

# Past Exams: Ch.1 to Ch.4

Physics 103: Classical Mechanics

Dr. Abdulaziz Alqasem

Physics and Astronomy Department King Saud University

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# Outline



1.	Ch.1: Physics and Measurement	. 3
2.	Ch.2: Motion in One Dimension	. 6
1.	Ch.3: Vectors	19
4.	Ch.4: Motion in Two Dimensions	24



## 1. Ch.1: Physics and Measurement

2. Ch.2: Motion in One Dimension

3. Ch.3: Vectors

4. Ch.4: Motion in Two Dimensions



## Question 1.1

If the change of position x of a train is given by  $x = \frac{1}{2}at^2 + bt^3$  (where a is the acceleration). The dimension of a is:

A) LT<sup>-2</sup>

B) LT<sup>3</sup>

C) LT<sup>-1</sup>

D) LT-3



• The dimension of each term in the equation must be the same. Therefore,

$$[x] = \left[\frac{1}{2}at^2\right]$$



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$$[at^2] = L$$



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$$[a] T^2 = L$$



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• Since the dimension of the position x is length L and the constant  $\frac{1}{2}$  is dimensionless, thus we can write,

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• The dimension of time t is T, so,

$$[a] T^2 = L$$

• Finally, the dimension of acceleration *a* is:

$$[a] = LT^{-2}$$



## 1. Ch.1: Physics and Measurement

#### 2. Ch.2: Motion in One Dimension

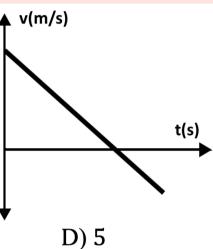
3. Ch.3: Vectors

4. Ch.4: Motion in Two Dimensions



## Question 2.2

the next graph represents the change in velocity (v) with time (t) of  $\phi$  v(m/s) motorcycle along a straight path. Which of the following accelerations (a) could be correct?



A) 
$$-5t$$

$$C) -5$$



The car is **slowing** down **linearly**, so the acceleration

$$a = \text{slope} = \frac{\Delta v}{\Delta t}$$

must be a constant number and a negative value at all times.

Therefore the only possible answer is **(C)** 



## Question 2.3

An airplane intial landing speed is 50 m/s. If it stops in 500 m, then the accelerattion (assumed to be constant) is:

A) - 7.5 
$$\frac{m}{s^2}$$

B) 
$$10 \frac{m}{s^2}$$

C) - 2.5 
$$\frac{m}{s^2}$$

D) 
$$5.0 \frac{m}{s^2}$$



$x_i$	$x_f$	$v_i$	$v_f$	a	t



$x_i$	$x_f$	$v_i$	$v_f$	a	t
0 m					

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$x_i$	$x_f$	$v_i$	$v_f$	a	t
0 m	500 m				

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$x_i$	$x_f$	$v_i$	$v_f$	a	t
0 m	500 m	50 m/s			

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$x_i$	$x_f$	$v_i$	$v_f$	a	t
0 m	500 m	50 m/s	0 m/s	?	-

• Since time t is not given, we can use the following equation to find the acceleration a:

$$v_f^2 = v_i^2 + 2a\big(x_f - x_i\big)$$



$x_i$	$x_f$	$v_i$	$v_f$	a	t
0 m	500 m	50 m/s	0 m/s	?	_

• Since time *t* is not given, we can use the following equation to find the acceleration *a*:

$$v_f^2 = v_i^2 + 2a(x_f - x_i)$$

• Rearranging the equation to find *a* gives:

$$a = \frac{v_f^2 - v_i^2}{2(x_f - x_i)} = \frac{0 - 2500}{2 * 500} = -2.5 \text{ m/s}^2$$



## Question 2.4

A car travelled north, and its initial speed was 100 km/h, then it reversed its direction and reached a final speed of 50 km/h. If the total time was 10 s, what is the average car acceleration in (m/s<sup>2</sup>)

A) 1.4

B) 
$$-1.4$$

$$D) - 4.2$$



• Since the car is decreasing its speed from  $+100~{\rm Km/h}$  to  $-50~{\rm Km/h}$ , it means that the acceleration is negative at all times.

