
- Nonconventional cash flows - cash flow signs change more than once
- Mutually exclusive projects
* Initial investments are substantially different (issue of scale)
. Timing of cash flows is substantially different


## IRR \& Nonconventional Cash Flows

- When the cash flows change sign more than once, there is more than one IRR
- When you solve for IRR you are solving for the root of an equation, and when you cross the $x$-axis more than once, there will be more than one return that solves the equation
- If you have more than one IRR, which one do you use to make your decision?


## Example - Nonconventional Cash Flows

- Suppose an investment will cost \$90,000 initially and will generate the following cash flows:
- Year 1: 132,000
- Year 2: 100,000
- Year 3: -150,000
- The required return is $15 \%$.
- Should we accept or reject the project?


## Cont'd

$0 \mathrm{NPV}=-90,000+132,000 / 1.15+100,000 /(1.15)^{2}$

$$
-150,000 /(1.15)^{3}=1,769.54
$$

- Calculator:
${ }^{2} \mathrm{CF}_{\mathrm{o}}=-90,000 ; \mathrm{Co1}=132,000 ; \mathrm{FO}=1 ; \mathrm{Co2}=100,000 ; \mathrm{FO}=1$; Co3 $=-150,000 ;$ Fo3 $=1 ;$ I $=15 ;$ CPT NPV $=1769.54$
- $\operatorname{IRR}=10.11 \%$


## NPV Profile

$\operatorname{IRR}=10.11 \%$ and $42.66 \%$


## Summary of Decision Rules

- The NPV is positive at a required return of $15 \%$, so you should Accept
- If you use the financial calculator, you would get an IRR of $10.11 \%$ which would tell you to Reject
- You need to recognize that there are nonconventional cash flows and look at the NPV profile


## IRR and Mutually Exclusive Projects

- Mutually exclusive projects:
- If you choose one, you can't choose the other
- Ex: You can choose to attend graduate school at either Harvard or Stanford, but not both
- Intuitively, you would use the following decision rules:
- NPV - choose the project with the higher NPV
- IRR - choose the project with the higher IRR


## Example with Mutually Exclusive Projects

- The required return for both projects is $10 \%$.
- Which project should we accept \& why?

| Period | Project A | Project B |
| :--- | :---: | :---: |
| 0 | -500 | -400 |
| 1 | 325 | 325 |
| 2 | 325 | 200 |
| IRR | $19.43 \%$ | $22.17 \%$ |
| NPV | 64.05 | 60.74 |

## NPV Profiles



Discount Rate

## Example 9.7

- Suppose we have the following two mutually exclusive investments:

| Year | Investment A | Investment B |
| :--- | :---: | :---: |
| 0 | -400 | -500 |
| 1 | 250 | 320 |
| 2 | 280 | 340 |

- What is the crossover rate?
- $\operatorname{NPV}(B-A)=-100+[70 /(1+R)]+\left[60 /(1+R)^{2}\right]$
- $\mathrm{R}=20 \%$


## Conflicts Between NPV and IRR

- NPV directly measures the increase in value to the firm
- Whenever there is a conflict between NPV and another decision rule, you should always use NPV
- IRR is unreliable in the following situations
- Nonconventional cash flows
- Mutually exclusive projects


## Modified IRR

- Calculate the net present value of all cash outflows using the borrowing rate.
- Calculate the net future value of all cash inflows using the investing rate.
- Find the rate of return that equates these values.
- Benefits: single answer and specific rates for borrowing and reinvestment


## Profitability Index

- Measures the benefit per unit cost, based on the time value of money
- A profitability index of 1.1 implies that for every $\$ 1$ of investment, we create an additional $\$ 0.10$ in value
- This measure can be very useful in situations in which we have limited capital
- PV of the future cash flows / initial investment


## Advantages \& Disadvantages of Profitability Index

- Advantages
- Closely related to NPV, generally leading to identical decisions
- Easy to understand and communicate
- May be useful when available investment funds are limited
- Disadvantages
- May lead to incorrect decisions in comparisons of mutually exclusive investments


## Capital Budgeting In Practice

- We should consider several investment criteria when making decisions
- NPV and IRR are the most commonly used primary investment criteria
- Payback is a commonly used secondary investment criteria


## Summary - DCF Criteria

- Net present value
- Difference between market value and cost
- Take the project if the NPV is positive
- Has no serious problems
- Preferred decision criterion
- Internal rate of return
- Discount rate that makes NPV = o
- Take the project if the IRR is greater than the required return
- Same decision as NPV with conventional cash flows
- IRR is unreliable with nonconventional cash flows or mutually exclusive projects


## Summary - DCF Criteria

- Profitability Index
- Benefit-cost ratio
- Take investment if PI > 1
- Cannot be used to rank mutually exclusive projects
- May be used to rank projects in the presence of capital rationing


## Summary - Payback Criteria

- Payback period
- Length of time until initial investment is recovered
- Take the project if it pays back within some specified period
- Doesn't account for time value of money, and there is an arbitrary cutoff period
- Discounted payback period
- Length of time until initial investment is recovered on a discounted basis
- Take the project if it pays back in some specified period
- There is an arbitrary cutoff period


## Summary - Accounting Criterion

- Average Accounting Return
- Measure of accounting profit relative to book value
- Similar to return on assets measure
- Take the investment if the AAR exceeds some specified return level
- Serious problems and should not be used

