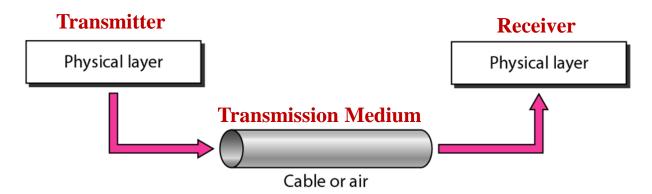
William Stallings Data and Computer Communications

Chapter 3

Data Transmission

Terminology (1)

- **XTransmitter**
- ***Receiver**
- **XTransmission Medium**
 - **Guided medium**
 - **△ Unguided medium**
 - ⊠e.g. air, water, vacuum



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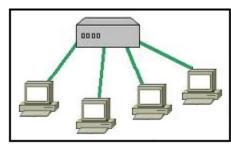
Terminology (2)

Network Topology:

#Point-to-point

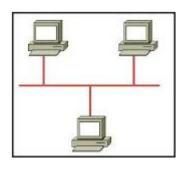
□ Direct link: No intermediate devices other than amplifiers or repeaters used to increase signal strength

○Only 2 devices share link



Point-to-Point Topology

Multi-point



Multi-point Topology

3

Terminology (3)

Communication Modes:

#Simplex

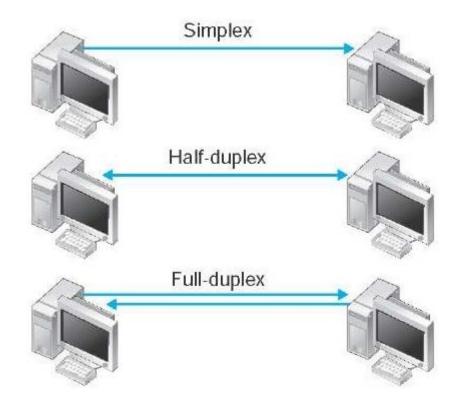
One direction
⋉e.g. Television

Half duplex

□ Either direction, but only one way at a time

#Full duplex

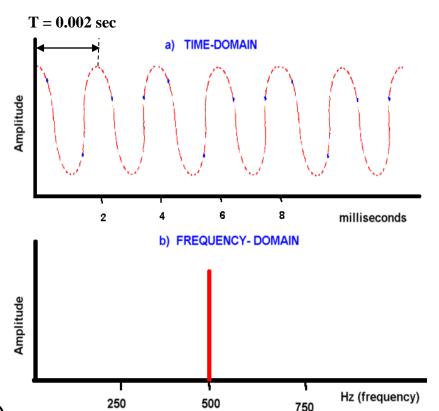
Both directions at the same time



Electromagnetic Signals

XTime-Domain

- Analog (varies smoothly over time)
- ☑ Digital (constant level over time, followed by a change to another level)



5

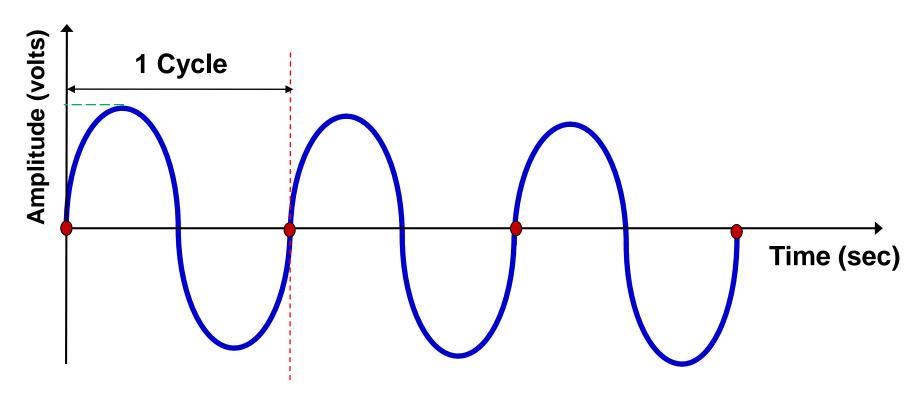
#Frequency-Domain

- Spectrum (range of frequencies)
- □ Bandwidth (width of the spectrum)

$$T = 0.002 \text{ sec}$$
 $\Rightarrow f = \frac{1}{T} = \frac{1}{0.002} = 500 \text{ Hz}$

Analog Signaling

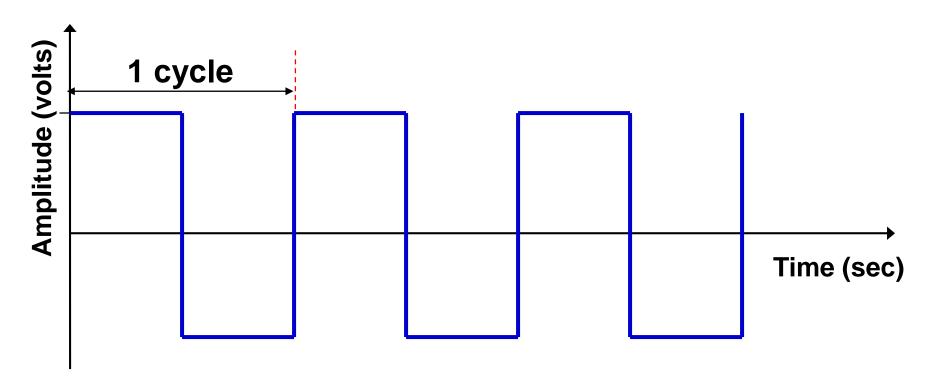
represented by sine waves



Frequency (Hertz) = Cycles per Second

Digital Signaling

#represented by square waves or pulses



Frequency (Hertz) = Cycles per Second

Frequency, Spectrum and Bandwidth

XTime domain concepts

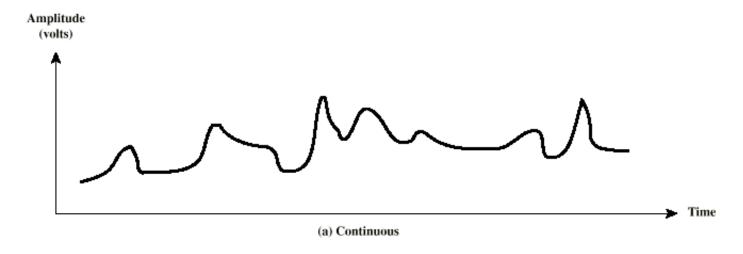
Continuous signal

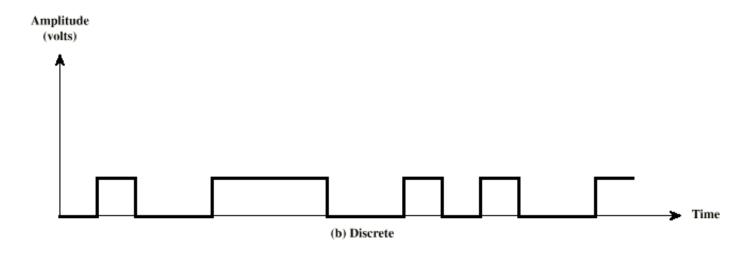
Discrete signal

Periodic signal

△Aperiodic signal

Continuous & Discrete Signals





Sine Wave

and

$$x(t) = A\sin(2\pi f t + \phi)$$

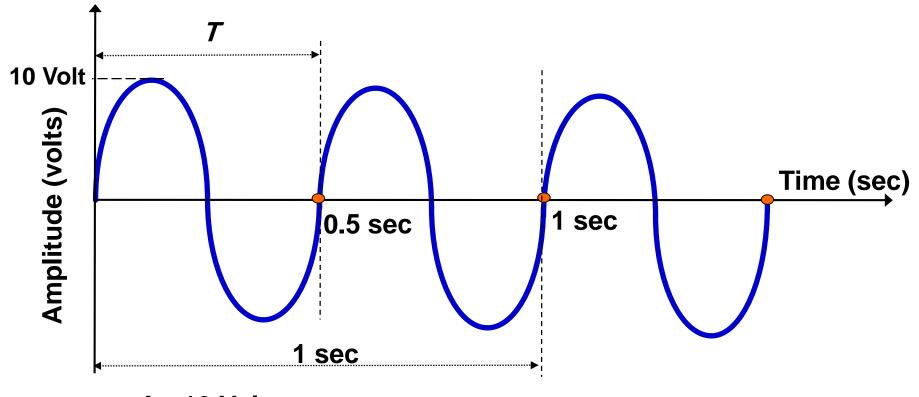
where x(t) is the signal at time t,

A is the maximum amplitude of the signal,

f represents the number of cycles per second,

• defines the phase of the signal.

