## Chapter 11 <br> Replacement Analysis

In comparing various investment alternatives in Chapters 5 thru 10, we considered a single alternative (where the decision is between investing and not investing) and a set of mutually exclusive alternatives (where we recommended the alternative having the greatest economic worth). Both situations could involve a replacement of an existing asset.

In the case of the single alternative, a decision not to invest in a new asset could be a decision to continue using a current asset; likewise, a decision to invest could be a decision to replace a current asset. The same holds for mutually exclusive alternatives, since one alternative could be continued usage of an existing asset (continue using current asset or replace it).

Because decisions to replace versus continue using an asset occur so frequently, a body of literature has evolved treating replacement decisions. We refer to the comparison of investment alternatives that involve the replacement of an asset as replacement analysis.

Replacement decisions occur all around us. Perhaps you have replaced a camera, car, cell phone, computer, printer, sound system, or television. If so, then your decision was probably influenced by economics, capacity concerns, deteriorating quality of service provided, changing requirements, prestige, fads, or a host of other reasons.

## Replacement decisions occur for a variety of reasons, including:

1. the current asset, which we call the defender, has developed several deficiencies, including high set-up cost, excessive maintenance expense, declining productivity, high energy cost, limited capability, and physical impairment;
2. potential replacement assets, which we call the challengers, are available which have a number of advantages over the defender, including new technology that is quicker to set-up and easier to use, along with having lower labor cost, lower maintenance expense, lower energy cost, higher productivity, and additional capabilities; and
3. a changing external environment, including
a) changing user and customer preferences and expectations,
b) changing requirements,
c) new, alternative ways of obtaining the functionality provided by the defender, including the availability of leased equipment and third-party suppliers, and
d) increased demand that cannot be met with the current equipment either supplementary equipment or replacement equipment is required to meet demand.

Although replacement of existing assets can offer considerable potential for increasing shareholder value, many firms fail to subject existing equipment to careful assesment on a periodic basis to ensure that capital is being used in the most effective manner. Why?

- Currently making a profit
- Equipment is operational
- Risks associated with change
- Decision to change is a future commitment
- Limited investment capital
- Uncertainty regarding future
- Psychological impact of sunk costs
- Technological improvement trap
- Prefer to be a "technology follower"
- Taking a "financial hit" on financial statements by writing off assets not fully depreciated


## Principle \#2 <br> Make investments that are economically justified <br> "If you need a new machine and don't buy it, you pay for it without ever getting it." <br> Henry Ford

## Principal Reason for Replacing an Asset: Obsolescence

*Functional obsolescence *Technological obsolescence *Economic obsolescence

## Replacement Analysis

Two approaches are commonly used in replacement analyses: the cash flow approach or insider approach and the opportunity cost approach or outsider viewpoint approach.

I If performed correctly, the two approaches will yield the same recommendation. (The essential difference in the two relates to how the salvage value of the defender is treated.)

We have not "made a big deal" out of replacement problems, since we prefer to treat them as just another investment alternative. Hence, we advocate using the same systematic approach when solving replacement problems.

## Systematic Economic Analysis Technique

 1. Identify the investment alternatives2. Define the planning horizon
3. Specify the discount rate
4. Estimate the cash flows
5. Compare the alternatives
6. Perform supplementary analyses
7. Select the preferred investment

## Cash Flow Approach

## Before-Tax Analysis

## Cash Flow Approach

The cash flow approach can be called the insider viewpoint approach. The cash flows used are those that are "seen" by the internal decision maker in answer to the question, "how much money will be spent and how much will be received if I adopt this alternative?" In sum, we are interested in knowing how much money will be spent and received/saved if the asset is replaced and how much money will be spent and received/saved if it is retained.

## Caution

# In performing replacement analyses, beware of sunk costs! 

A sunk cost is a cost that has already been incurred and cannot be recovered

## Example 11.1

A surface mount placement machine was acquired 10 years ago for $\$ 300,000$. It can be kept for a maximum of 5 more years, at which time it will have a negligible salvage value. Annual O\&M costs for the defender have been increasing by $\$ 5,000$ a year since its acquisition. Next year, the O\&M costs will total $\$ 120,000$.

A new SMP machine (challenger) being considered as a replacement for the defender has a current market value of $\$ 50,000$. The new SMP machine will cost $\$ 500,000$ and have annual $0 \& M$ costs of $\$ 10,000$ the first year, increasing by \$5,000 a year.

Based on the remaining useful life of the defender, a 5 -year planning horizon is used. After 5 years, the challenger will have a market value of $\$ 200,000$. With a BTMARR of $16.67 \%$, should the defender be replaced?

