College of Science.
Department of Mathematics

# Final Exam <br> Academic Year 1442-1443 Hijri- SecondSemester 



Student Information معلومات الطالب

| Student Information معلومات الطالب |  |  |
| :---: | :---: | :---: |
| Student's Name |  | اسم الطالب |
| ID number |  | الرقم الجامعي |
| Section No. |  | رقم الشعبة |
| Serial Number |  | الرقمّ التسلسلي |

General Instructions:

- Your Exam consists of 8 PAGES (except this paper)
- Keep your mobile and smart watch out of the classroom.

الورقة)

- يجب إبقاء الهو اتف والساعات الذكية خارج قاعة الامتحان.
- 

هذا الجزء خاص بأستاذ المادة
This section is ONLY for instructor

| $\#$ | Course Learning Outcomes (CLOs) | Related <br> Question (s) | Points | Final <br> Score |
| :--- | :--- | :--- | :--- | :--- |
| 1 |  |  |  |  |
| 2 |  |  |  |  |
| 3 |  |  |  |  |
| 4 | . |  |  |  |
| 5 |  |  |  |  |
| 6 |  |  |  |  |
| 7 |  |  |  |  |
| 8 |  |  |  |  |

Answer all of the following questions, please make sure that your hand writing is clear:
QI. For all complex numbers $z$, show that $\sqrt{2} z \geq|\operatorname{Re} z|+|\operatorname{Im} z|$. When do we have equality?
QII. Use de Moivre's formula to find $(\sqrt{3}-i)^{100}$.
QIII. Write the Cauchy-Riemann equations in $x-y$ coordinates. