# Regulation, Free-Riding Incentives, and Investment in R&D with Spillovers

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## Introduction

Firms' investment in clean (or environmentally friendly) research and development (R&D) has increased over time, from less than \$30 billion in 2005 to \$159 billion in 2012 worldwide.

National Science Foundation's Science and Engineer in Indicators(2014), Chapter 6 (https://www.nsf.gov/statistics/seind14/index.cfm/chapter-6).

- Katsoulacos and Xepapadeas (1996); Montero (2002a); Comin (2004); Poyago-Theotoky (2007); While Espinola-Arredondo (2016).
- The aforementioned literature assumes that all firms are subject to uniform environmental policies. However, when firms are asymmetric, they may invest different amounts in clean R&D, generating a distinct amount of pollution.
- This asymmetry calls for a type-dependent environmental policy that takes into account the different marginal environmental damage each firm generates (firstbest policy), whereas a uniform regulation, that sets the same emission fee to all firms, represents a second-best policy in this context.

### **Contribution:**

Two regulatory regimes and focuses on settings where the regulator can accurately observe each firm's pollution before choosing emission fees (point pollution) or, alternatively, contexts in which R&D is observable thus helping the regulator infer the reduction in pollution.

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## 2 Model

Consider a duopoly market similar to Poyago-Theotoky (2007) where: (3 stages)

1<sup>st</sup> stage, every firm i independently and simultaneously chooses its investment in R&D,  $z_i$ .

2<sup>nd</sup> stage, the regulator selects an emission fee t by maximizing social welfare.

 $3^{rd}$  stage, every firm i competes `a la Cournot choosing its output level  $q_i$ .

For generality, firms can be symmetric in their R&D abilities, if  $\gamma_i = \gamma_j$ , or asymmetric, if  $\gamma_i \neq \gamma_j$ , where the latter can occur when one of the two firms has a previous history of innovation in the market.

Firms face linear demand

p(Q) = a - Q where *p* is price, a > 0, and  $Q \equiv q_i + q_j$  is the aggregate output level.

Both firms have the same marginal cost of production c, where a > c > 0.

Two forms of emission fees: uniform, where both firms are subject to the same fee *t*; and type dependent, whereby each firm is subject to a distinct fee  $t_i$ , which might affect firms' incentives to invest in R&D

In order to sustain type-dependent fees, we consider that environmental damage is  $ED = \frac{1}{2} d(e_i^2 + e_j^2)$ , where d > 1.

## **3 Equilibrium Analysis**

### 1. Third Stage

Solving by backward induction, we first analyze optimal output under both policy regimes in the third stage of the game. Therefore, every firm solves:

$$\max \pi_i = (a - q_i - q_j)q_i - cq_i - t(q_i - z_i - \beta z_j),$$

where  $t = t_i$  when the fee is type-dependent, and  $\beta \in [0, 1]$  represents the knowledge spillover from firm j to i. Hence, when  $\beta = 0$  spillover effects are absent, whereas when  $0 < \beta \le 1$  firm i benefits from every unit of investment in R&D by firm j (either fully, if  $\beta = 1$ , or partially, if  $0 < \beta < 1$ ).

**Lemma 1.** In the third stage, every firm *i* chooses output according to

$$q(t_i, t_j) = \frac{a - c - 2ti + t_j}{3}$$

under a type-dependent fee, and  $q(t) = \frac{a-c-t}{3}$  under a uniform fee.

Hence, when the emission fee is uniform, a reduction in t benefits both firms. However, when the fee is type-dependent, a reduction on firm i's tax is completely appropriated by this firm (which regulator sets emission fees, and immediately after firms compete in quantities. increases its output level) but harms its rival, decreasing its production.

#### 3.2 Second Stage

The following lemma examines optimal fees under uniform regulation in the second stage of the game. In this case, the regulator solves:

$$\max SW_t = CS + PS + T - ED \tag{1}$$

where *CS* and *PS* represent consumer and producer surplus, respectively, and *T* denotes total tax revenue. A similar problem applies when regulation is type-dependent, and thus the regulator can set a pair of fees ( $t_i$ ,  $t_j$ ).