## Solution to Example 11.1

The cash flows for the defender (alternative 1) and challenger (alternative 2) are shown below. Based on the following incremental EUAC (Equivalent Uniform Annualized Cost) analysis, it is recommended that the defender continue to be used until a more attractive challenger is identified.
$E U A C_{2-1}(16.67 \%)=\$ 450,000(A / P 16.67 \%, 5)-\$ 200,000(A / F 16.67 \%, 5)$

- \$110,000 = \$890.00 > \$0*
$=$ PMT(16.67\%,5,-450000,200000)-110000 = \$889.06

| EOY | CF(1) | CF(2) | $\mathbf{C F}(\mathbf{2}) \mathbf{- C F}(\mathbf{1})$ |
| :---: | ---: | ---: | ---: |
| 0 | $\$ 0.00$ | $-\$ 450,000.00$ | $-\$ 450,000.00$ |
| 1 | $-\$ 120,000.00$ | $-\$ 10,000.00$ | $\$ 110,000.00$ |
| 2 | $-\$ 125,000.00$ | $-\$ 15,000.00$ | $\$ 110,000.00$ |
| 3 | $-\$ 130,000.00$ | $-\$ 20,000.00$ | $\$ 110,000.00$ |
| 4 | $-\$ 135,000.00$ | $-\$ 25,000.00$ | $\$ 110,000.00$ |
| 5 | $-\$ 140,000.00$ | $\$ 170,000.00$ | $\$ 310,000.00$ |

* EUAC > \$0 means AW < \$0

Principles of Engineering Economic Analysis, 5th edition

## Solution to Example 11.1

The cash flows for the defender (alternative 1) and challenger (alternative 2) are shown below. Based on the following incremental EUAC analysis, it is recommended that the defender continue to be used until a more attractive challenger is identified.
$E U A C_{2-1}(16.67 \%)=\$ 450,000(A / P 16.67 \%, 5)-\$ 200,000(A / F 16.67 \%, 5)$

- \$110,000 = \$890.00 > \$0*
$=$ PMT(16.67\%,5,-450000,200000)-110000 = \$889.06


## Since EUAC ${ }_{2-1}$ (16.67\%) > \$0, Do Not Replace!

| $-\$ 130,000.00$ | $-\$ 20,000.00$ | $\$ 110,000.00$ |
| :--- | :--- | :--- |
| $-\$ 135,000.00$ | $-\$ 25,000.00$ | $\$ 110,000.00$ |
| $-\$ 140,000.00$ | $\$ 170,000.00$ | $\$ 310,000.00$ |

* EUAC > \$0 means AW < \$0

Principles of Engineering Economic Analysis, 5th edition

## Example 11.2

A filter press was purchased 3 yrs ago for $\$ 30,000$. O\&M costs are expected to be $\$ 7,000$ next year if the filter press is kept; they will increase by $\$ 1,000$ per year, thereafter. In 5 yrs, the filter press can be sold for $\$ 2,000$. Its book value is $\$ 21,000$.

A new filter press can be purchased for $\$ 36,000$. purchased, the old filter press can be sold for $\$ 9,000$. O\&M costs will follow a $\$ 1,000$ gradient series, with no cost in the first year. At the end of 5 yrs, the new press will have a $\$ 12,000$ salvage value.

With a $15 \%$ BTMARR, what should be done?

## Solution to Example 11.2

$$
\begin{aligned}
& \text { Alternative 1: keep the old press } \\
& \text { AW(15\%) }=-\$ 7,000-\$ 1,000(A \mid G 15 \%, 5) \\
& \text { + \$2,000(A|F 15\%,5) } \\
& \text { AW(15\%) }=-\$ 7,000-\$ 1,000(1.72281) \\
& \text { + \$2,000(0.14832) } \\
& \text { AW(15\%) = -\$8,426.17/yr } \\
& \text { Alternative 2: replace old press } \\
& \text { AW(15\%) = -\$27,000(A|P 15\%,5) - \$1,000(A|G 15\%,5) } \\
& \text { + \$12,000(A|F 15\%,5) } \\
& \mathrm{AW}(15 \%)=-\$ 27,000(0.29832)-\$ 1,000(1.72281) \\
& \text { + \$12,000(0.14832) } \\
& \text { AW(15\%) }=-\$ 7,997.61 / \mathrm{yr} \\
& \mathrm{AW}_{2-1}(15 \%)=\$ 428.56 \\
& \text { Replace the filter press! }
\end{aligned}
$$

## Example 11.3

In the previous example, what should be done if a 10-yr planning horizon is used, a replacement press will cost $\$ 31,000$ in 5 yrs and have a salvage value of \$15,000 after 5 yrs use, and O\&M costs for the new press will be a $\$ 1,000$ gradient series? Assume a salvage value of $\$ 3000$ for the challenger at the end of the $10^{\text {th }}$ year.

