



Q1] p-type silicon of $L = 20 \mu m$

doping decreased from 10^{17} at $x=0$
to 10^{15} at $x=L$

$$N_p = 500 \text{ cm}^2/\text{V}\cdot\text{s}$$

what is diffusion
current density?

* diffusion current direction = with holes
* drift " " = " E

$$J = (+) q D_p \frac{dp}{dx}$$

$$\frac{D_p}{N_p} = V_T \Rightarrow V_T = \frac{kT}{q}$$

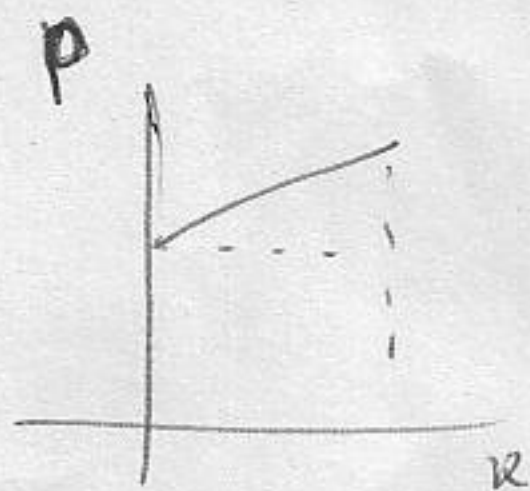
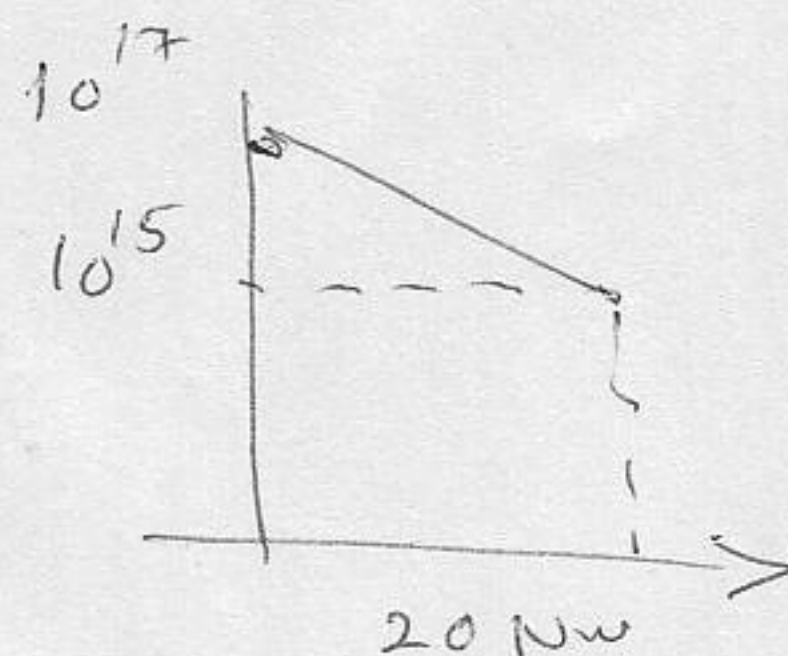
$$V_T = \frac{8.62 \times 10^{-5} \times 300}{1} = 0.025 \text{ V} \quad V_T \text{ for silicon at room temp}$$

$$\Rightarrow D_p = N_p \times V_T = 500 \times 0.025 = 12.5 \text{ cm}^2/\text{s}$$

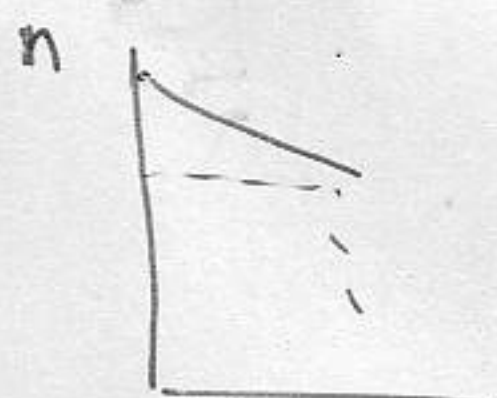
$$J_p = (+) 1.6 \times 10^{-19} \times 12.5 \times \left| \frac{10^{17} - 10^{15}}{20 \mu m} \right|$$