Sine Wave – Example 1

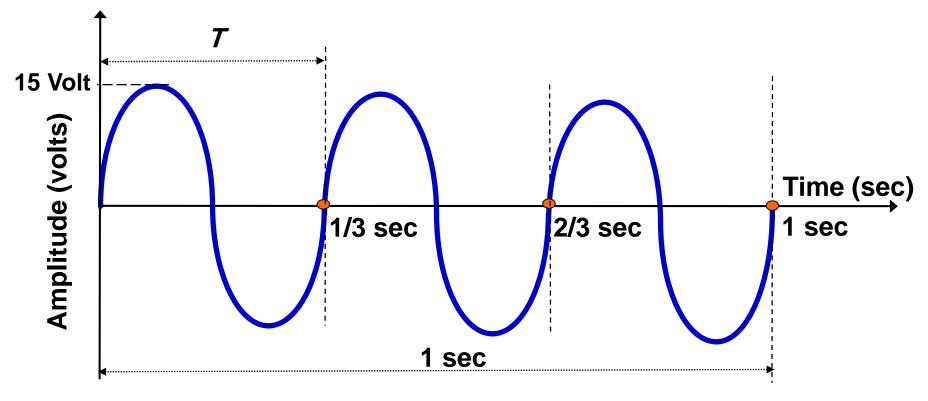


A = 10 Volt

f = 2 Hz

 ϕ = 0 Radian

Sine Wave – Example 2

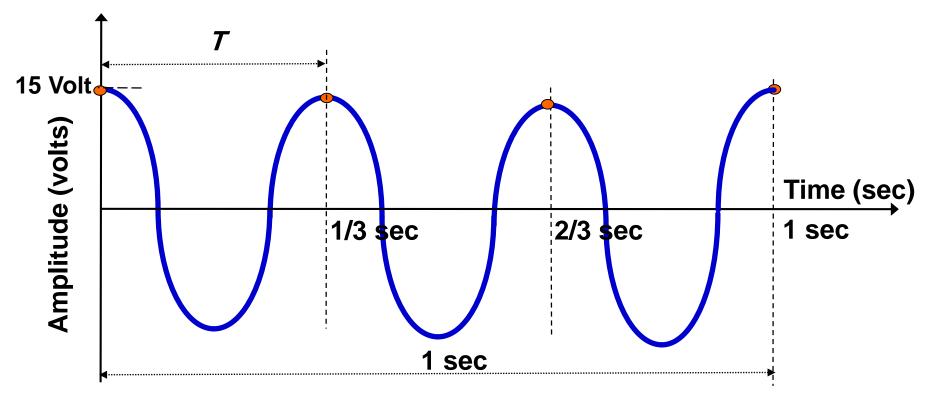


A = 15 Volt

f = 3 Hz

 ϕ = 0 Radian

Sine Wave – Example 3



A = 15 Volt

f = 3 Hz

 $\phi = \pi/2$ Radian

Sine Wave

Amplitude:

☐ The amplitude is the instantaneous value of a signal at any time.

Peak Amplitude (A):

Maximum strength of a signal. Its unit is Volt.

Frequency (f)

- Rate of change of signal
- □ Hertz (Hz) or cycles per second
- Period = time for one repetition (T)
- $\triangle T = 1/f$

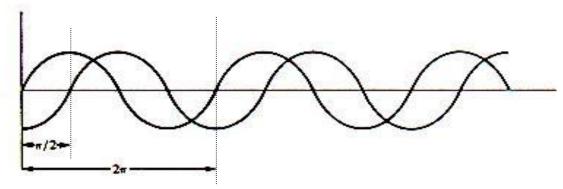
Phase (♦)

Position of the waveform relative to time zero.

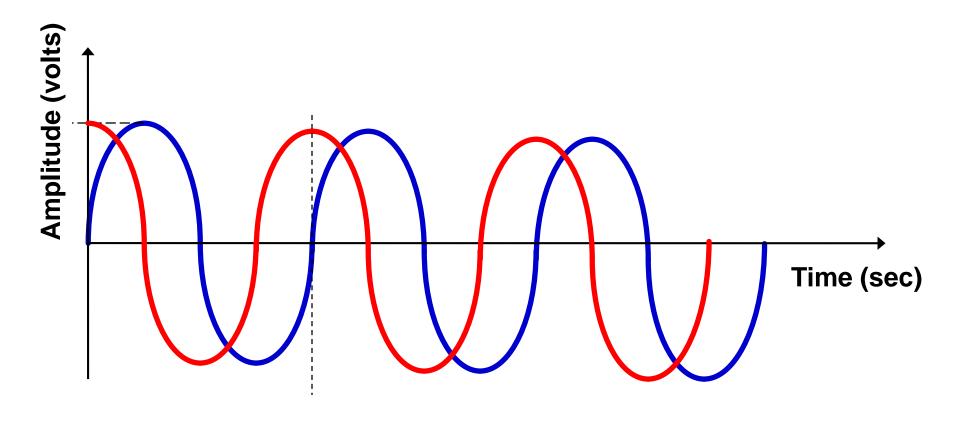
Sine Wave

Phase:

- ☐ The phase describes the position of the waveform relative to time zero. The range of shift is within a single period of a signal.
- The phase is a measure in degree or radian $(2\pi = 360^{\circ})$.
- The figure shows two signals that are out of phase by $\pi/2$ radians.

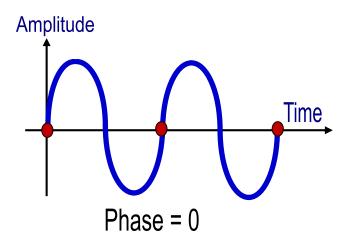


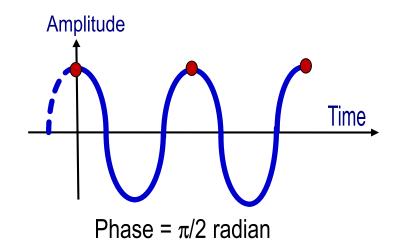
Phase

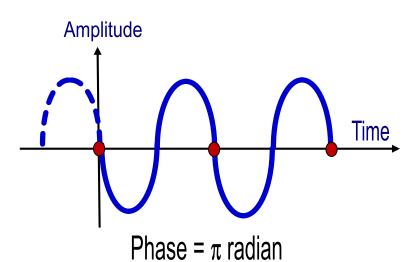


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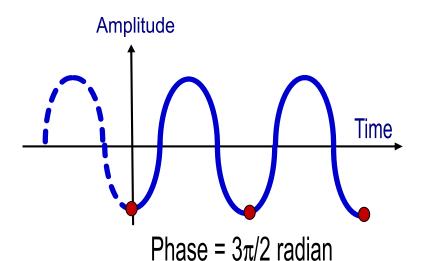
Phase



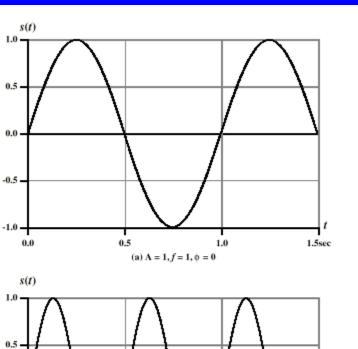


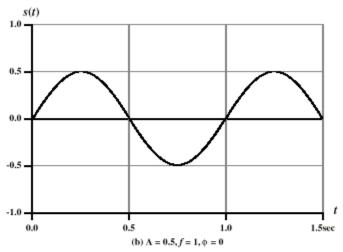


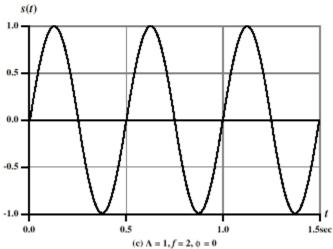
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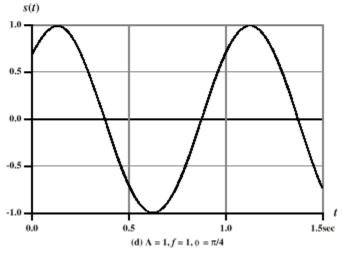


Varying Sine Waves









18

Wavelength

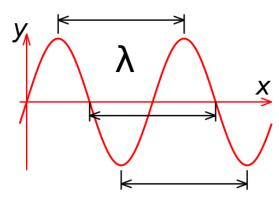
- # Distance occupied by one cycle
- # Distance between two points of corresponding phase in two consecutive cycles
- \aleph Wavelength is commonly designated by λ
- # The wavelength is related to the period as follows:

$$\lambda = vT$$

where ν : signal velocity

T: signal period

$$v = \lambda f$$



where $v = c = 3*10^8 \,\text{ms}^{-1}$ (speed of light in free space)

Example

Your voice is a summation of sine waves, each sine wave having its own frequency, phase, and amplitude. The range of frequencies is normally between 300 and 3300 Hz. Give a general equation.

$$x(t) = A_1 \sin(2\pi f_0 t + \phi_1) + A_2 \sin(2\pi f_2 t + \phi_2) + \dots + A_n \sin(2\pi f_n t + \phi_n)$$

with 300 Hz $< f_i <$ 3300 Hz. f_0 is called the *fundamental* frequency, and f_2 , f_3 ... f_n are called the harmonics.

Periodic Signal

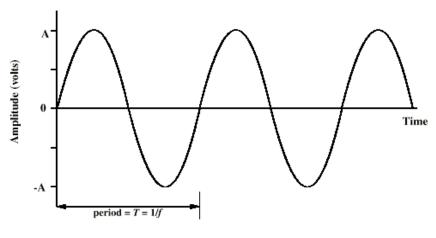
#Periodic signal: a signal that repeats itself at equal time interval.

XIt is made up of a infinite series of sinusoidal frequency components.

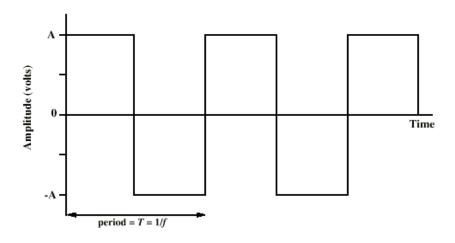
******A signal is **periodic** if and only if:

$$s(t+T) = s(t) \qquad -\infty < t < +\infty$$

Periodic Signals



(a) Sine wave



(b) Square wave





Periodic Signal

****** Mathematically, we can express any periodic waveform as follows:

$$v(t) = a_0 + \sum_{n=1}^{\infty} a_n \cos n\omega_0 t + \sum_{n=1}^{\infty} b_n \sin n\omega_0 t$$

where:

v(t) is the voltage signal representation as a function of time ω_0 is the fundamental frequency component in radians per second $T = 2\pi/\omega_0$ is the period of the waveform in seconds

The terms a_0 , a_n and b_n are known as the Fourier coefficients and, for a particular waveform, we can derive them from the following set of integrals:

$$a_0 = \frac{1}{T} \int_0^T v(t) dt$$

$$a_n = \frac{2}{T} \int_0^T v(t) \cos(n\omega_0 t) dt$$

$$b_n = \frac{2}{T} \int_0^T v(t) \sin(n\omega_0 t) dt$$

We can deduce from the first integral that a_0 is the mean of the signal over the period T and is known as the DC component.