| EOY | CF(1) | CF(2) |
| :---: | ---: | ---: |
| 0 | $\$ 0.00$ | $-\$ 27,000.00$ |
| 1 | $-\$ 7,000.00$ | $\$ 0.00$ |
| 2 | $-\$ 8,000.00$ | $-\$ 1,000.00$ |
| 3 | $-\$ 9,000.00$ | $-\$ 2,000.00$ |
| 4 | $-\$ 10,000.00$ | $-\$ 3,000.00$ |
| 5 | $-\$ 40,000.00$ | $-\$ 4,000.00$ |
| 6 | $\$ 0.00$ | $-\$ 5,000.00$ |
| 7 | $-\$ 1,000.00$ | $-\$ 6,000.00$ |
| 8 | $-\$ 2,000.00$ | $-\$ 7,000.00$ |
| 9 | $-\$ 3,000.00$ | $-\$ 8,000.00$ |
| 10 | $\$ 11,000.00$ | $-\$ 6,000.00$ |

## Example 11.3

In the previous example, what should be done if a 10-yr planning horizon is used, a replacement press will cost $\$ 31,000$ in 5 yrs and have a salvage value of $\$ 15,000$ after 5 yrs use, and O\&M costs for the new press will be a $\$ 1,000$ gradient series? Assume a salvage value of $\$ 3000$ for the challenger at the end of the $10^{\text {th }}$ year.

|  | EOY | CF(1) | CF(2) |
| :---: | :---: | :---: | :---: |
|  | 0 | \$0.00 | -\$27,000.00 |
|  | 1 | -\$7,000.00 | \$0.00 |
|  | 2 | -\$8,000.00 | -\$1,000.00 |
| $+\$ 2,000=-\$ 40,000$ | 4 | -\$9,000.00 | -\$2,000.00 |
| $+\$ 2,000=-\$ 40,000$ | 4 | $\text { -\$10, } \$ 40,000.00$ | -\$3,000.00 |
|  | 5 |  | -\$4,000.00 |
|  |  | \$0.00 | -\$5,000.00 |
|  | 1 | -\$1,000.00 | -\$6,000.00 |
|  | 8 | -\$2,000.00 | -\$7,000.00 |
|  | 9 | -\$3,000.00 | -\$8,000.00 |
|  | 10 | \$11,000.00 | -\$6,000.00 |

## Example 11.3

In the previous example, what should be done if a 10-yr planning horizon is used, a replacement press will cost $\$ 31,000$ in 5 yrs and have a salvage value of $\$ 15,000$ after 5 yrs use, and O\&M costs for the new press will be a $\$ 1,000$ gradient series? Assume a salvage value of $\$ 3000$ for the challenger at the end of the $10^{\text {th }}$ year.

|  | EOY | CF(1) | CF(2) |
| :---: | :---: | :---: | :---: |
|  | 0 | \$0.00 | -\$27,000.00 |
|  | 1 | -\$7,000.00 | \$0.00 |
|  | 2 | -\$8,000.00 | -\$1,000.00 |
|  | 3 | -\$9,000.00 | -\$2,000.00 |
|  | 4 | -\$10,000.00 | -\$3,000.00 |
|  | 5 | -\$40,000.00 | -\$4,000.00 |
|  | 6 | \$0.00 | -\$5,000.00 |
|  | 7 | -\$1,000.00 | -\$6,000.00 |
|  | -\$2,000.00 |  | -\$7,000.00 |
| -\$4,000 + \$15,000 = | $10 \$ 11,000.00$ |  | -\$8,000.00 |
| \$11,000 |  |  | -\$6,000.00 |

## Example 11.3

In the previous example, what should be done if a 10-yr planning horizon is used, a replacement press will cost $\$ 31,000$ in 5 yrs and have a salvage value of $\$ 15,000$ after 5 yrs use, and O\&M costs for the new press will be a $\$ 1,000$ gradient series? Assume a salvage value of $\$ 3000$ for the challenger at the end of the $10^{\text {th }}$ year.

| EOY | CF(1) | CF(2) |  |
| :---: | :---: | :---: | :---: |
| 0 | \$0.00 | -\$27,000.00 |  |
| 1 | -\$7,000.00 | \$0.00 |  |
| 2 | -\$8,000.00 | -\$1,000.00 |  |
| 3 | -\$9,000.00 | -\$2,000.00 |  |
| 4 | -\$10,000.00 | -\$3,000 00 |  |
| 5 | -\$40,000.00 | -\$4.0.0.0 | $-\$ 9,000+\$ 3,000=$ |
| 6 | \$0.00 | -25,000.00 |  |
| 7 | -\$1,000.00 | \$6,000.00 | Table 11.2 shows |
| 8 | -\$2,000.00 | -考7,000.00 | $\mathrm{S}_{2,10}=\$ 3,000$ |
| 9 | -\$3,000.0 | -\$800 |  |
| 10 | \$11,000\% | -\$6,000.00 |  |

