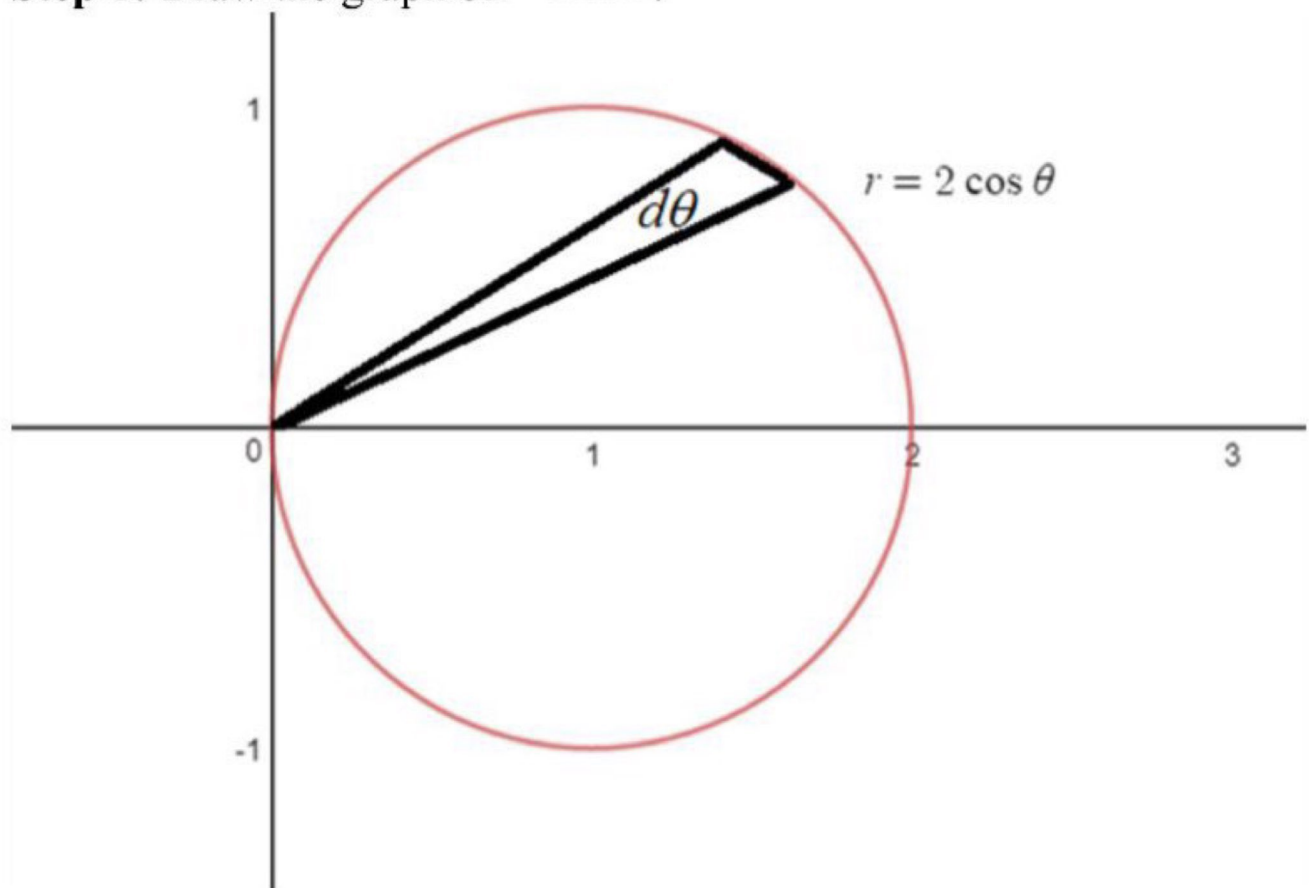


Consider, $r = 2 \cos \theta$

Step 1: Draw the graph of $r = 2 \cos \theta$.



