



**Midterm 1 – Math 228- semester 1- 1447H**  
**Time: 1h 30 min**

**Question 1:( 2+2+2+2=8 marks)**

1) Find the average value of the function  $f(x) = \frac{1}{x} + 1$  on the interval  $[1, e]$

2) Find the derivative of  $F(x) = \int_{2x}^{\sec x} \sqrt{t^2 - 1} dt$

3) Find the area of the region bounded by the graphs of  
 $y = x^2$  and  $y = -x + 2$

4) Find the volume of the solid generated by revolving the region bounded by the graphs of  $y = x^2$  and  $y = 2x$  around the x- axis.

**Question 2: Evaluate the following integrals (17 mark)**

1)  $\int \frac{1}{\cos^2(\frac{x}{2})} dx$  (2)

2)  $\int x e^{2x} dx$  (2)

3)  $\int \tan^3(x) \sec^3(x) dx$  (3)

4)  $\int \frac{1}{x^2 \sqrt{9-x^2}} dx$  (3)

5)  $\int \frac{1}{x \sqrt{(\ln x)^2 - 1}} dx$  (2)

6)  $\int \frac{x+3}{x^2+3x+2} dx$  (3)

8)  $\int \frac{1}{1-\cos x} dx$  (2)