Dr. Abdulaziz Algasem
Past Exams: Ch.1 to Ch.4

12 / 36



- Since the car is decreasing its speed from  $+100~{\rm Km/h}$  to  $-50~{\rm Km/h}$ , it means that the acceleration is negative at all times.
- To find the value of average acceleration, we need first to convert the speeds from Km/h to m/s:

$$100 \text{ km/h} * \left(\frac{1000 \text{ m}}{1 \text{ km}}\right) * \left(\frac{1h}{3600s}\right) = 27.78 \text{ m/s}$$



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• Now, we can find the average acceleration using the formula:

$$a_{\mathrm{avg}} = \frac{\Delta v}{\Delta t} = \frac{v_f - v_i}{t_f - t_i}$$



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• Now, we can find the average acceleration using the formula:

$$a_{\rm avg} = \frac{\Delta v}{\Delta t} = \frac{v_f - v_i}{t_f - t_i} = \frac{-13.89 - 27.78}{10 - 0} = -4.2 \ {\rm m/s^2}$$



# Question 2.5

As a free-falling object speeds-up, what is happening to its acceleration due to gravity?

A) decreases

B) none of these answers C)

C) increases

D) stays the same



Free-falling objects always experience a **constant** acceleration due to gravity

$$a_y = -g = -9.8 \text{ m/s}^2$$

regardless of their velocities, mass, ... etc.



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regardless of their velocities, mass, ... etc.

• Therefore, the correct answer is the acceleration **stays the same**.



## Question 0.6

A worker ascending at 7m/s in an open elevator 20 m above the ground accidently drops a stone. The velocity of the stone just before touching the ground is:

A) - 21 m/s

B) 58 m/s

C) - 14 m/s

D) 18 m/s



$y_i$	$y_f$	$v_i$	$v_f$	a	t
0 m	$-20 \mathrm{\ m}$	+7 m/s	?	-g	1



$y_i$	$y_f$	$v_{i}$	$v_f$	a	t
0 m	$-20 \mathrm{\ m}$	+7 m/s	?	-g	1

- Since time t is not given, we can use the following equation to find the final velocity  $\boldsymbol{v_f}$ :

$$v_f^2 = v_i^2 + 2a\big(y_f - y_i\big)$$



$y_i$	$y_f$	$v_{i}$	$v_f$	a	t
0 m	$-20 \mathrm{\ m}$	+7 m/s	?	-g	1

• Since time t is not given, we can use the following equation to find the final velocity  $\boldsymbol{v_f}$ :

$$v_f^2 = v_i^2 + 2a\big(y_f - y_i\big)$$

• Rearranging the equation to find  $v_f$  gives:

$$v_f = \sqrt{v_i^2 + 2a(y_f - y_i)} = \sqrt{49 + 2*(-9.8)*(-20)} = \pm 21 \text{ m/s}$$



$y_i$	$y_f$	$v_{i}$	$v_f$	a	t
0 m	$-20 \mathrm{\ m}$	+7 m/s	?	-g	-

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• The positive value indicates that the stone is moving in the positive direction (upwards) when it hits the ground, which is not true. Therefore, the correct answer is *only* the negative value ( $v_f = -21 \text{ m/s}$ ).



# Question 0.7

A freely falling body is found to be moving downwards at -27.2 m/s at one instant. If it continues to fall, 1 second later the object would be moving with a downward velocity?

A) 27 m/s

B) -57 m/s

C) - 37 m/s

D) 47 m/s



• Quick analysis: Every second, the velocity increases by  $-9.8~\rm m/s$  under gravity. Therefore, after 1s, the speed should be:



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• Formal solution:

$$v_f = v_i - gt$$



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$$-27.2 \text{ m/s} - 9.8 \text{ m/s} = -37 \text{ m/s}$$

• Formal solution:

$$v_f = v_i - gt = -27.2 \text{ m/s} + (-9.8 \text{ m/s}^2)(1s) = -37 \text{ m/s}$$