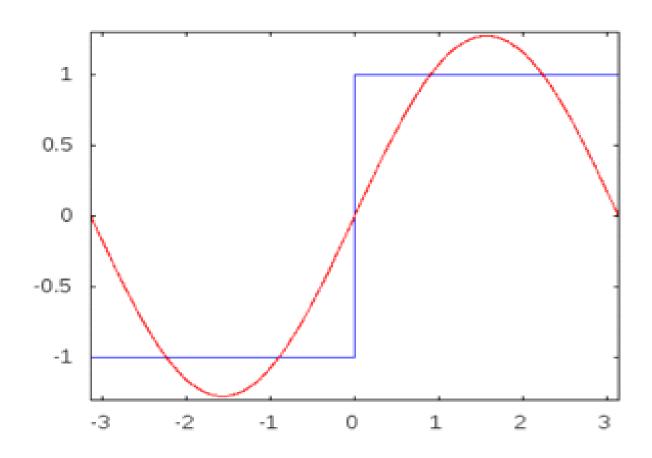
Frequency Domain Concepts

- **#**Signal usually made up of many frequencies
- **#**Components are sine waves
- **#**Can be shown (**Fourier analysis**) that any signal is made up of component sine waves
- ****** Can plot frequency domain functions

The Frequency components of a square wave with amplitude A and -A can be expressed as follows:

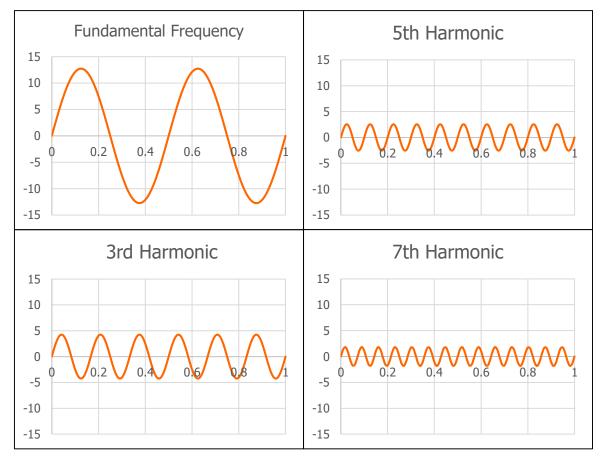
$$s(t) = A \times \frac{4}{\pi} \times \sum_{\substack{k \text{ oddk}=1}}^{\infty} \frac{\sin(2\pi kft)}{k}$$

- # This waveform has an infinite number of frequency components, and hence an infinite bandwidth.
- # The peak amplitude of the kth frequency component is only 1/k, so most of the energy in this waveform is in the first few frequency components



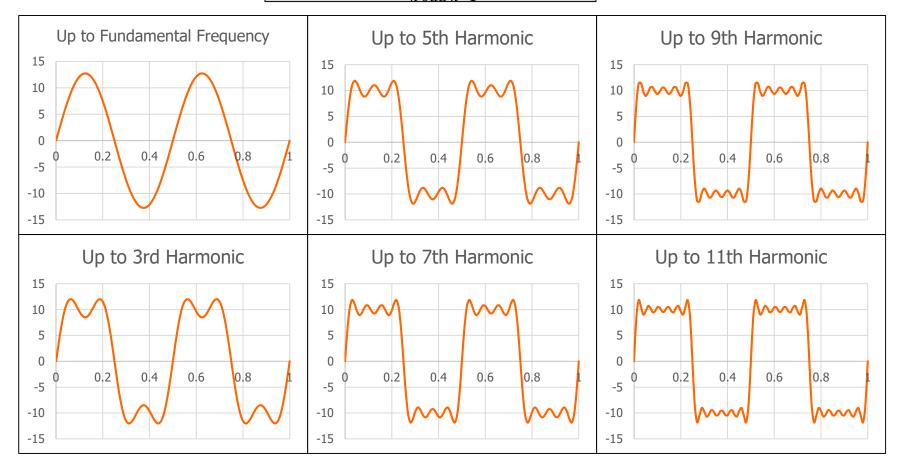
$$s(t) = A \times \frac{4}{\pi} \times \sum_{\substack{k \text{ odd } k=1}}^{\infty} \frac{\sin(2\pi k f t)}{k}$$

A = 10 Volt, f = 2 Hz



$$s(t) = A \times \frac{4}{\pi} \times \sum_{\substack{k \text{ odd } k=1}}^{\infty} \frac{\sin(2\pi k f t)}{k}$$

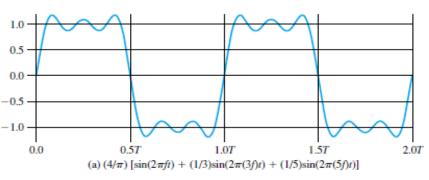
A = 10 Volt, f = 2 Hz

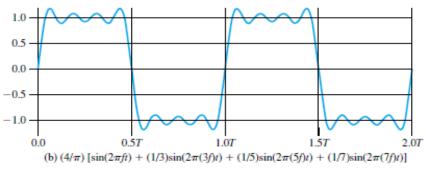


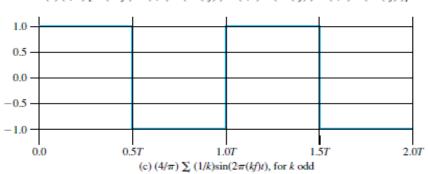
Fundamental Frequency + Third harmonic + Fifth Harmonic:

Fundamental Frequency + Third harmonic + Fifth Harmonic + Seventh Harmonic:

Square waveform with an infinite number of frequency components







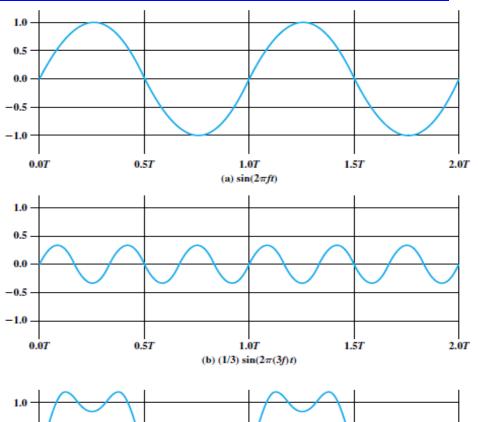


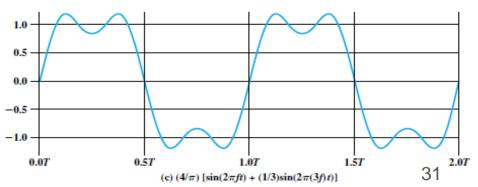
Addition of Frequency Components

Fundamental Frequency Component:

Third Harmonic:

Fundamental Frequency + Third Harmonic Components:

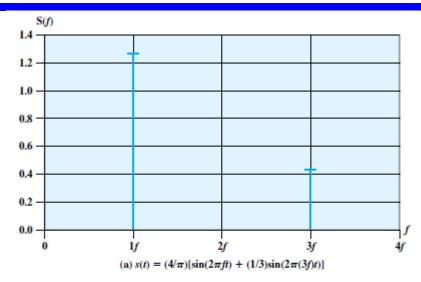


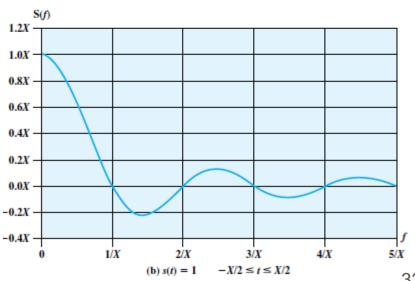


Frequency-Domain

- ** For square waves, only odd harmonics exist (plus the fundamental component of course)
- # Figure (a) is discrete because the time domain function is **Periodic**.

Figure (b) is continuous because the time domain function is **Aperiodic**.





Spectrum & Bandwidth

Spectrum

range of frequencies contained in signal

***Absolute bandwidth**

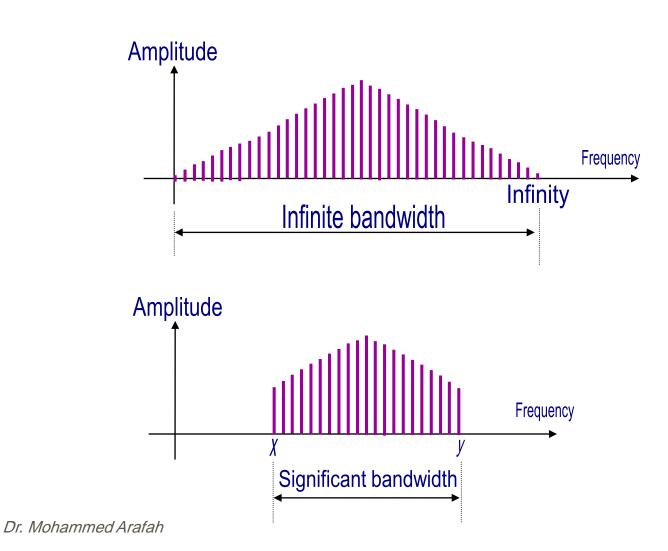
Effective bandwidth

- ○Often just bandwidth
- Narrow band of frequencies containing most of the energy

#DC Component

Component of zero frequency

Absolute and Effective Bandwidth



Bandwidth Example 1

#If a periodic signal is decomposed into five sine waves with frequencies of 100, 300, 500, 700, and 900 Hz, what is the bandwidth?