## Solution to Example 11.3

$$
\begin{aligned}
E U A C_{1}(15 \%)= & {[\$ 7,000(P / A 15 \%, 5)+\$ 1,000(P / G 15 \%, 5)} \\
& +\$ 29,000(P / F 15 \%, 5)+\$ 1,000(P / G 15 \%, 5)(P / F 15 \%, 5) \\
& -\$ 15,000(P / F 15 \%, 10)](A / P 15 \%, 10) \\
= & {[\$ 7,000(3.35216)+\$ 1,000(5.77514)+\$ 29,000(0.49718)} \\
& +\$ 1,000(5.77514)(0.49718)-\$ 15,000(0.24718)](0.19925) \\
= & \$ 8,532.30 / \mathrm{yr} \\
E U A C_{2}(15 \%)= & \$ 27,000(A / P 15 \%, 10)+\$ 1,000(A / G 15 \%, 10) \\
& -\$ 3,000(A / F 15 \%, 10) \\
= & \$ 27,000(0.19925)+\$ 1,000(3.38320)-\$ 3,000(0.04925) \\
= & \$ 8,615.20 / \mathrm{yr} \\
& \\
& \text { Keep the Filter Press!}
\end{aligned}
$$

The technology forecast for filter presses reversed the recommendation.

## Example 11.4

In Example 11.2, suppose the equipment supplier offers a $\$ 10,000$ trade-in for the old press (CF 2). Also, suppose two new alternatives are considered: a $\$ 40,000$ filter press having a $\$ 13,000$ salvage value in 5 yrs, O\&M equal to a $\$ 500$ gradient series on a $\$ 500$ base, and a $\$ 12,000$ trade-in for the old press (CF3); and a leased press, with $\$ 7,500$ beginning-of-year lease costs and end-of-year O\&M costs given by an $\$ 800$ gradient series. If leasing is pursued, the old press will be sold for \$9,000.

| EOY | CF(1) | CF(2) | $\mathbf{C F ( 3 )}$ | CF(4) |
| :---: | ---: | ---: | ---: | :--- |
| 0 | $\$ 0.00$ | $-\$ 26,000.00$ | $-\$ 28,000.00$ | $\$ 1,500.00$ |
| 1 | $-\$ 7,000.00$ | $\$ 0.00$ | $-\$ 500.00$ | $-\$ 7,500.00$ |
| 2 | $-\$ 8,000.00$ | $-\$ 1,000.00$ | $-\$ 1,000.00$ | $-\$ 8,300.00$ |
| 3 | $-\$ 9,000.00$ | $-\$ 2,000.00$ | $-\$ 1,500.00$ | $-\$ 9,100.00$ |
| 4 | $-\$ 10,000.00$ | $-\$ 3,000.00$ | $-\$ 2,000.00$ | $-\$ 9,900.00$ |
| 5 | $-\$ 9,000.00$ | $\$ 8,000.00$ | $\$ 10,500.00$ | $-\$ 3,200.00$ |

## Example 11.4

In Example 11.2, suppose the equipment supplier offers a $\$ 10,000$ trade-in for the old press. Also, suppose two new alternatives are considered: a $\$ 40,000$ filter press having a $\$ 13,000$ salvage value in 5 yrs , $\mathrm{O} \& \mathrm{M}$ equal to a $\$ 500$ gradient series on a $\$ 500$ base, and a $\$ 12,000$ trade-in for the old press; and a leased press, with $\$ 7,500$ beginning-ofyear lease costs and end-of-year O\&M costs given by an $\$ 800$ gradient series. If leasing is pursued, the old press will be sold for \$9,000.

| EOY | CF(1) | CF(2) | CF(3) | CF(4) |
| :---: | ---: | :---: | :---: | :---: |
| 0 | $\$ 0.00$ | $-\$ 26,000.00$ | $-\$ 28,000$ | $\$ 1,500.00$ |
| 1 | $-\$ 7,000.00$ | $\$ 0.00$ | $-\$ 500$. | $-\$ 7,500.00$ |
| 2 | $-\$ 8,000.00$ | $-\$ 1,000.00$ | $-\$ 1,000.0$ | $-\$ 8,300.00$ |
| 3 | $-\$ 9,000.00$ | $-\$ 2,000$ | $-\$ 36,000+\$ 10,000$ | $-\$ 9,100.00$ |
| 4 | $-\$ 10,000.00$ | $-\$ 3,000$ | $=\$ 26,000$ | $-\$ 9,900.00$ |
| 5 | $-\$ 9,000.00$ | $\$ 8,000.00$ | $\$ 10,500.00$ | $-\$ 3,200.00$ |