1. Ch.1: Physics and Measurement

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# Question 3.8

If  $\mathbf{A} = (6 \mathbf{i} - 8 \mathbf{j})$  units,  $\mathbf{B} = (-8 \mathbf{i} + 3 \mathbf{j})$  units, and  $\mathbf{C} = (26 \mathbf{i} + 19 \mathbf{j})$  units, the values of a and b respectively in units such that  $(a\mathbf{A} + b\mathbf{B} + \mathbf{C} = 0)$  are:

A) 5, 7

B) 2, 3

C)3,7

D) 5, 9



$$a\vec{A} + b\vec{B} + \vec{C} = 0$$



$$a\vec{A} + b\vec{B} + \vec{C} = 0$$
  
 $a(6\hat{\imath} - 8\hat{\jmath}) + b(-8\hat{\imath} + 3\hat{\jmath}) + (26\hat{\imath} + 19\hat{\jmath}) = 0$ 



$$a\vec{A} + b\vec{B} + \vec{C} = 0$$

$$a(6\hat{\imath} - 8\hat{\jmath}) + b(-8\hat{\imath} + 3\hat{\jmath}) + (26\hat{\imath} + 19\hat{\jmath}) = 0$$

$$(6a - 8b + 26)\hat{\imath} + (-8a + 3b + 19)\hat{\jmath} = 0$$



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$$(6a - 8b + 26)\hat{\imath} + (-8a + 3b + 19)\hat{\jmath} = 0$$

Therefore, both components must be zero:



$$a\vec{A} + b\vec{B} + \vec{C} = 0$$

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$$(6a - 8b + 26)\hat{\imath} + (-8a + 3b + 19)\hat{\jmath} = 0$$

Therefore, both components must be zero:

$$6a - 8b + 26 = 0$$



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Therefore, both components must be zero:

$$6a - 8b + 26 = 0$$
$$-8a + 3b + 19 = 0$$

Checking the options, we find that the correct answer is **(A)**:



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$$a(6\hat{\imath} - 8\hat{\jmath}) + b(-8\hat{\imath} + 3\hat{\jmath}) + (26\hat{\imath} + 19\hat{\jmath}) = 0$$

$$(6a - 8b + 26)\hat{\imath} + (-8a + 3b + 19)\hat{\jmath} = 0$$

Therefore, both components must be zero:

$$6a - 8b + 26 = 0$$
$$-8a + 3b + 19 = 0$$

Checking the options, we find that the correct answer is **(A)**:

$$6(5) - 8(7) + 26 = 30 - 56 + 26 = 0$$



$$a\vec{A} + b\vec{B} + \vec{C} = 0$$

$$a(6\hat{\imath} - 8\hat{\jmath}) + b(-8\hat{\imath} + 3\hat{\jmath}) + (26\hat{\imath} + 19\hat{\jmath}) = 0$$

$$(6a - 8b + 26)\hat{\imath} + (-8a + 3b + 19)\hat{\jmath} = 0$$

Therefore, both components must be zero:

$$6a - 8b + 26 = 0$$
$$-8a + 3b + 19 = 0$$

Checking the options, we find that the correct answer is **(A)**:

$$6(5) - 8(7) + 26 = 30 - 56 + 26 = 0$$
  $\checkmark$   $-8(5) + 3(7) + 19 = -40 + 21 + 19 = 0$   $\checkmark$ 



# Question 3.9

If  $A = [10 \text{ m}, 60^{\circ}]$  and  $B = [5 \text{ m}, 140^{\circ}]$ , in polar coordinates, what is the magnitude of the sum of these two vectors?