\#Let f_H be the highest frequency, f_L be the lowest frequency, and B be the bandwidth. Then,

$$B = f_H - f_I = 900 - 100 = 800 \text{ Hz}$$

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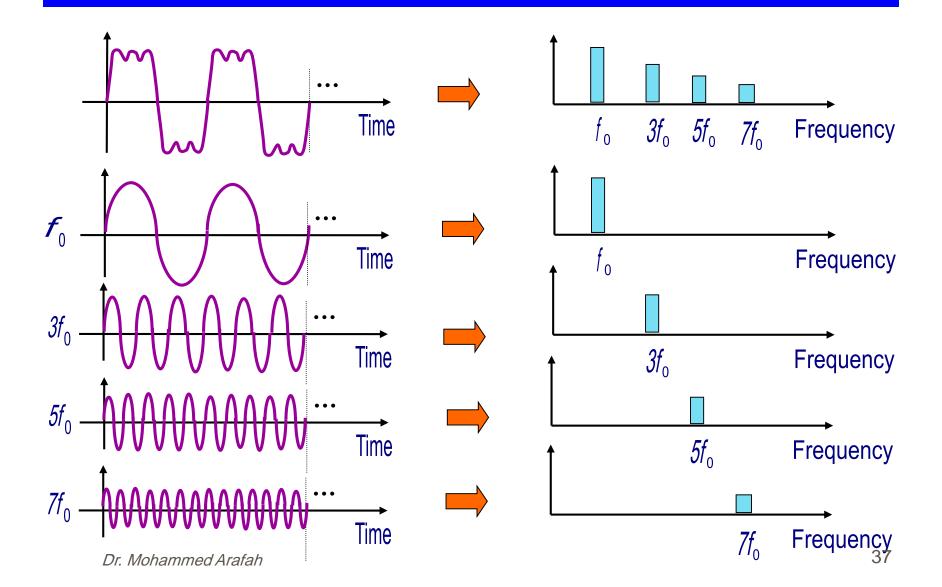
Bandwidth Example 2

XA signal has a bandwidth of 20 KHz. The highest frequency is 60 KHz. What is the lowest frequency?

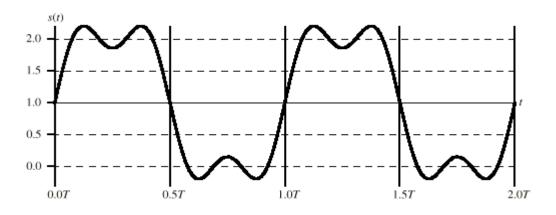
 \mathbb{H} Let f_H be the highest frequency, f_L be the lowest frequency, and B be the bandwidth. Then,

B =
$$f_H$$
 - f_L
 \Rightarrow $f_L = f_H$ - B
 \Rightarrow $f_I = 60 \text{ KHz} - 20 \text{ KHz} = 40 \text{ KHz}$

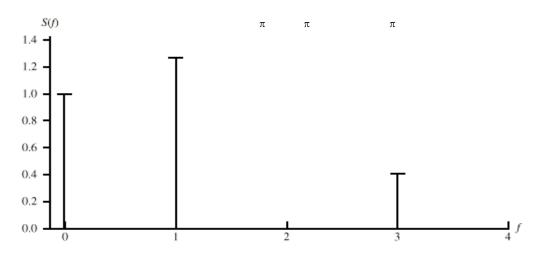
Decomposition of a Digital Signal



Signal with DC Component

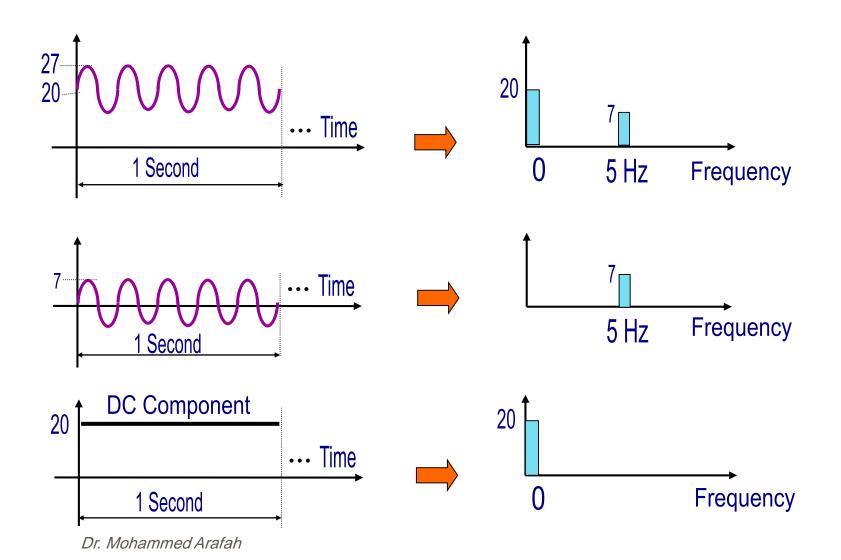


(a) $s(t) = 1 + (4/) [\sin(2 ft) + (1/3) \sin(2 (3f)t)]$



(b) S(f)

Time Domain and Frequency Domain



39

Data Rate and Bandwidth

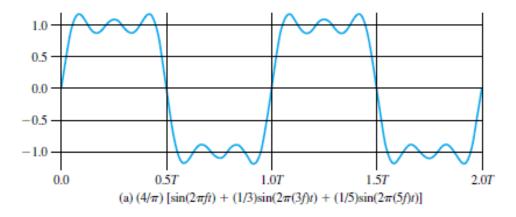
******Any transmission system has a limited band of frequencies

#This limits the data rate that can be carried

#For economic and practical reasons, digital information must be approximated by the signal of limited bandwidth.

Data Rate and Bandwidth Example 1:

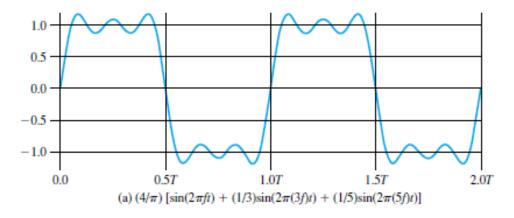
$$\Re f = 1 \text{ MHz}$$



- # Bandwidth = $f_H f_L = 5$ MHz 1 MHz = 4 MHz
- # Period of the signal = $T = 1/f = 1 \mu sec$
- # The signal is a bit string of 1s and 0s
- \sharp One bit occurs every T_b=0.5 µsec → Data Rate of 2 Mbps (R= 1/T_b)
- # Thus, a bandwidth of 4 MHz, a data rate of 2 Mbps is achieved.

Data Rate and Bandwidth Example 2:

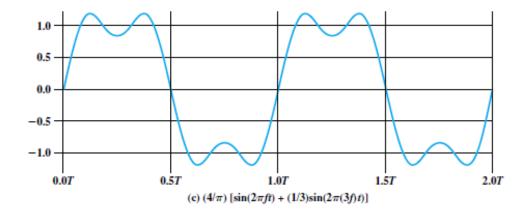
$$\# f = 2 \text{ MHz}$$



- # Bandwidth = $f_H f_L = 10$ MHz 2 MHz = 8 MHz
- # Period of the signal = $T = 1/f = 0.5 \mu sec$
- # The signal is a bit string of 1s and 0s
- # One bit occurs every 0.25 μ sec \rightarrow Data Rate of 4 Mbps
- **# Thus, by doubling the bandwidth, we double the potential data rate**

Data Rate and Bandwidth Example 3:

$$\# f = 2 \text{ MHz}$$



- # Bandwidth = $f_H f_L = 6MHz 2 MHz = 4 MHz$
- # Period of the signal = $T = 1/f = 0.5 \mu sec$
- # The signal is a bit string of 1s and 0s
- # One bit occurs every 0.25 μ sec \rightarrow Data Rate of 4 Mbps

Analog and Digital Data Transmission

Data

#Signals

□ Electric or electromagnetic representations of data

XTransmission

Communication of data by propagation and processing of signals

Data

***Analog**

- Continuous values within some interval
- △e.g. **sound**, **video**

Digital

- □ Discrete values
- △e.g. **text**, **integers**

Signals

- **#** Means by which data are propagated
- ***Analog**
 - Continuously variable
 - ✓ Various media: wire, fiber optic, space
 - **Speech** bandwidth 100Hz to 7kHz
 - **Telephone** bandwidth 300Hz to 3300Hz
 - **△Video** bandwidth 4MHz

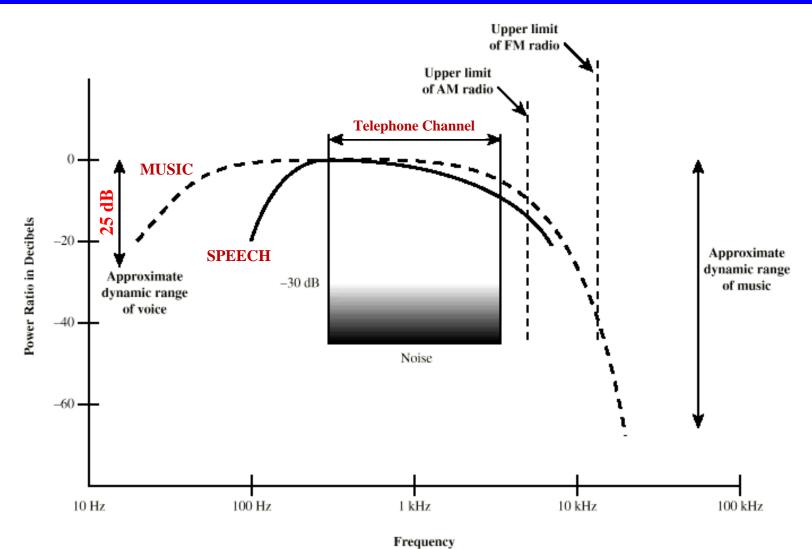
Digital

✓ Use two DC components





Acoustic Spectrum (Analog)







Acoustic Spectrum (Analog)

- #The power ratio of typical speech has a dynamic range of about 25 dB (decibels)
- #The power produced by the loudest shout may be as much as 300 times greater than the least whisper.