$\hookrightarrow 20 \mu m = 20 \times 10^{-6} = 20 \times 10^{-4} \text{ cm}$

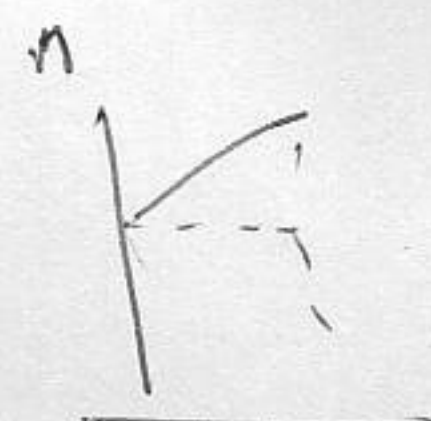
$$\approx 199 \text{ A/cm}^2$$



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what is I_{drift} ? $\Rightarrow I_{diffusion}$
in open cct.

3.110 Find the current flow in a silicon bar of $10\text{-}\mu\text{m}$ length having a $5\text{-}\mu\text{m} \times 4\text{-}\mu\text{m}$ cross-section and having free-electron and hole densities of $10^5/\text{cm}^3$ and $10^{15}/\text{cm}^3$, respectively, with 1 V applied end-to-end. Use $\mu_n = 1200\text{ cm}^2/\text{V}\cdot\text{s}$ and $\mu_p = 500\text{ cm}^2/\text{V}\cdot\text{s}$.

3.110

$$10\mu\text{m} = 10 \times 10^{-6} = 10^{-3}\text{ cm}$$

$$5\mu\text{m} \times 4\mu\text{m} = 5 \times 10^{-4} \times 4 \times 10^{-4} = 5 \times 4 \times 10^{-8}$$

$$J_{\text{drift}} = q (n \mu_n + p \mu_p) E \quad \text{A/cm}^2$$

$$I_{\text{drift}} = q (n \mu_n + p \mu_p) E \cdot A$$

$$= 1.6 \times 10^{-19} (10^5 \cdot 1200 + 10^{15} \cdot 500) \times$$

$$\frac{1}{10^{-3}} \times (5 \times 4 \times 10^{-8})$$

$$16 \mu\text{A}$$

$$= \underline{\underline{16 \mu\text{A}}}$$

look at Exercise 3.32, 3.33, Problem 3.114
Problem 3.115

PN Junction, $N_A = 10^{17}/\text{cm}^3$, $N_D = 10^{16}/\text{cm}^3$, $T = 300\text{K}$

① ~~V_0~~ $V_0 = ?!$, $x_p = ?$, $x_n = ?$

② if Area is 100nm^2 , what is the charge stored in each side?

③ find C_{j0} and C_j if $m = 1/2$

④ if a reverse bias voltage of 2V was applied, repeat 1, 2, 3

① $V_T \big|_{300\text{K}} = 0.025$ صباحه وادى

$$V_0 = V_T \ln \left(\frac{N_A N_D}{n_i^2} \right) = 0.025 \times \ln \left(\frac{10^{17} \times 10^{16}}{(1.5 \times 10^{10})^2} \right)$$

300K
 $n_i = 1.5 \times 10^{10}$

$$= 0.728\text{mV} \approx 0.73\text{mV}$$

$$W = \sqrt{\frac{2\epsilon_s}{q} \left(\frac{1}{N_A} + \frac{1}{N_D} \right) (V_0 + V_R)}$$

$(\text{cm}) \quad 1 \times 10^{-12}$

$$= \sqrt{\frac{2 \times 11.7 \times 8.85 \times 10^{-14}}{1.6 \times 10^{-19}} \left(\frac{1}{10^{17}} + \frac{1}{10^{16}} \right) (728\text{mV})}$$

$$= \sqrt{1.00 \times 10^{-9}} = 31.6 \times 10^{-6} \text{cm}$$

$\text{cm} \quad \text{الطول بوحدة}$

$$\Rightarrow x_n N_D = x_p N_A, \quad w = x_n + x_p \Rightarrow x_p = 31.6 \times 10^{-6} - x_n$$

$$x_n = \frac{10^{17}}{10^{16}} (31.6 \times 10^{-6} - x_n) \Rightarrow x_n + \frac{10^{17}}{10^{16}} x_n = \frac{10^{17}}{10^{16}} (31.6 \times 10^{-6})$$

$$x_n = 28.7 \times 10^{-6} \text{cm}$$

$$x_p = w - x_n = 31.6 \times 10^{-6} - 28.7 \times 10^{-6} = 2.87 \times 10^{-6} \text{cm}$$