A) 12.5 m

B) 9.3 m

C) 10.2 m

D) 11.9 m

Dr. Abdulaziz Alqasem Past Exams: Ch.1 to Ch.4 22 / 36



$$\vec{A} = 10\cos(60^{\circ})\hat{\imath} + 10\sin(60^{\circ})\hat{\jmath} = 5\hat{\imath} + 8.66\hat{\jmath}$$



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$$\vec{B} = 5\cos(140^{\circ})\hat{\imath} + 5\sin(140^{\circ})\hat{\jmath} = -3.83\hat{\imath} + 3.21\hat{\jmath}$$



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$$\vec{B} = 5\cos(140^{\circ})\hat{\imath} + 5\sin(140^{\circ})\hat{\jmath} = -3.83\hat{\imath} + 3.21\hat{\jmath}$$

$$\vec{C} = \vec{A} + \vec{B} = (5 - 3.83)\hat{\imath} + (8.66 + 3.21)\hat{\jmath} = 1.17\hat{\imath} + 11.87\hat{\jmath}$$



$$\vec{A} = 10\cos(60^{\circ})\hat{\imath} + 10\sin(60^{\circ})\hat{\jmath} = 5\hat{\imath} + 8.66\hat{\jmath}$$

$$\vec{B} = 5\cos(140^{\circ})\hat{\imath} + 5\sin(140^{\circ})\hat{\jmath} = -3.83\hat{\imath} + 3.21\hat{\jmath}$$

$$\vec{C} = \vec{A} + \vec{B} = (5 - 3.83)\hat{\imath} + (8.66 + 3.21)\hat{\jmath} = 1.17\hat{\imath} + 11.87\hat{\jmath}$$

$$|\vec{C}| = \sqrt{(1.17)^2 + (11.87)^2} = 11.9 \text{ m}$$



1. Ch.1: Physics and Measurement

2. Ch.2: Motion in One Dimension

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4. Ch.4: Motion in Two Dimensions



# Question 4.10

A projectile is launched with an initial velocity of **20 m/s** at an angle of **30°** above the horizontal. What is the maximum height reached by the projectile?

A) 15.5 m

B) 21.3 m

C) 11.1 m

D) 5.1 m



# Answer 4.10

$$h = \frac{v_i^2 \sin^2(\theta)}{2g}$$



# Answer 4.10

$$h = \frac{v_i^2 \sin^2(\theta)}{2g} = \frac{20^2 \sin^2(30^\circ)}{2 * 9.8} = 5.1 \text{ m}$$



# Question 4.11

A particle moves in the xy-plane with a constant acceleration of  $4 \text{ m/s}^2$  at an angle of  $30^\circ$  above the positive x-axis. If the particle's initial position is (0, 0) and its initial velocity is (2 m/s, 3 m/s), what is its velocity vector after 3 seconds?

A) (16.6 m/s, 13.8 m/s)

B) (12.4 m/s, 9 m/s)

C) (14.5 m/s, 11.7 m/s)

D) (15.3 m/s, 12.2 m/s)



## Answer 4.11

The acceleration vector in cartesian coordinates is given by:

$$\vec{a} = 4\cos(30^{\circ})\hat{\imath} + 4\sin(30^{\circ})\hat{\jmath} = 3.46\hat{\imath} + 2\hat{\jmath}$$



#### Answer 4.11

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$$\vec{a} = 4\cos(30^{\circ})\hat{\imath} + 4\sin(30^{\circ})\hat{\jmath} = 3.46\hat{\imath} + 2\hat{\jmath}$$

• The velocity vector at after t = 3s is given by:

$$\vec{v} = \vec{v}_0 + \vec{a}t = (2\hat{\imath} + 3\hat{\jmath}) + (3.46\hat{\imath} + 2\hat{\jmath}) \times 3 = 12.4\hat{\imath} + 9\hat{\jmath}$$



# Question 4.12

Two particles, **A** and **B**, start from the same point at the same time and move with constant accelerations. Particle **A** has an acceleration of  $2 \text{ m/s}^2$  in the positive x-direction, while particle **B** has an acceleration of  $3 \text{ m/s}^2$  in the positive y-direction. Which particle will be farther from the origin after 5 seconds?