## Example 11.4

In Example 11.2, suppose the equipment supplier offers a $\$ 10,000$ trade-in for the old press. Also, suppose two new alternatives are considered: a \$40,000 filter press having a $\$ 13,000$ salvage value in $5 \mathrm{yrs}, \mathrm{O} \& \mathrm{M}$ equal to a $\$ 500$ gradient series on a $\$ 500$ base, and a $\$ 12,000$ trade-in for the old press; and a leased press, with $\$ 7,500$ beginning-ofyear lease costs and end-of-year O\&M costs given by an $\$ 800$ gradient series. If leasing is pursued, the old press will be sold for \$9,000.

| EOY | CF(1) | CF(2) | CF(3) | CF(4) |
| :---: | :---: | :---: | :---: | :---: |
| 0 | \$0.00 | -\$26,000.00 | -\$28,000.00 | 500.00 |
| 1 | -\$7,000.00 | \$0.00 | -\$500.00 | (p, 500.00 |
| 2 | -\$8,000.00 | -\$1,000.00 | -\$1,000.00 | -\$8, 00.00 |
| 3 | -\$9,000.00 | -\$2,000.00 | -\$1.500.00 | - 00.00 |
| 4 | -\$10,000.00 | -\$3,000.00 | -\$40,000 + \$12,000 | - 00.00 |
| 5 | -\$9,000.00 | \$8,000.00 | $=-\$ 28,000$ | S,200.00 |

## Example 11.4

In Example 11.2, suppose the equipment supplier offers a $\$ 10,000$ trade-in for the old press. Also, suppose two new alternatives are considered: a $\$ 40,000$ filter press having a $\$ 13,000$ salvage value in 5 yrs , $\mathrm{O} \& \mathrm{M}$ equal to a $\$ 500$ gradient series on a $\$ 500$ base, and a $\$ 12,000$ trade-in for the old press; and a leased press, with $\$ 7,500$ beginning-ofyear lease costs and end-of-year O\&M costs given by an $\$ 800$ gradient series. If leasing is pursued, the old press will be sold for $\$ 9,000$.

| EOY | CF(1) | CF(2) | CF(3) | CF(4) |
| :---: | :---: | :---: | :---: | :---: |
| 0 | \$0.00 | -\$26,000.00 | -\$28,000 | \$1,500.00 |
| 1 | -\$7,000.00 | \$0.00 | -\$500 | -\$7,500.00 |
| 2 | -\$8,000.00 | -\$1,000.00 | -\$1,000.00 | -\$8,300.00 |
| 3 | -\$9,000.00 | -\$2,000.00 | -\$1,500 0 | -\$9,100.00 |
| 4 | -\$10,000.00 | -\$3,000.00 | -\$2,000 | \$9,000-\$7,5 |
| 5 | -\$9,000.00 | \$8,000.00 | \$10,500. | \$1,500 |

## Solution to Example 11.4

$$
\begin{aligned}
E U A C_{1}(15 \%) & =\$ 7,000+\$ 1,000(A / G 15 \%, 5)-\$ 2,000(A / F 15 \%, 5) \\
& =\$ 7,000+\$ 1,000(1.72281)-\$ 2,000(0.14832) \\
& =\$ 8,426.17 / \mathrm{yr}(\$ 8,426.18 \text { with Excel } ®)
\end{aligned}
$$

$$
\begin{aligned}
E U A C_{2}(15 \%) & =\$ 26,000(A / P 15 \%, 5)+\$ 1,000(A / G 15 \%, 5)-\$ 12,000(A / F 15 \%, 5) \\
& =\$ 26,000(0.29832)+\$ 1,000(1.72281)-\$ 12,000(0.14832) \\
& =\$ 7,699.29 / \mathrm{yr}(\$ 7,699.23 \text { with Excel® })
\end{aligned}
$$

$$
\begin{aligned}
E U A C_{3}(15 \%) & =\$ 28,000(A / P 15 \%, 5)+\$ 500+\$ 500(A / G 15 \%, 5) \\
& =\$ 28,000(0.29832)+\$ 500+\$ 500(1.72281) \\
& =\$ 7,786.21 / \mathrm{yr}(\$ 7,786.14 \text { with Excel® })
\end{aligned}
$$

$E U A C_{4}(15 \%)=\$ 7,500(F / P 15 \%, 1)+\$ 800(A / G 15 \%, 5)-\$ 9,000(A / P 15 \%, 5)$

$$
=\$ 7,500(1.15000)+\$ 800(1.72281)-\$ 9,000(0.29832)
$$

$$
=\$ 7,318.37 / y r(\$ 7,318.41 \text { with Excel } ® \text { ) }
$$

Lease a New Filter Press!