$$\#$$
 25 dB = 10 $\log_{10}X$

$$\rightarrow \log_{10} X = 2.5$$

$$\rightarrow 10^{\log_{10} X} = 10^{2.5}$$

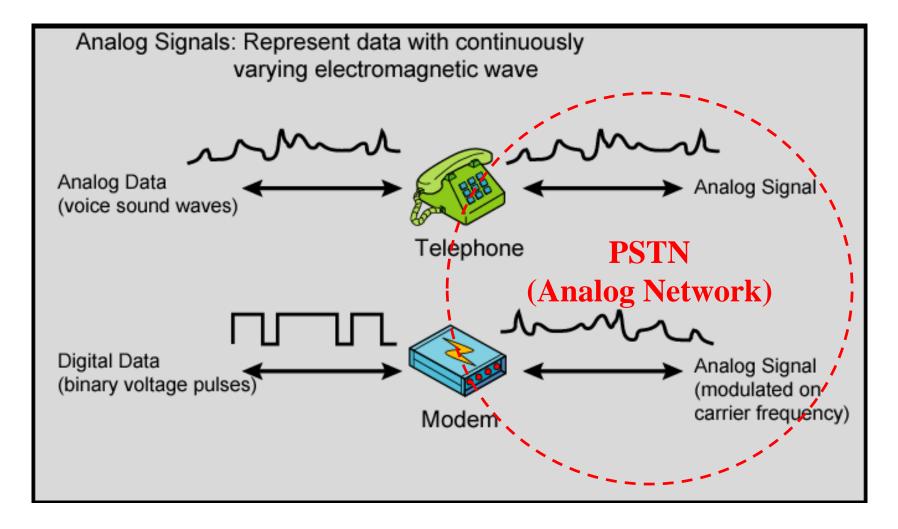
$$\rightarrow$$
 X = $10^{2.5}$ = 316

Data and Signals

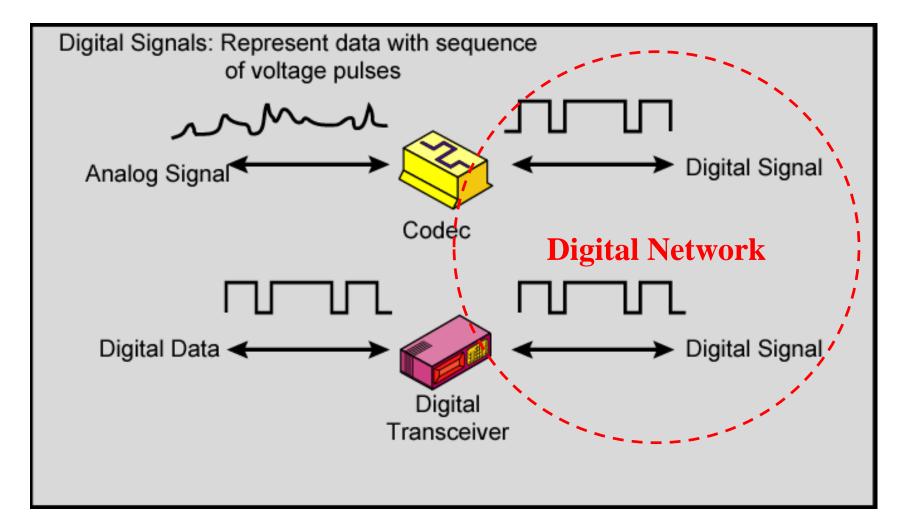
****Usually use digital signals for digital data** and analog signals for analog data

Can use analog signal to carry digital dataModem

Analog Signals Carrying Analog and Digital Data



Digital Signals Carrying Analog and Digital Data



Analog Transmission

- ******Analog signal transmitted without regard to content
- ****** May be analog or digital data
- ******Attenuated over distance
- **#**Use **amplifiers** to boost signal
- **#**Also amplifies noise

Digital Transmission

- **#**Concerned with content
- #Integrity endangered by noise, attenuation etc.
- ***Repeaters** used
 - Repeater receives signal
 - Extracts bit pattern
 - Retransmits
- *****Attenuation is overcome
- **X** Noise is not amplified

Advantages of Digital Transmission

Digital technology is cheaper

★ Data integrity

Longer distances over lower quality lines

★ Capacity utilization

- High degree of multiplexing easier with digital techniques

Security & Privacy

Encryption

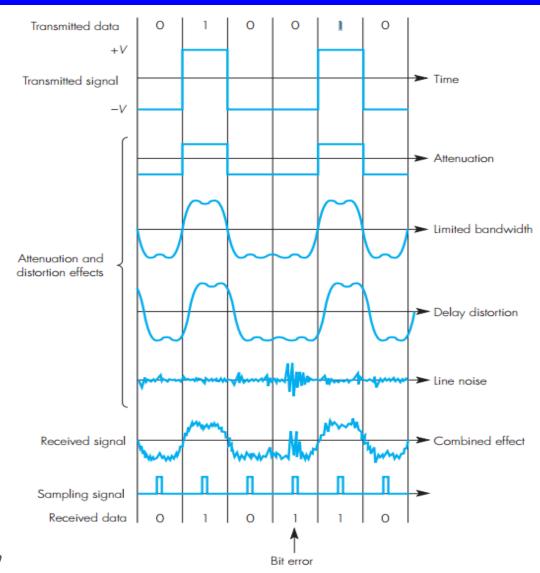
Integration

□ Can treat analog and digital data similarly

Transmission Impairments

- ★ Signal received may differ from signal transmitted
- **Analog** degradation of signal quality
- **♯ Digital bit errors**
- **X** Caused by
 - 1. Attenuation and attenuation distortion
 - 2. Limited Bandwidth
 - 3. Delay distortion
 - 4. Noise

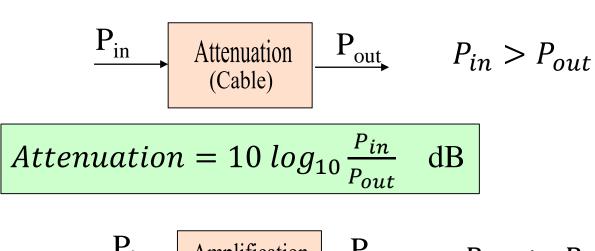
Transmission Impairments



#Signal strength falls off with distance

- **#Depends on medium (Chapter4)**
- ****** Received signal strength:
 - must be enough to be detected
 - must be sufficiently higher than noise to be received without error
- #Attenuation is an increasing function of frequency (Chapter4)

 \mathbb{H} If we denote transmitted signal power level by P_1 and the received power by P_2 , then

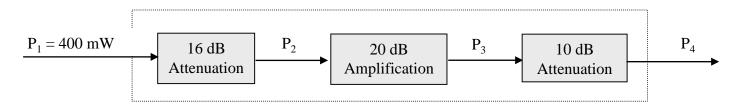


$$\begin{array}{c|c} P_{\text{in}} & P_{\text{out}} \\ \hline & (\text{Repeater}) \end{array} \quad \begin{array}{c} P_{\text{out}} \\ \end{array} \quad P_{out} > P_{in}$$

$$Amplification = 10 \log_{10} \frac{P_{out}}{P_{in}} dB$$

Example:

A transmission channel between two DTEs is made up of three section. The first introduces an attenuation of 16 dB, the second an amplification of 20 dB, and the third an attenuation of 10 dB. Assuming a mean transmitted power level of 400 mW, determine the mean output power of the channel.



 $P_1 = 10log_{10} (400)$ $\Rightarrow P_1 = 26.02 dBm$

Solution:

First section:

$$Attenuation = 10 log_{10} \frac{P_1}{P_2}$$

$$\rightarrow 16 = 10 \log_{10} \frac{400}{P_2}$$

$$\rightarrow 1.6 = log_{10} \frac{400}{P_2}$$

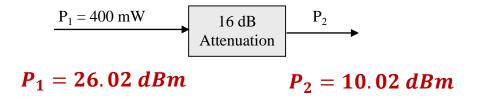
$$\rightarrow 10^{1.6} = 10^{\log_{10} \frac{400}{P_2}}$$

$$\rightarrow 39.81 = \frac{400}{P_2}$$

$$ightharpoonup P_2 = \frac{400}{39.81}$$

$$\rightarrow P_2 = 10.0475 \, mW$$

$$\rightarrow P_2 = 10log_{10} (10.0475) = 10.02 \text{ dBm}$$



Solution:

Second section:

$$Amplification = 10 \log_{10} \frac{P_3}{P_2}$$

$$\rightarrow 20 = 10 \log_{10} \frac{P_3}{10.0475}$$

$$\rightarrow 2 = log_{10} \frac{P_3}{10.0475}$$

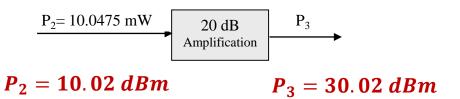
$$\rightarrow 10^2 = 10^{\log_{10} \frac{P_3}{10.0475}}$$

$$\rightarrow 100 = \frac{P_3}{10.0475}$$

$$\rightarrow P_3 = 100 \times 10.0475$$

$$\rightarrow P_3 = 1004.75 \, mW$$

$$\rightarrow P_3 = 10log_{10} (1004.75) = 30.02 \text{ dBm}$$



Solution:

Third section:

$$Attenuation = 10 \log_{10} \frac{P_3}{P_4}$$

$$\rightarrow 10 = 10 \log_{10} \frac{1004.75}{P_4}$$

$$\rightarrow 1 = log_{10} \frac{1004.75}{P_4}$$

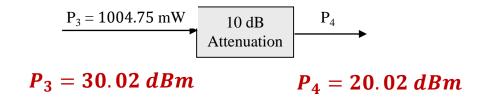
$$\rightarrow 10^1 = 10^{\log_{10} \frac{1004.75}{P_4}}$$