كعب الخردال الـ Cm

② Charge in each side

$$A = 100 \text{ Nm}^2 = 100 \times 10^{-8} \text{ Cm}^2$$

* n-side

$$\begin{aligned} \text{Volume} &= A \times x_n = 100 \text{ Nm}^2 \times 28.7 \times 10^{-8} \text{ m} \\ &= 100 \times 10^{-8} \text{ Cm}^2 \times 28.7 \times 10^{-6} \text{ Cm} \\ &\approx 28.7 \times 10^{-12} \text{ Cm}^3 \end{aligned}$$

$$\text{Charge} = N_D \times \text{Volume}$$

$$\text{Charge} = 10^{16} \times 28.7 \times 10^{-12} = 28.7 \times 10^4 \text{ Coulomb}$$

* P-side ;

$$\begin{aligned} \text{Volume} &= 100 \times 10^{-8} \text{ Cm}^2 \times 2.87 \times 10^{-6} \text{ Cm} \\ &= 2.87 \times 10^{-12} \text{ Cm}^3 \end{aligned}$$

$$\begin{aligned} \text{Charge} &= N_A \times \text{Volume} = 10^{17} \times 2.87 \times 10^{-12} = 2.87 \times 10^5 \text{ Coulomb} \\ &= 28.7 \times 10^4 \text{ C} = \text{n-side} \end{aligned}$$

$\Rightarrow$ n-side = p-side for open c.c.

$$\textcircled{3} C_{j0} = \frac{\epsilon_s A}{W_{\text{dep}}} = \frac{11.7 \times 8.8 \times 10^{-14} \times 1 \text{ Cm}^2}{31.6 \times 10^{-6}} = 32.58 \text{ nF}$$

$$C_j = C_{j0} \Big|_{V=0} = 32.58 \text{ nF/Cm}^2$$

Per unit area $A = 1 \text{ Cm}^2$

$$C_{j0 \text{ total}} = 32.58 \text{ nF} \times (100 \times 10^{-8}) = 32.58 \text{ fF}$$

④ (i) $V_0 = 728 \text{ mV}$

$$W = \sqrt{\frac{2\epsilon_s}{q} \left(\frac{1}{N_A} + \frac{1}{N_D} \right) (V_0 + V_R)^{2V}} = \sqrt{1.41 \times 10^9 (728 \text{ mV} + 2)}$$

$$= \sqrt{3.86 \times 10^9} = 62.1 \times 10^6 \text{ cm}$$

$\kappa_n N_D = \kappa_p N_A \Rightarrow W = \kappa_p + \kappa_n$

$\Rightarrow \kappa_p = 62.1 \times 10^6 \text{ cm} - \kappa_n$

$\kappa_n = \frac{\frac{N_A}{10^{17}}}{\frac{N_D}{10^{16}}} \left[62.1 \times 10^6 - \kappa_n \right] \Rightarrow 11 \kappa_n = 6.21 \times 10^5$

$\boxed{\kappa_n = 5.64 \times 10^6 \text{ cm}}$

$\kappa_p = 62.1 \times 10^6 - 5.64 \times 10^6 = \boxed{0.57 \times 10^6 \text{ cm}}$

(ii) Charge = $N \times \text{Volume}$ - $A = 100 \text{ cm}^2 = 1 \text{ cm}^2$

$V_n = 100 \times 10^{-8} \times 5.64 \times 10^6 \text{ cm} = 5.64 \times 10^{-12} \text{ cm}^3$

$V_p = 100 \times 10^{-8} \times 0.57 \times 10^6 = 0.57 \times 10^{-12} \text{ cm}^3$

$C_n = 10^{16} \times 5.64 \times 10^{-12} = 5.64 \times 10^4 \text{ Coulomb}$

$C_p = 10^{17} \times 0.57 \times 10^{-12} = 0.57 \times 10^4 \text{ Coulomb}$
 $= 5.7 \times 10^3 \text{ Coulomb} = n\text{-side.}$

$C_n = C_p$

(iii) $C_j = \frac{C_{j0}}{\left(1 + \frac{V_R}{V_0}\right)^m} = \frac{32.58 \text{ nF/cm}^2}{\sqrt{1 + \frac{2}{0.728}}} = 16.83 \text{ nF/cm}^2$

$\downarrow$
 0.5
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