# Opportunity Cost Approach 

## Before-Tax Analysis

## Opportunity Cost Approach

The opportunity cost approach views the transaction from the perspective of an "outsider" who does not own the existing asset. The outsider considers the salvage value of the existing asset to be its investment cost if it is retained in service. (Recall our opportunity cost discussion.)

The analogy of an outsider purchasing the defender on a used equipment market is likely to break down with respect to assumptions made regarding the planning horizon, depreciation allowances, and income tax rate used.

If an outsider purchases the defender, is it reasonable to assume that the same planning horizon will be used? Likewise, is it reasonable to assume the new owner will use the depreciation allowances available to the previous owner, instead of starting a new and taking full depreciation allowances for the equipment? Finally, is it reasonable to assume that the new owner's tax bracket is the same as that of the previous owner? For these reasons, we prefer to call this approach the opportunity cost approach.

## Example 11.9

A surface mount placement machine was acquired 10 years ago for $\$ 300,000$. It can be kept for a maximum of 5 more years, at which time it will have a negligible salvage value. Annual O\&M costs for the defender have been increasing by $\$ 5,000$ a year since its acquisition. Next year, the O\&M costs will total \$120,000.

A new SMP machine (challenger) is being considered as a replacement for the defender, which has a current market value of $\$ 50,000$. The challenger will cost $\$ 500,000$ and have annual $0 \& M$ costs of $\$ 10,000$ the first year, increasing by \$5,000 a year.

Based on the remaining useful life of the defender, a 5-year planning horizon is used. After 5 years, the challenger will have a market value of $\$ 200,000$. With a BTMARR of $16.67 \%$, using an opportunity cost approach, should the defender be replaced?

## Solution to Example 11.9

Based on the incremental cash flows shown below and an EUAC analysis, the old SMP machine (defender) should be retained.

| EOY | $\mathbf{C F}(\mathbf{1})$ | $\mathbf{C F}(\mathbf{2})$ | $\mathbf{C F}(\mathbf{2}) \mathbf{- C F}(\mathbf{1})$ |
| :---: | ---: | ---: | ---: |
| 0 | $-\$ 50,000.00$ | $-\$ 500,000.00$ | $-\$ 450,000.00$ |
| 1 | $-\$ 120,000.00$ | $-\$ 10,000.00$ | $\$ 110,000.00$ |
| 2 | $-\$ 125,000.00$ | $-\$ 15,000.00$ | $\$ 110,000.00$ |
| 3 | $-\$ 130,000.00$ | $-\$ 20,000.00$ | $\$ 110,000.00$ |
| 4 | $-\$ 135,000.00$ | $-\$ 25,000.00$ | $\$ 110,000.00$ |
| 5 | $-\$ 140,000.00$ | $\$ 170,000.00$ | $\$ 310,000.00$ |

$E U A C_{2-1}(16.67 \%)=\$ 450,000(A / P 16.67 \%, 5)$

- \$200,000(A/F 16.67\%,5) - \$110,000
$=\$ 890.00>\$ 0^{*}$
=PMT(16.67\%,5,-450000,200000)-110000
= \$889.06
*CF(2) - CF(1) identical to cash flow approach


## Solution to Example 11.9

Based on the incremental cash flows shown below and an EUAC analysis, the old SMP machine (defender) should be retained.
$1-\$ 120.000 .00-\$ 10.000 .00$ \$110.000.00
Since $E U A C_{2-1}(16.67 \%)>\$ 0$,
Do Not Replace!
$E U A C_{2-1}(16.67 \%)=\$ 450,000(A / P 16.67 \%, 5)$

- \$200,000(A/F 16.67\%,5) - \$110,000
$=\$ 890.00>\$ 0^{*}$
=PMT(16.67\%,5,-450000,200000)-110000
= \$889.06
* CF(2) - CF(1) identical to cash flow approach


## Example 11.10

A filter press was purchased 3 yrs ago for $\$ 30,000$. O\&M costs are expected to be $\$ 7,000$ next year if the filter press is kept; they will increase by $\$ 1,000$ per year. In 5 yrs, the filter press can be sold for $\$ 2,000$. Its book value is $\$ 12,600$.
A new press can be purchased for $\$ 36,000$. If purchased, the old filter press can be sold for $\$ 9,000$. O\& M costs will follow a $\$ 1,000$ gradient series, with no cost in the first year. At the end of 5 yrs, the new press will have a $\$ 12,000$ salvage value.