**Lemma 2.** In the second stage, under a uniform regulation, the regulator sets an emission fee

$$t(z_i, z_j) = \frac{2(a-c)(d-1) - 3d(1+\beta)(z_i + z_j)}{2(d+2)},$$
  
and in the case of type-dependent regulation, a fee of  
$$t_i(z_i, z_j) = \frac{(a-c)(d-1) - z_i[1+2d+\beta(d-1)] - z_j[d-1+\beta(2d+1)]}{d+2}$$

for every firm i.

of

While an increase in either firm's investment in R&D produces a symmetric reduction in the uniform emission fee  $t(z_i, z_j)$ , such effect is asymmetric when firms face type-dependent regulation,  $t_i(z_i, z_j)$ .

spillovers are absent,  $\beta = 0$ , firm *i*'s investment in R&D decreases its emission fee  $t_i(z_i, z_j)$ . Similarly, an increase in its rival's investment in R&D,  $z_j$ , also decreases firm *i*'s emission fee  $t_i$ .

When spillovers are present,  $\beta > 0$ , similar effects arise, but an increase in firm *j*'s investment now facilitates firm *i*'s pollution abatement, producing a larger decrease in the optimal emission fee  $t_i$  than when spillover effects are absent.

Free-ride off each other's investment in R&D as the spillover effect increases.

## 3.3 First Stage

We next analyze optimal investment in R&D in the first stage of the game under uniform regulation, and afterwards under type-dependent policy. In the case of uniform fees, every firm *i* solves

$$\max \pi_i \stackrel{z_{\perp}}{=} [a - q_i(t(z_i, z_j)) - q_j(t(z_i, z_j))] q_i(t(z_i, z_j)) - cq_i(t(z_i, z_j)) - t[q_i(t(z_i, z_j)) - z_i - \beta z_j] - \frac{1}{2} \gamma_i z_i. \quad (2)$$

which includes total revenue, production cost, tax payments which depend on net emissions,  $q_i(t(z_i, z_j)) - z_i - \beta z_j$ , and the cost of investing in R&D.

**Proposition 1.** In the first stage, every firm i chooses an R&D investment level of

$$Z_i^U = \frac{2(a-c)(d(\beta+d+2)-2)(3(\beta^2-1)d-C_j)}{A[3d(\beta^2-1)(6(\beta+3)+(\beta+7)d)+BC_i+C_j(AB-C_i(d+2))]}$$
(3)

where U denotes uniform fee,  $A \equiv (\beta + 1)d$ ,  $B \equiv (\beta - 5)d - 12$ , and  $C_i \equiv 2\gamma_i(d + 2)$ . In addition,  $z^U$  decreases in  $\gamma_i$  but increases in  $\gamma_i$ .

Hence, firm *i* invests less in R&D as the cost of investing increases (larger  $\gamma_i$ ), but invests more as the cost of its rival increases. This is because  $z_i$  and  $z_j$  are strategic substitutes, implying that an increase in  $\gamma_j$  shifts firm *j*'s best response function downwards, thus reducing  $z_j$ , which ultimately increases  $z_i$  since best response functions are negatively sloped. In addition, when firm *i* is the more efficient firm,  $\gamma_i < \gamma_j$ , the aggregate investment in R&D,  $z_i^U + z^U$ , increases in firm *i*'s efficiency (lower  $\gamma_i$ ) but decreases on the competitor's efficiency level. **Proposition 2.** In the first stage, every firm i chooses an R&D investment level of

$$z_i^{TD} = \frac{(a-c)(d(d+3)-2\beta)(E-\frac{C_i}{2})}{(\beta+1)[Ed((\beta+3)(d+3)-2(\beta-1))-DC_i]-DC_j(\beta+1)-(2+d)^3\gamma_i\gamma_j}$$
(4)

where  $D \equiv (1-\beta + d(d+3))$ ,  $E \equiv (\beta^2 - 1)(d+1)$ , and TD denotes type-dependent fee. In addition,  $z^{TD}$  decreases in  $\gamma_i$  but increases in  $\gamma_j$ .

We next analyze aggregate investment in R&D, and how it is affected by the asymmetry in investment efficiency.

**Corollary 1.** Consider that  $\gamma_i < \gamma_j$ . A symmetric marginal improvement in efficiency produces

 $\frac{\partial z_i^K}{\partial \gamma_i} > \frac{\partial z_j^K}{\partial \gamma_j} \text{ in individual investments, and } \frac{\partial (z_i^K + z_j^K)}{\partial \gamma_i} > \frac{\partial (z_i^K + z_j^K)}{\partial \gamma_j} \text{ in aggregate investment for every policy regime } K = \{TD, U\}, \text{ where } \frac{\partial (z_i + z_j)}{\partial \gamma_i} < 0 \text{ for every firm } i.$ 

If firm *i* is the most efficient ( $\gamma_i < \gamma_j$ ), a symmetric improvement in efficiency produces a larger increase in investment in R&D from firm *i* than from *j*.

## 4 Comparison

We next compare equilibrium investment levels under uniform and type-dependent regulation.