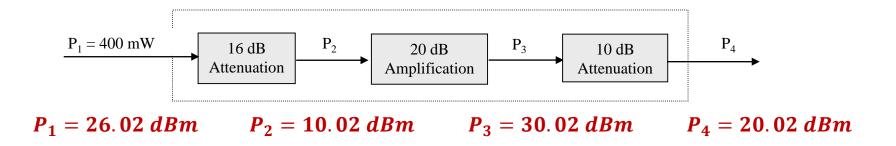
$$\rightarrow 10 = \frac{1004.75}{P_4}$$

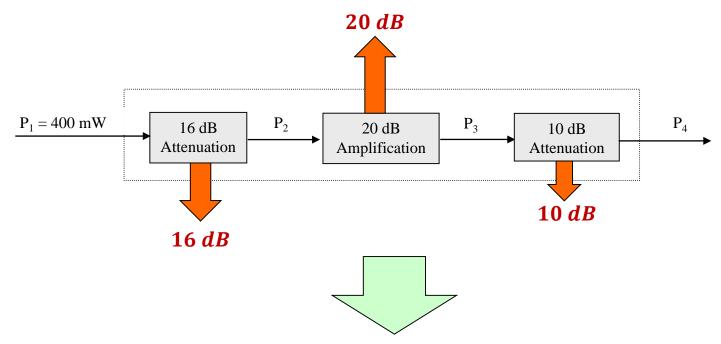
$$\rightarrow P_4 = \frac{1004.75}{10}$$

$$\rightarrow P_4 = 100.475 \, mW$$

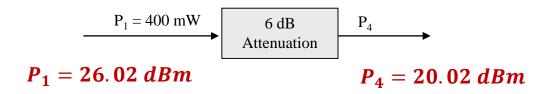
→
$$P_4 = 10log_{10}$$
 (100.475) = 20.02 dBm







Overall Attenuation Channel = 16 - 20 + 10 = 6 dB



Overall Attenuation Channel = 16 - 20 + 10 = 6 dB

$$P_1 = 400 \text{ mW}$$
Attenuation
$$P_4$$

$$P_1 = 26.02 \text{ } dBm$$

$$P_4 = 20.02 \text{ } dBm$$

$$Attenuation = 10 log_{10} \frac{P_1}{P_4}$$

$$\rightarrow 6 = 10 \log_{10} \frac{400}{P_4}$$

$$\rightarrow 0.6 = log_{10} \frac{400}{P_4}$$

$$\rightarrow 10^{0.6} = 10^{\log_{10} \frac{400}{P_4}}$$

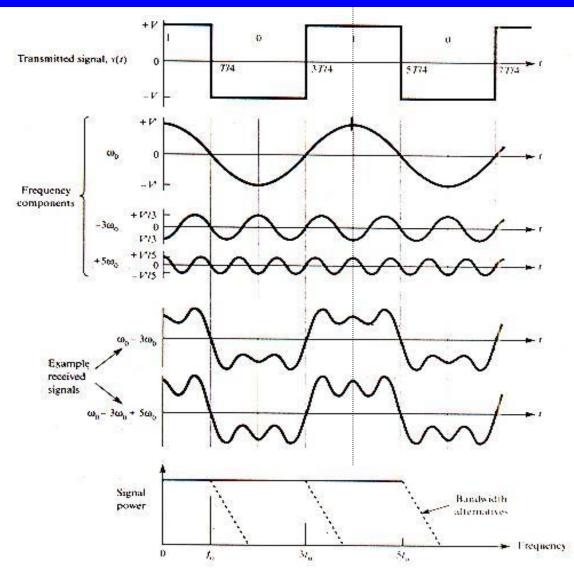
$$\rightarrow 3.981 = \frac{400}{P_A}$$

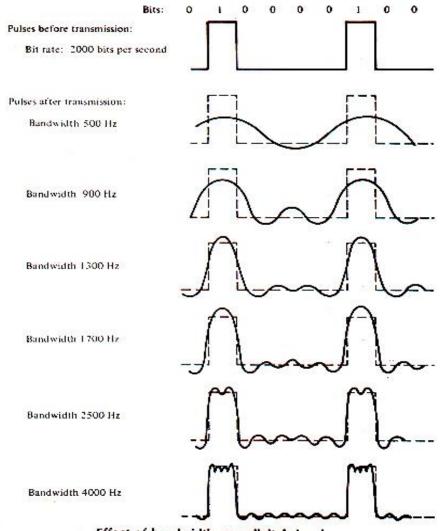
$$\rightarrow P_4 = \frac{400}{3.981}$$

$$\rightarrow P_4 = 100.475 \, mW$$

$$\rightarrow P_4 = 10log_{10} (100.475) = 20.02 \text{ dBm}$$

- \Re Channel Bandwidth specifies the sinusoidal frequency components from 0 up to some frequency f_c that will be transmitted by the channel undiminished. All frequencies above this cutoff frequency are strongly attenuated.
- # In general, channel bandwidth refers to the width of the range of frequencies that channel can transmit, and not the frequency themselves.
- # If the lowest frequency a channel can transmit is f_1 and the highest is f_2 , then the bandwidth is: $f_2 f_1$.
- # Because the **telephone line** can transmit frequencies from approximately 300 to 3300 Hz, its **bandwidth is 3 KHz**.





Effect of bandwidth on a digital signal.

68

- # The sequence 101010... generates the highest-frequency components, while a sequence of all 1s or all 0s is equivalent to a zero frequency of the appropriate amplitude.
- # The **channel capacity** is the data rate, in bit per second (bps), at which data can be communicated.
- In 1928, **Nyquest** developed the relationship between bandwidth (*B*) and the channel capacity (*R*) in <u>noise-free</u> <u>environment</u>. The **Nyquest relationship** is:

$$R = 2B$$

Example:

A binary signal of rate 500 bps is to be transmitted over a communication channel. Derive the minimum bandwidth required assuming:

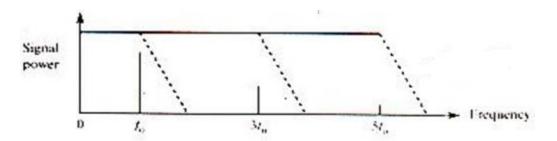
- (a) The fundamental frequency only,
- (b) The fundamental and third harmonic, and
- (c) The fundamental, third, and fifth harmonic of the worst-case sequence are to be received.

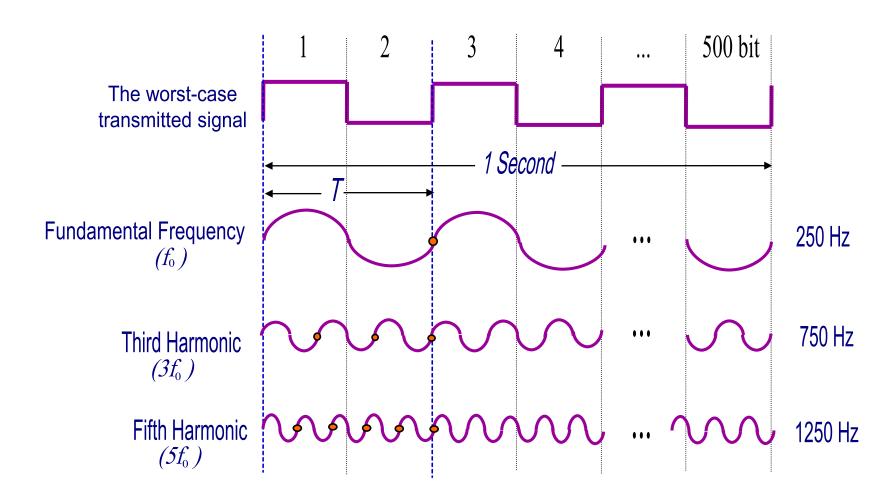
Solution:

The worst case sequence 101010... at 500 bps has a fundamental frequency component of 250 Hz. Hence the third harmonic is 750 Hz and the fifth harmonic is 1250Hz.

The bandwidth required in each case is as follows:

- (a) 0-250 Hz.
- (b) 0-750 Hz.
- (c) 0-1250 Hz.





We can transmit more than one bit with each change in the signal amplitude, therefore increasing the data bit rate.

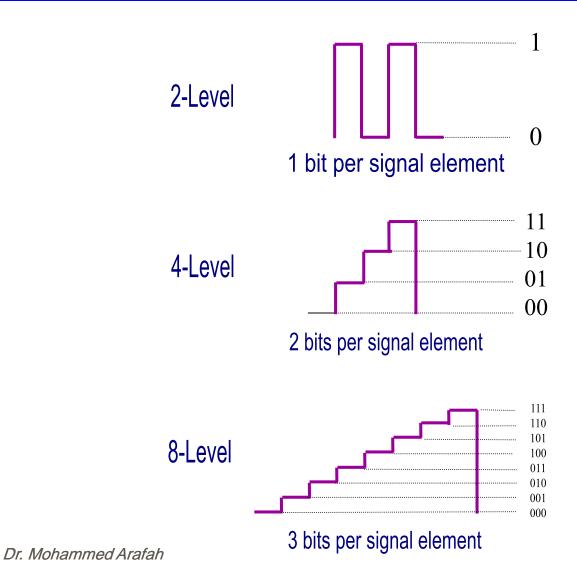
With multilevel signaling in noise-free environment, the Nyquest formulation becomes:

$$R = 2B \log_2 M$$

 \triangle Where R is the channel capacity in bps.

B is the bandwidth of the channel in Hz.

M is the number of levels per signaling elements.



74

For Limited-bandwidth channel such as PSTN, we can often use more than two levels. This means that each signal element can represent more than a single binary digit.