With a 15\% BTMARR, using an opportunity cost approach, what should be done?

## Solution to Example 11.10

Given the incremental cash flows shown below, based on an EUAC analysis, the old filter press should be replaced.

$$
\begin{aligned}
E U A C_{2-1}(15 \%) & =\$ 27,000(A / P 15 \%, 5)-\$ 17,000(A / F 15 \%, 5)-\$ 7000 \\
& =\$ 27,000(0.29832)-\$ 10,000(0.14832)-\$ 7000 \\
& =-\$ 428.56 / \mathrm{yr}<\$ 0 \\
& =\operatorname{PMT}(15 \%, 5,-27000,17000)-7000 \\
& =-\$ 428.64 / \mathrm{yr}<\$ 0
\end{aligned}
$$

The challenger is preferred; replace the old filter press.

| EOY | CF(1) | CF(2) | CF(2) - CF(1) |
| :---: | :---: | ---: | ---: |
| 0 | $-\$ 9,000.00$ | $-\$ 36,000.00$ | $-\$ 27,000.00$ |
| 1 | $-\$ 7,000.00$ | $\$ 0.00$ | $\$ 7,000.00$ |
| 2 | $-\$ 8,000.00$ | $-\$ 1,000.00$ | $\$ 7,000.00$ |
| 3 | $-\$ 9,000.00$ | $-\$ 2,000.00$ | $\$ 7,000.00$ |
| 4 | $-\$ 10,000.00$ | $-\$ 3,000.00$ | $\$ 7,000.00$ |
| 5 | $-\$ 9,000.00$ | $\$ 8,000.00$ | $\$ 17,000.00$ |

## Alternate Solution to Example 11.10

Alternative 1: keep the old press
EUAC $_{1}(15 \%)=\$ 9,000$ (A|P 15\%,5) $+\$ 7,000$ + \$1,000(A|G 15\%,5) - \$2,000 (A|F 15\%,5)
EUAC $_{1}(15 \%)=\$ 9,000(0.29832)+\$ 7,000+\$ 1,000(1.72281)$ - \$2,000(0.14832)

EUAC $_{1}(15 \%)=\$ 11,111.05 / \mathrm{yr}$
Alternative 2: replace the old press
EUAC $_{2}(15 \%)=\$ 36,000$ (A|P 15\%,5) $+\mathbf{\$ 1 , 0 0 0 ( A | G 1 5 \% , 5 )}$ - \$12,000(A|F 15\%,5)
$\mathrm{EUAC}_{2}(15 \%)=\$ 36,000(0.29832)+\$ 1,000(1.72281)$

- \$12,000(0.14832)
$\operatorname{EUAC}_{2}(15 \%)=\$ 10,682.49 / \mathrm{yr}$


## Example 11.11

In Example 11.10, suppose the equipment supplier offers a $\$ 10,000$ trade-in for the old press (CF2). Also, suppose two new alternatives are considered: a $\$ 40,000$ filter press having a $\$ 13,000$ salvage value in 5 yrs, O\&M equal to a $\$ 500$ gradient series on a $\$ 500$ base, and a $\$ 12,000$ trade-in for the old press (CF3); and a leased press, with \$7,500 beginning-of-year lease costs and end-of-year O\%M cost given by an $\$ 800$ gradient series. If leasing is pursued, the old press will be sold for \$9,000.

| EOY | CF(1) | CF(2) | CF(3) | CF(4) |
| :---: | ---: | ---: | ---: | :---: |
| 0 | $-\$ 9,000.00$ | $-\$ 35,000.00$ | $-\$ 37,000.00$ | $-\$ 7,500.00$ |
| 1 | $-\$ 7,000.00$ | $\$ 0.00$ | $-\$ 500.00$ | $-\$ 7,500.00$ |
| 2 | $-\$ 8,000.00$ | $-\$ 1,000.00$ | $-\$ 1,000.00$ | $-\$ 8,300.00$ |
| 3 | $-\$ 9,000.00$ | $-\$ 2,000.00$ | $-\$ 1,500.00$ | $-\$ 9,100.00$ |
| 4 | $-\$ 10,000.00$ | $-\$ 3,000.00$ | $-\$ 2,000.00$ | $-\$ 9,900.00$ |
| 5 | $-\$ 9,000.00$ | $\$ 8,000.00$ | $\$ 10,500.00$ | $-\$ 3,200.00$ |

## Solution to Example 11.11

$E U A C_{1}(15 \%)=\$ 9,000(A \mid P 15 \%, 5)+\$ 7,000+\$ 1,000(A / G 15 \%, 5)$