**Corollary 2.** Every firm i's best response function in the investment stage under a type- dependent fee lies above the best response function under a uniform fee for all  $z_j$  and all parameter values. In addition, equilibrium investment in R&D satisfies  $z_i^{TD} > z_j^U$  for all parameter values.

Intuitively, when firm i invests an additional unit in R&D under type-dependent regulation, it reduces its future emission fee more significantly than when facing uniform regulation. As a consequence, firms have more incentives to invest in R&D.



Figure 1: Difference between the uniform and typedependent fees as a function of firm *i*'s efficiency. **Profits** Figures 2 and 3 show the profit difference across regimes,  $\pi^U - \pi^{TD}$ , for every firm *i*, as a function of its own efficiency,  $\gamma_i$ , when the efficiency of its rival is held constant at  $\gamma_j = 2/3$ .







Figure 5: Social welfare difference between the two regulation types for different spillovers.



Figure 6: Social welfare difference between the two regulation types for different environmental damages.

#### **Environmental Research Cartel (ERC).**

In order to evaluate the free-riding effect of in vestment in R&D, we need to evaluate the investment decision if the firms were to collude in the first stage. This will give us the joint profit maximizing amount of investment in R&D. This case, known as an environmental research cartel (ERC) in Poyago-Theotoky (2007), uses the second and third stage decisions from lemmas 1 and 2, but firms maximize joint profits by solving:

 $\max \pi_i + \pi_j$ .

The objective function of this joint maximization problem is the same under both policy regimes. This means that, under each regime, when firms are engaged in an ERC, each firm faces the same emission fee.

**Proposition 3.** The equilibrium level of investment in R&D for every firm i when firms engage in an environmental research cartel is



$$z_i^{ERC} = \frac{(\beta+1)\gamma_j \, [d(d+3)-2](a-c)}{\gamma_j \, [2(\beta+1)^2 d(d+3)+\gamma_i (d+2)^2]+2(\beta+1)^2 \gamma_i d(d+3)}.$$



Figure 7: Investment in R&D as a function of the spillover under the two regimes and the ERC.



Figure 8: The total level of investment in R&D as a function of the spillover under the two regimes and the ERC.

#### 5 Discussion

#### When is type-dependent regulation critical.

Our results show that when spillovers are small, such as when firms are located far apart or operate in different industries, regulators should pay close attention to the difference in each firm's pollution when designing environmental policy. Doing so induces firms to increase their investment in R&D, reducing pollution, and thus helping regulators more easily reach their environmental targets. In contrast, when spillover effects are significant, such as in industry clusters, the use of either policy regime does not entail substantial differences in investment levels. Since the uniform regime is easier to implement, our findings imply that the regulator can rely on this policy tool to achieve similar welfare levels.

#### Efficiency and type-dependent policies.

We find that firms exhibiting efficiency in R&D investment would gain from a change in policy regime. In particular, a move from uniform to type-dependent fees increases the efficient firm's profits, appropriating a larger proportion of their investment, while it reduces the profits of inefficient firms who would favor uniform policies. Hence, regulators should expect efficient firms aggressively lobbying for fine-tuned regulation that takes into account each firm's characteristics, whereas inefficient firms would favor uniform standards across the industry.

#### Preference alignment.

When firms are efficient at investing in R&D, they would favor type- dependent policies, as described above. Similarly, regulators would like to introduce this policy as it yields a large reduction in pollution, and thus an increase in welfare, relative to uniform fees. Therefore, both regulator and firm would favor a similar policy regime, thus facilitating the introduction of more fine-tuned policies. However, when firms are inefficient, they prefer a uniform policy, while regulators still find welfare gains from introducing type-dependent fees. In this case, the preferences of firms and regulator become misaligned over policy.

#### Further Research.

Our model can be extended along different dimensions. First, we consider that R&D investment is deterministic, but a different setting could assume that firm i's investment  $z_i$  is succesful with a positive probability, affecting the difference in emission fees across policy regimes. Second, we consider that every firm benefits from its own R&D investment, and a share of its rival's (spillover effect). However, abatement patents could follow an R&D tournament structure, as in Lazear and Rosen (1981) and Nalebluff and Stiglitz (1983). In this setting, every firm would only benefit from either its own R&D investment (if it wins the tournament) or from a share of its rival's (if it loses), rather than from both. In these two extensions, R&D expenditure can differ from R&D outcomes, implying that taxing outcomes can induce firms to invest suboptimal amounts in R&D. In this context, it would be interesting to analyze whether this inefficiency is, as in our model, larger when the regulator uses uniform rather than type-dependent policies.