In general, if the number of signal levels is M, the number of bits per signal element m, is given by:

$$m = \log_2 M$$

 \mathbb{H} The rate of change of signal is known as the **signaling** rate (Baud rate) (R_s) , and measures in baud.

$$R_s = 2B$$

It is related to the data bit rate, R, by the following expression:

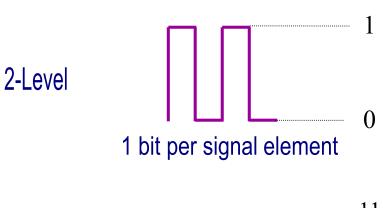
$$R = R_s m$$

 \mathbb{H} The signaling element time period, T_{s} , is given by:

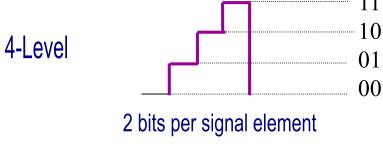
$$T_s = \frac{1}{R_s}$$

The time duration of each bit, T_b , is:

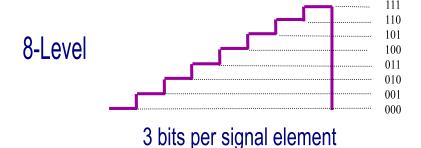
$$T_b = \frac{1}{R}$$



$$M=2 \Longrightarrow m=1 \Longrightarrow R=R_{s}$$



$$M = 4 \Longrightarrow m = 2 \Longrightarrow R = 2 \times R_s$$

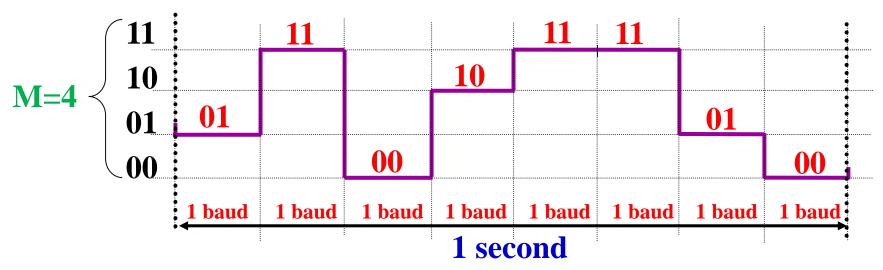


$$M = 8 \Longrightarrow m = 3 \Longrightarrow R = 3 \times R_s$$

77

Example 1: (Theoretical)

Data = 01 11 00 10 11 11 01 00

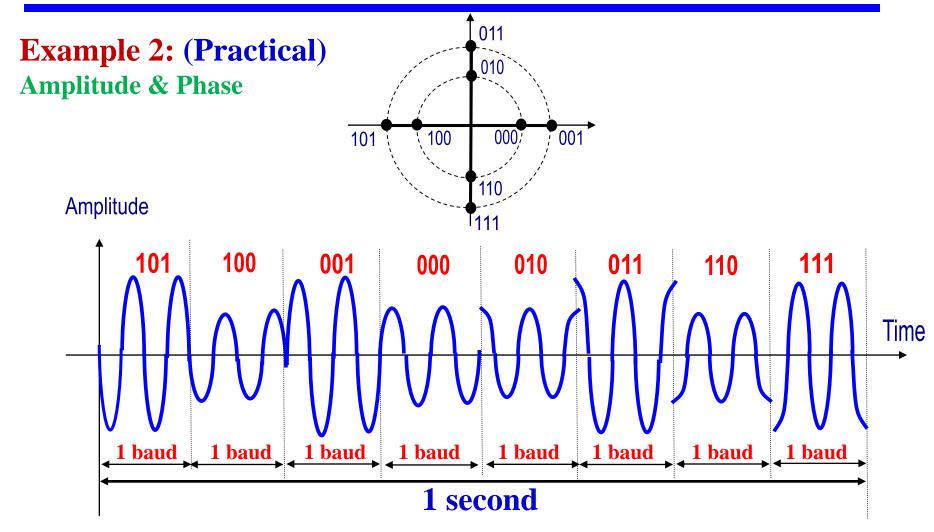


$$M=4 \rightarrow m=2$$

Baud Rate =
$$R_s = 8$$
 baud $\rightarrow T_s = \frac{1}{8}$ sec

$$\mathbf{R} = \mathbf{R}_{s} \times \mathbf{m} = \mathbf{16} \text{ bps}$$
 $\rightarrow T_{b} = \frac{1}{16} \sec$

78

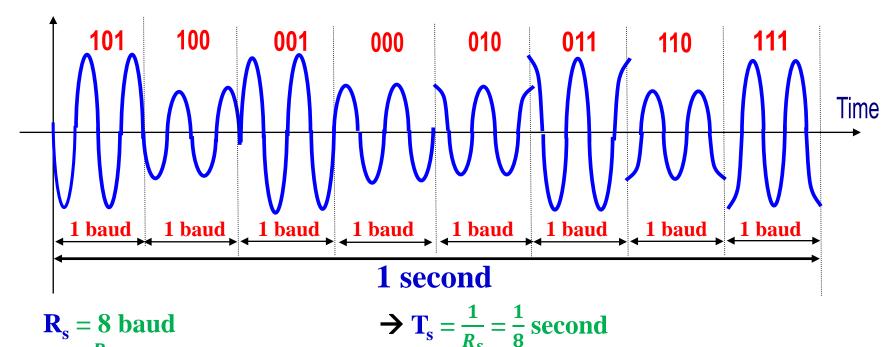


 $\mathbf{R} = \mathbf{m} \times \mathbf{R}_{s} = 3 \times 8 = 24 \text{ bps}$

Example 2: (Practical)

Amplitude & Phase

Amplitude



$$R_s = 8$$
 band

$$\mathbf{B} = \frac{R_s}{2} = 4 \text{ Hz}$$

$$\mathbf{R} = \mathbf{m} \times \mathbf{R}_{s} = 3 \times 8 = 24 \text{ bps} \quad \Rightarrow \mathbf{T}_{b} = \frac{1}{R} = \frac{1}{24} \text{ second}$$

$$\rightarrow$$
 $T_b = \frac{1}{R} = \frac{1}{24}$ second

****The bandwidth efficiency** of transmission channel is defined as:

BandwidthEffeciency=
$$\frac{R}{B} = \frac{2Bm}{B} = 2m$$

Example 1:

Data is to be transmitted over the PSTN using a transmission scheme with eight levels per signaling element. If the bandwidth of the PSTN is 3000 Hz, determine the Nyquest maximum data transfer rate (*R*) and the bandwidth efficiency.

Solution:

$$R = 2Blog_2M$$

$$\rightarrow R = 2 \times 3000 \times 3 = 18000$$
 bps

Bandwidth Efficiency = 2m

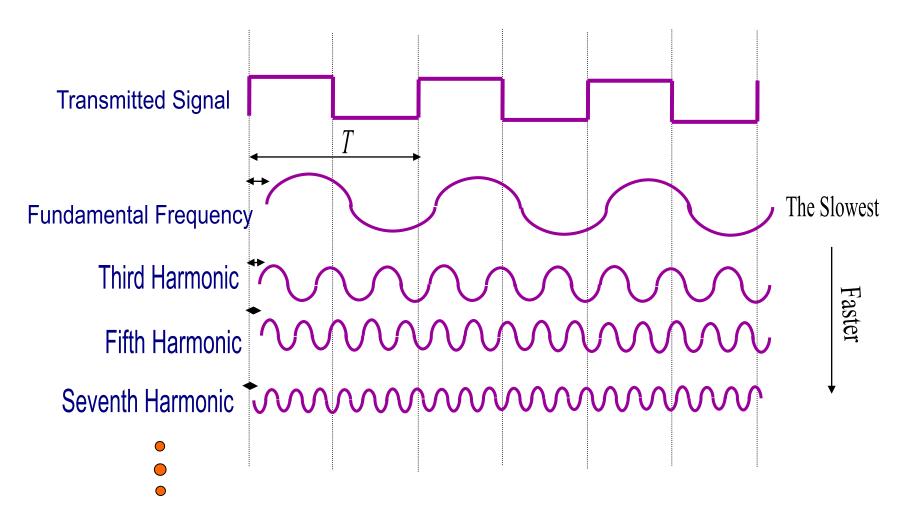
 \rightarrow Bandwidth Efficiency = $2 \times 3 = 6$ bps/Hz

3. Delay Distortion

- **# The rate of propagation of a sinusoidal signal along a transmission line varies with the frequency of the signal.**
- # When we transmit a digital signal with various frequency components, making up the signal, arrive at the receiver with varying delays, resulting in delay distortion of the received signal.

Note that:
$$\lambda = \frac{v}{f}$$
 $\Rightarrow v \propto f$

3. Delay Distortion



******Additional signals inserted between transmitter and receiver

XA.Thermal Noise

- □ Due to thermal agitation of electrons
- □ Uniformly distributed → White noise
- △At all temperatures above absolute zero, all transmission media experience thermal noise, where absolute zero = 0 kelvin (K) = - 273° C.

XThermal Noise

$$N_o = kT$$

where N_o is the noise power density for one Hz (watts/Hz), k is Boltzmann's constant (1.3803 x 10^{-23} joule K⁻¹), and T is the temperature in Kelvin (K).

EXAMPLE 3.1 Room temperature is usually specified as $T = 17^{\circ}\text{C}$, or 290 K. At this temperature, the thermal noise power density is

$$N_0 = (1.38 \times 10^{-23}) \times 290 = 4 \times 10^{-21} \text{ W/Hz} = -204 \text{ dBW/Hz}$$

where dBW is the decibel-watt, defined in Appendix 3A.