- \$2,000(A/F 15\%,5)
$=\$ 9,000(0.29832)+\$ 7,000+\$ 1,000(1.72281)-\$ 2,000(0.14832)$
= \$11,111.05/yr (\$11,111.02 with Excel)

$$
\begin{aligned}
E U A C_{2}(15 \%) & =\$ 35,000(A / P 15 \%, 5)+\$ 1,000(A / G 15 \%, 5)-\$ 12,000(A / F 15 \%, 5) \\
& =\$ 35,000(0.29832)+\$ 1,000(1.72281)-\$ 12,000(0.14832) \\
& =\$ 10,384.17 / \mathrm{yr}(\$ 10,384.07 \text { with Excel })
\end{aligned}
$$

$$
\begin{aligned}
E U A C_{3}(15 \%) & =\$ 37,000(A / P 15 \%, 5)+\$ 500+\$ 500(A / G 15 \%, 5) \\
& =\$ 37,000(0.29832)+\$ 500+\$ 500(1.72281) \\
& =\$ 10,471.09 / \mathrm{yr}(\$ 10,470.98 \text { with Excel })
\end{aligned}
$$

$$
\begin{aligned}
E U A C_{4}(15 \%)= & \$ 7,500(F / P 15 \%, 1)+\$ 800(A / G 15 \%, 5) \\
= & \$ 7,500(1.15000)+\$ 800(1.72281) \\
= & \$ 10,003.25 / \mathrm{yr}(\$ 10,003.25 \text { with Excel) } \\
& \text { Lease a New Filter Press! }
\end{aligned}
$$

## Pit Stop \#11—Pick Up the Pace! Don’t Get Replaced!

1. True or False: In performing engineering economic analyses of replacement alternatives, it is best to perform before-tax analyses, since incorporating income tax considerations in the analysis is difficult, due to the treatment of trade-in values not equaling book values.
2. True or False: The two approaches used in performing replacement analyses are the cash flow approach and the insider approach.
3. True or False: In determining the optimum replacement interval, it is necessary to assume negligible salvage values.
4. True or False: Before-tax replacement analyses and after-tax replacement analyses seldom yield the same recommendation.
5. True or False: Section 1031 exchanges of property can be performed for any real or personal property.
6. True or False: If the optimum replacement interval for an over-the-road tractor is $\mathbf{4}$ years and the initial cost of the tractor is increased by $20 \%$ then the optimum replacement interval for the next tractor might be less than 4 years.
7. True or False: If the optimum replacement interval for an over-the-road tractor is 4 years and the salvage value for used tractors is suddenly cut in half, then the optimum replacement interval for the next tractor might be greater than 4 years.
8. True or False: If the optimum replacement interval for an over-the-road tractor is 4 years and the ATMARR is increased from $9 \%$ to $12 \%$, then the optimum replacement interval for the next tractor might be less than 4 years.
9. True or False: If the optimum replacement interval for an over-the-road tractor is 4 years and the rate of increase in O\&M costs doubles, then the optimum replacement interval for the next tractor might be less than 4 years.
10. True or False: Section 1031 Property Exchanges are no longer permitted by the U.S. Internal Revenue Service.

## Pit Stop \#11—Pick Up the Pace! Don’t Get Replaced!

1. True or False: In performing engineering economic analyses of replacement alternatives, it is best to perform before-tax analyses, since incorporating income tax considerations in the analysis is difficult, due to the treatment of trade-in values not equaling book values. False
2. True or False: The two approaches used in performing replacement analyses are the cash flow approach and the insider approach. False
3. True or False: In determining the optimum replacement interval, it is necessary to assume negligible salvage values. False
4. True or False: Before-tax replacement analyses and after-tax replacement analyses seldom yield the same recommendation. False
5. True or False: Section 1031 exchanges of property can be performed for any real or personal property. False
6. True or False: If the optimum replacement interval for an over-the-road tractor is 4 years and the initial cost of the tractor is increased by $20 \%$ then the optimum replacement interval for the next tractor might be less than 4 years. False
7. True or False: If the optimum replacement interval for an over-the-road tractor is 4 years and the salvage value for used tractors is suddenly cut in half, then the optimum replacement interval for the next tractor might be greater than 4 years. True
8. True or False: If the optimum replacement interval for an over-the-road tractor is 4 years and the ATMARR is increased from $9 \%$ to $12 \%$, then the optimum replacement interval for the next tractor might be less than 4 years. False
9. True or False: If the optimum replacement interval for an over-the-road tractor is 4 years and the rate of increase in O\&M costs doubles, then the optimum replacement interval for the next tractor might be less than 4 years. True
10. True or False: Section 1031 Property Exchanges are no longer permitted by the U.S. Internal Revenue Service. False