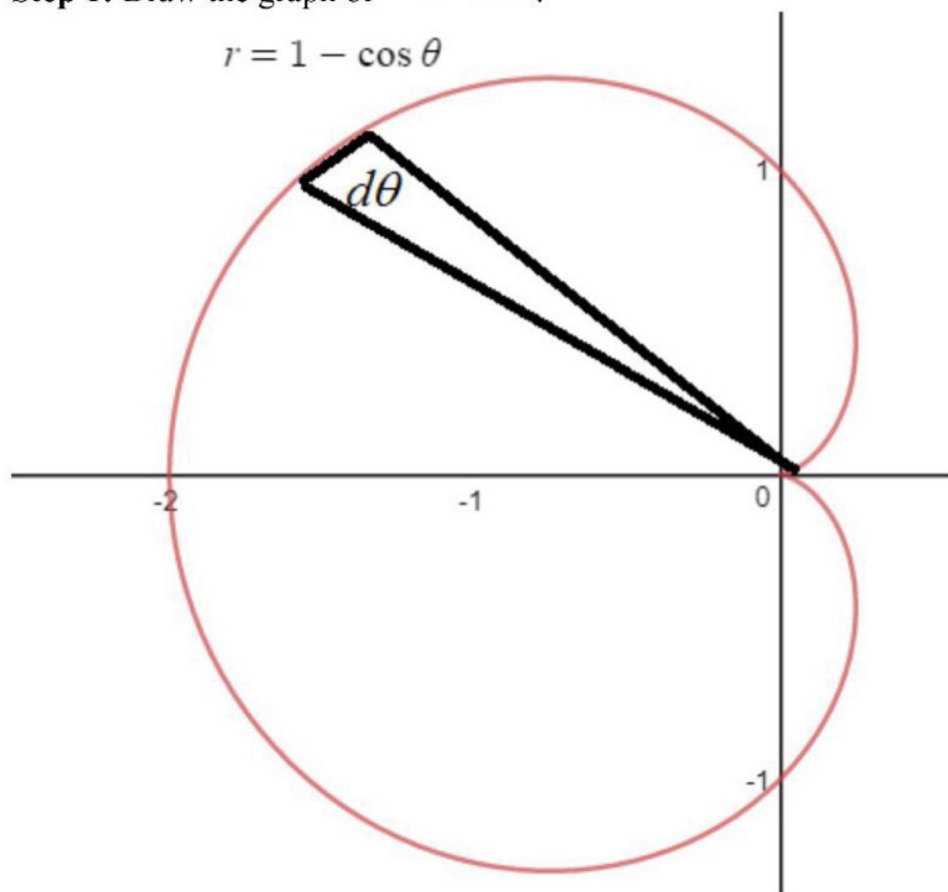
Step 2: Take $\alpha = 0$ and $\beta = \frac{\pi}{2}$ for smallest and larger value of θ .

Step 3: Find the area of the area of the region bounded by $r = 2\cos\theta$ using $A = \frac{1}{2} \int_{\alpha}^{\beta} r^2 d\theta$
Required area = $2A$

$$\begin{aligned} &= 2 \int_0^{\frac{\pi}{2}} \frac{1}{2} (2\cos\theta)^2 d\theta \\ &= 4 \int_0^{\frac{\pi}{2}} \cos^2 \theta d\theta \\ &= 4 \int_0^{\frac{\pi}{2}} \left(\frac{1 + \cos 2\theta}{2} \right) d\theta \\ &= 2 \int_0^{\frac{\pi}{2}} (1 + \cos 2\theta) d\theta \\ &= 2 \left[\theta + \frac{\sin 2\theta}{2} \right]_0^{\frac{\pi}{2}} \\ &= 2 \left(\frac{\pi}{2} - 0 \right) \\ &= \pi \end{aligned}$$

Consider, $r = 1 - \cos \theta$

Step 1: Draw the graph of $r = 1 - \cos \theta$.



Step 2: Take $\alpha = 0$ and $\beta = \pi$ for smallest and larger value of θ .