XThermal Noise

□ The thermal noise in watts present in a bandwidth of B Hz can be expressed by:

$$N = B \times N_o$$

$$N = 10\log_{10}k + 10\log_{10}T + 10\log_{10}B$$

EXAMPLE 3.2 Given a receiver with an effective noise temperature of 294 K and a 10-MHz bandwidth, the thermal noise level at the receiver's output is

$$N = -228.6 \text{ dBW} + 10 \log(294) + 10 \log 10^7$$

= -228.6 + 24.7 + 70
= -133.9 dBW

B. Intermodulation Noise

- ☐ The effect of intermoduation noise is to produce signals at a frequency that is the sum of two original frequencies or multiples of those frequencies.
- ightharpoonup For example, the mixing of signals at frequencies f_1 and f_2 might produce energy at the frequency f_1 + f_2 .
- This derived signal could interfere with an intended signal at the frequency f_1+f_2 .

B. Intermodulation Noise - Example

$$\mathbf{I} = \cos \mathbf{x} + \cos \mathbf{y}$$

$$\mathbf{i}^{2}$$
Nonlinear System
$$\mathbf{Output} = (\cos \mathbf{x} + \cos \mathbf{y})^{2}$$

$$Output = (\cos x + \cos y)^{2}$$

$$Output = \cos x \cos x + 2\cos x \cos y + \cos y \cos y$$

$$\cos A.\cos B = \frac{1}{2}\cos(A-B) + \frac{1}{2}\cos(A+B)$$

Output =
$$\frac{1}{2}\cos 2x + \frac{1}{2} + \cos(x + y) + \cos(x - y) + \frac{1}{2}\cos 2y + \frac{1}{2}$$

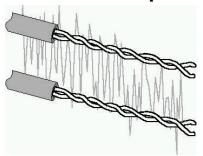
Multiple of Original Frequency

Sum of Two Original Frequencies

Difference of Two Original Frequencies Multiple of Original Frequency

#C. Crosstalk Noise

△A signal from one line is picked up by another



#D. Impulse Noise

△e.g. External electromagnetic interference

△Short duration

The Signal-to-Noise Ratio (SNR) is expressed in decibels as:

$$SNR = 10\log_{10}(\frac{S}{N}) \qquad dB$$

where *S* is the average power in a received signal, and *N* is noise power.

High SNR means a high power signal relative to the prevailing noise level, resulting in a good-quality signal.

In 1948, **Shannon** calculated the theoretical maximum bit rate of a channel of bandwidth B as

$$C = B \log_2(1 + \frac{S}{N})$$

where *C* is the maximum channel capacity in bps, *B* is the bandwidth of the channel in Hz, *S* is the average signal power in watts, and *N* is the thermal noise power in watts.

X Note that:

$$\log_2 x = \frac{\ln x}{\ln 2}$$

$$SNR_{dB} = 10log \frac{S}{N}$$

 $SNR_{dB} = 10log S - 10log N$
 $SNR_{dB} = S_{dBW} - N_{dBW}$

Example:

S is Given

N can be calculated using N=B kT

Method 1:

Calculate $\frac{s}{N}$

Then calculate $SNR_{dB} = 10log \frac{S}{N}$

Method 2:

Calculate $S_{dBW} = 10logS$ and calculate $N_{dBW} = 10logN$ Then calculate $SNR_{dB} = S_{dBW} - N_{dBW}$

93

Example 1:

Assuming that a PSTN has a bandwidth of 3000 Hz and a signal-to-noise ratio of 20 dB, determine the maximum theoretical data rate that can be achieved.

Solution:

$$SNR = 10 \log_{10}(\frac{S}{N})$$
 \implies $20 = 10 \log_{10}(\frac{S}{N})$ \implies $\frac{S}{N} = 10^2 = 100$

$$C = B \log_2(1 + \frac{S}{N})$$

$$C = 3000 \log_2(1+100) \qquad C = 3000 \frac{\ln 101}{\ln 2} = 19963 \, bps$$

Example 2:

EXAMPLE 3.4 Let us consider an example that relates the Nyquist and Shannon formulations. Suppose that the spectrum of a channel is between 3 MHz and 4 MHz and $5 \text{NR}_{dB} = 24 \text{ dB}$. Then

$$B = 4 \text{ MHz} - 3 \text{ MHz} = 1 \text{ MHz}$$

$$SNR_{dB} = 24 \text{ dB} = 10 \log_{10}(SNR)$$

$$SNR = 251$$

Using Shannon's formula,

$$C = 10^6 \times \log_2(1 + 251) \approx 10^6 \times 8 = 8 \text{ Mbps}$$

This is a theoretical limit and, as we have said, is unlikely to be reached. But assume we can achieve the limit. Based on Nyquist's formula, how many signaling levels are required? We have

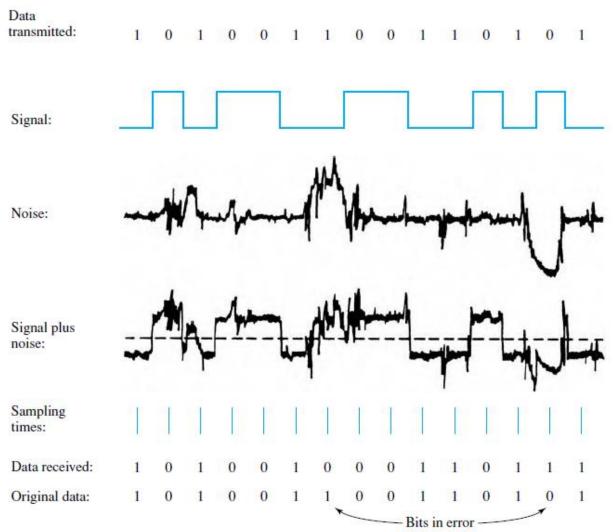
$$C = 2B \log_2 M$$

$$8 \times 10^6 = 2 \times (10^6) \times \log_2 M$$

$$4 = \log_2 M$$

$$M = 16$$

Effect of Noise on a Digital Signal



The Expression E_b/N_0

- ****** The parameter is the ratio of signal energy per bit to noise power density per Hertz
- ****** Consider a signal, digital or analog, that contains binary digital data transmitted at a certain bit rate *R*.
- \mathbb{H} Recalling that 1 Watt = 1 J/s, the energy per bit in a signal is given by $E_b = ST_b$, where S is the signal power and is the T_b is the time required to send one bit.
- \Re The data rate R is just $R = 1/T_b$. Thus

$$\frac{E_b}{N_0} = \frac{S/R}{N_0} = \frac{S}{kTR}$$

The Expression E_b/N_o

₩ or, in decibel notation,

$$\left| \left(\frac{E_b}{N_0} \right)_{dB} = 10 \log_{10} S - 10 \log_{10} R - 10 \log_{10} k - 10 \log_{10} T \right|$$

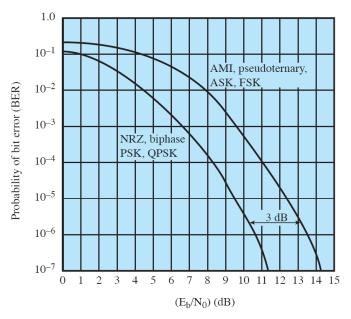
$$\left(\frac{E_b}{N_0}\right)_{dB} = S_{dBW} - 10\log_{10}R + 228.6_{dBW} - 10\log_{10}T$$

Dr. Mohammed Arafah

98

The Expression E_b/N_0

The ratio E_b/N_0 is important because the **bit error rate** for digital data is a (decreasing) function of this ratio.



- # Given a value of needed to achieve a desired error rate, the parameters in the preceding formula may be selected.
- \divideontimes Note that as the bit rate *R* increases, the transmitted signal power, relative to noise, must increase to maintain the required E_h/N_0 .

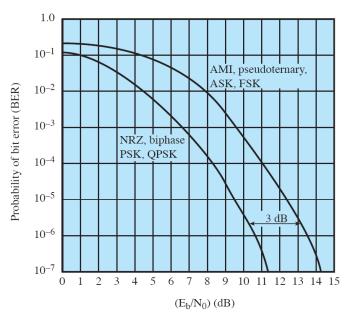
The Expression E_b/N_0

- # Thus, for constant signal to noise ratio (SNR), an increase in data rate increases the error rate.
- # The advantage of E_b/N_0 over SNR is that the latter quantity depends on the bandwidth.

EXAMPLE 3.5 For binary phase-shift keying (defined in Chapter 5), $E_b/N_0 = 8.4$ dB is required for a bit error rate of 10^{-4} (one bit error out of every 10,000). If the effective noise temperature is 290°K (room temperature) and the data rate is 2400 bps, what received signal level is required?

We have

$$8.4 = S(dBW) - 10 \log 2400 + 228.6 dBW - 10 \log 290$$
$$= S(dBW) - (10)(3.38) + 228.6 - (10)(2.46)$$
$$S = -161.8 dBW$$



The Expression E_b/N_o

We can relate E_b/N_0 to SNR as follows. We have:

$$\left| \frac{E_b}{N_0} = \frac{S}{N_0 R} \right|$$

The parameter N_0 is the noise power density in Watts/Hertz. Hence, the noise in a signal with bandwidth B is $N = N_0 B$. Substituting, we have:

$$\frac{E_b}{N_0} = \frac{S}{N} \times \frac{B}{R}$$

$$\frac{S}{N} = \frac{E_b}{N_0} \times \frac{R}{B}$$

The Expression E_h/N_0

- \mathbb{H} Another formulation of interest relates E_h/N_0 to spectral efficiency.
- **#** Shannon's result can be rewritten as:

$$C = B \log_2(1 + \frac{S}{N})$$
 $\frac{S}{N} = 2^{C/B} - 1$

$$\frac{S}{N} = 2^{C/B} - 1$$

$$\frac{E_b}{N_0} = \frac{B}{C} (2^{C/B} - 1)$$

This is a useful formula that relates the achievable spectral efficiency C/B to E_h/N_o .

> **EXAMPLE 3.6** Suppose we want to find the minimum E_b/N_0 required to achieve a spectral efficiency of 6 bps/Hz. Then

$$E_b/N_0 = (1/6)(2^6 - 1) = 10.5 = 10.21 \text{ dB}.$$

Required Reading

#Stallings chapter 3