

Q1)

```
install.packages("readxl")
```

```
library(readxl)
```

```
d<- read_excel("C:/Users/ch4ex1.xlsx")
```

```
d
```

```
i=d$i
```

```
i
```

```
y=d$y
```

```
y
```

```
#Plot the number of cases y against time period i ( i= 1,...,20)
```

```
plot(i,y,pch=16)
```

```
# plot logi against logy
```

```
plot(log(i),log(y))
```

```
# Fit the model
```

```
model<-glm(y~log(i),family=poisson(link="log"),data=d)
```

```
summary(model)
```

```
# an approximate 95% confidence interval for beta1 and beta 2
```

```
CI_of_beta <- confint.default(model,level=0.95)
```

```
CI_of_beta
```

```
# The variance-covariance matrix of the MLE
```

```
Tauinver<-vcov(model)
```

```
Tauinver
```

```
# use the iterative formula to fit model
```

```
# Initial values b0
```

```
beta<-c(1,1)
```

```
beta
```

```
#Design matrix (X)
```

```
X=matrix(c(rep(1,20),log(i)),nrow=20,ncol = 2,byrow = F)
```

```
X
```

```
#Transform Design matrix (Xt)
```

```
Xt<-t(X)
```

```
Xt
```

```
#Working weights matrix (W )
```

```
W<-exp(beta[1])*diag(c(i^beta[2]),nrow = 20,ncol = 20)
```

```
W
```

```
#Information matrix, Tau= Xt*W*X
```

```
# Multiply the matrices.
```

```
tau<- Xt%*%W%*%X
```

```
tau
```

#The score statistics are: (U1 and U2)

```
U1<-sum(y-exp(beta[1]+beta[2]*log(i)))
```

```
U2<-sum(y*log(i)-log(i)*exp(beta[1]+beta[2]*log(i)))
```

#The vector of scores (U)

```
U<-matrix(c(U1,U2))
```

U

##iterative equation to find an approximate estimate of beta: b1, b2

```
b<-beta+solve(tau)%*%U
```

b

Q2)

#Design matrix (X) :

```
X=matrix(c(rep(1,17),xi),nrow=17,ncol = 2,byrow = F)
```

X

#Transpose of design matrix :

```
Xt<-t(X)
```

Xt

#The matrix of working weights (W) is :

```
W<-diag(c(rep(1,17)),nrow = 17,ncol = 17)
```

W

##Information matrix, $\text{Tau} = X^t * W * X$ (Multiply the matrices):

```
tau<- Xt%%W%%X
```

tau

#The score statistics are: (U1 and U2

```
U1<-sum(-1+(yi/exp(beta[1]+beta[2]*xi)))
```

```
U2<-sum(-xi+(yi*xi/exp(beta[1]+beta[2]*xi)))
```

```
U<-matrix(c(U1,U2))
```

U

#We make the following Calculation: (to compute b

```
b<-beta+solve(tau)%%U
```

b

#Fit the model described in (c) using statistical software

```
model<-glm(yi~xi ,family =Gamma(link = "log"))
```

```
summary(model, dispersion =1)
```

#Find the 95% confidence interval

```
CI_of_beta <- confint.default(model,level=0.95)
```

CI_of_beta

#The variance-covariance matrix of the MLE

```
Tauinver<-vcov(model, dispersion =1)
```

Tauinver

```
#Find approximate of the information matrix evaluated at b
```

```
Tau_at_b<-solve(vcov(model, dispersion =1))
```

```
Tau_at_b
```

```
#the model fitted
```

```
yhat<-exp(8.4775-1.1093*xi) #or yhat=fitted.values(m,dispersion =1)
```

```
yhat
```

```
#residuals
```

```
ri<-(yi-yhat)/yhat
```

```
ri
```

```
#test statistics
```

```
test_statistic<- sum(ri^2)
```

```
test_statistic
```

```
#table value
```

```
chi_table<-qchisq(1-0.05,17-2)
```

```
chi_table
```