

Question 1: (2+2+2+2=8 marks)

- 1) Find the average value of the function $f(x) = \frac{1}{x} + 1$ on the interval $[1, e]$
- 2) Find the derivative of $F(x) = \int_{2x}^{\sec x} \sqrt{t^2 - 1} dt$
- 3) Find the area of the region bounded by the graphs of $y = x^2$ and $y = -x + 2$
- 4) Find the volume of the solid generated by revolving the region bounded by the graphs of $y = x^2$ and $y = 2x$ around the x-axis.

Question 2: Evaluate the following integrals (17 mark)

1) $\int \frac{1}{\cos^2(\frac{x}{2})} dx$ (2)

2) $\int x e^{2x} dx$ (2)

3) $\int \tan^3(x) \sec^3(x) dx$ (3)

4) $\int \frac{1}{x^2 \sqrt{9-x^2}} dx$ (3)

5) $\int \frac{1}{x \sqrt{(\ln x)^2 - 1}} dx$ (2)

6) $\int \frac{x+3}{x^2+3x+2} dx$ (3)

8) $\int \frac{1}{1-\cos x} dx$ (2)