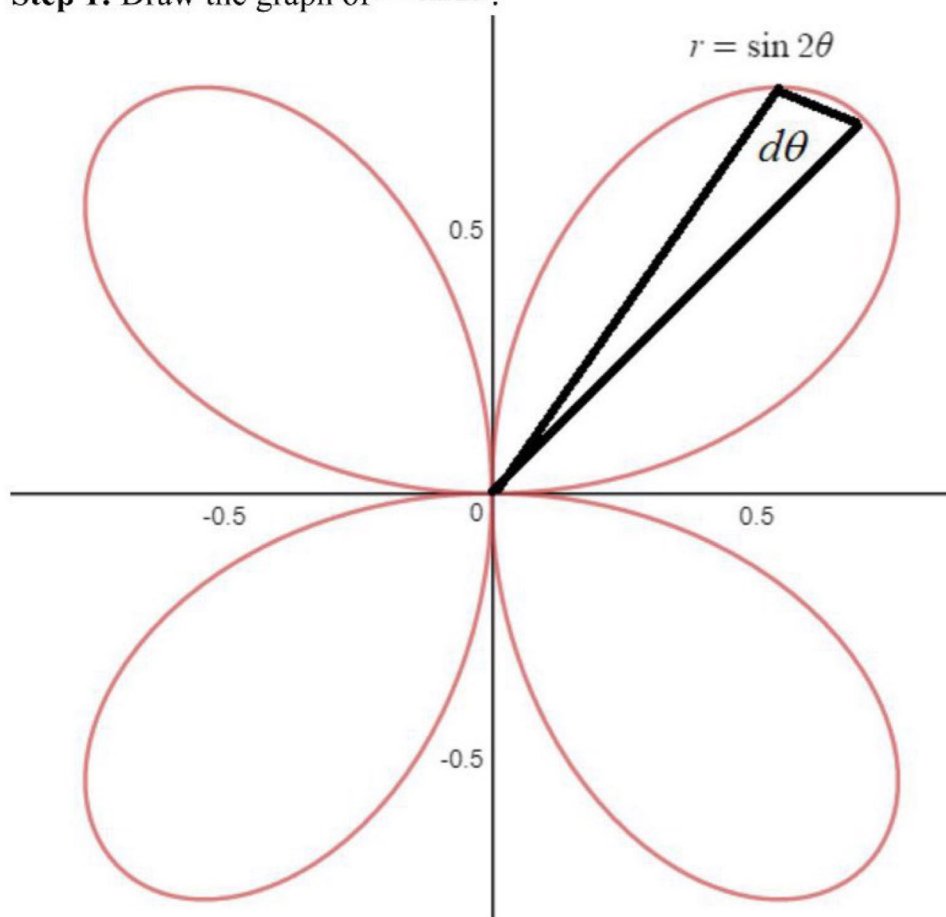
Step 3: Find the area of the area of the region bounded by $r = 1 - \cos \theta$ using

$$A = \frac{1}{2} \int_{\alpha}^{\beta} r^2 d\theta$$

$$\begin{aligned} \text{Required area} &= 2 \int_0^{\pi} \frac{1}{2} (1 - \cos \theta)^2 d\theta \\ &= \int_0^{\pi} (1 + \cos^2 \theta - 2 \cos \theta) d\theta \\ &= \int_0^{\pi} \left(1 + \frac{1 + \cos 2\theta}{2} - 2 \cos \theta \right) d\theta \\ &= \frac{1}{2} \int_0^{\pi} (3 + \cos 2\theta - 4 \cos \theta) d\theta \\ &= \frac{1}{2} \left[3\theta + \frac{\sin 2\theta}{2} - 4 \sin \theta \right]_0^{\pi} \\ &= \frac{3\pi}{2} \end{aligned}$$

Consider, $r = \sin 2\theta$

Step 1: Draw the graph of $r = \sin 2\theta$.



Step 2: Take $\alpha = 0$ and $\beta = \frac{\pi}{2}$ for smallest and larger value of θ .

Step 3: Find the area of the area of the region bounded by $r = \sin 2\theta$ using $A = \frac{1}{2} \int_a^\beta r^2 d\theta$
Required area = $4A$

$$\begin{aligned} &= 4 \int_0^{\frac{\pi}{2}} \frac{1}{2} (\sin 2\theta)^2 d\theta \\ &= 2 \int_0^{\frac{\pi}{2}} \sin^2 2\theta d\theta \\ &= 2 \int_0^{\frac{\pi}{2}} \left(\frac{1 - \cos 4\theta}{2} \right) d\theta \\ &= \int_0^{\frac{\pi}{2}} (1 - \cos 4\theta) d\theta \\ &= \left[\theta - \frac{\sin 4\theta}{4} \right]_0^{\frac{\pi}{2}} \\ &= \left(\frac{\pi}{2} - 0 \right) \\ &= \frac{\pi}{2} \end{aligned}$$