A) Particle B

B) It depends on the C) Particle A initial velocities of the particles

D) They will be at the same distance



#### Answer 4.12

From the equation of motion  $(\vec{r} = \vec{r}_i + \vec{v}_i t + \frac{1}{2} \vec{a} t^2)$ , we see that when  $r_i = v_i = 0$ ,

the position vector only depends on the acceleration as:

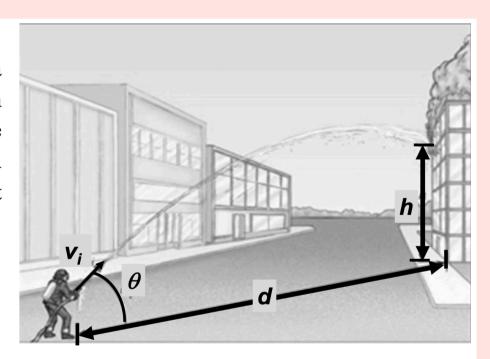
$$ec{m{r}}=rac{1}{2}ec{m{a}}t^2$$

Therefore, the particle with the largest acceleration will have the largest displacement after the same time interval. In this case, **particle B**.



# Question 4.13

A firefighter, at a distance d = 50 m from a burning building, directs a stream of water from a fire hose at an angle  $\theta = 30^{\circ}$  above the horizontal (as in the Figure). If the initial speed of the water stream is 40 m/s, the height at which the water strike the building is:



A) 24.3 m

B) 18.7 m

C) 5.6 m

D) 31.2 m



# Answer 4.13

• First, we need to find the time at which the stream of water reaches the building.



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$$d = v_i \cos(\theta) t$$



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$$d = v_i \cos(\theta) t \implies t = \frac{d}{v_i \cos(\theta)} = \frac{50}{40 \cos(30^\circ)} = 1.44s$$



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$$d = v_i \cos(\theta) t \implies t = \frac{d}{v_i \cos(\theta)} = \frac{50}{40 \cos(30^\circ)} = 1.44s$$

• Next, we can find the vertical position of the water stream at this time using the following equation:

$$y=v_i\sin(\theta)t-\frac{1}{2}gt^2$$



• First, we need to find the time at which the stream of water reaches the building.

$$d = v_i \cos(\theta) t \implies t = \frac{d}{v_i \cos(\theta)} = \frac{50}{40 \cos(30^\circ)} = 1.44s$$

• Next, we can find the vertical position of the water stream at this time using the following equation:

$$\begin{split} y &= v_i \sin(\theta) t - \frac{1}{2} g t^2 \\ &= 40 \sin(30^\circ) (1.44) - \frac{1}{2} (9.8) (1.44)^2 \\ &= 28.8 - 10.2 = 18.64 \text{ m} \end{split}$$



# Question 0.14

A race car moving with a constant speed of 60 m/s completes one lap around a circular track in 50

s. What is the magnitude of the acceleration of the race car?

A)  $7.5 \text{ m/s}^2$ 

B)  $2.5 \text{ m/s}^2$ 

C)  $3.4 \text{ m/s}^2$ 

D)  $5.4 \text{ m/s}^2$ 



• Since the car is moving in a circular path, the centripetal acceleration is given by  $v^2/r$ .



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$$T = \frac{2\pi r}{v} \implies r = \frac{vT}{2\pi} = \frac{60 \times 50}{2\pi} = 477.7 \text{ m}$$



• Since the car is moving in a circular path, the centripetal acceleration is given by  $v^2/r$ . The velocity is given (60 m/s) and the radius r can be found from the period T using:

$$T = \frac{2\pi r}{v} \implies r = \frac{vT}{2\pi} = \frac{60 \times 50}{2\pi} = 477.7 \text{ m}$$

Therefore, the magnitude of the centripetal acceleration is:

$$a = \frac{v^2}{r} = \frac{60^2}{477.7} = 7.5 \text{ m/s}^2$$



# Question 0.15

The speed of a particle moving in a circle 2 m in radius increases at the constant rate of  $4.4 \text{ m/s}^2$ . At an instant when the magnitude of the total acceleration is  $6 \text{ m/s}^2$ , what is the speed of the particle?

A) 1.4 m/s

B) 4.2 m/s

C) 2.9 m/s

D) 3.8 m/s



$$r=2 \text{ m}, \quad a_t=4.4 \text{ m/s}^2, \quad a_{\text{tot}}=6 \text{ m/s}^2, \quad \text{ Find } v=?$$



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$$\implies v = 2.9 \text{ m/s}$$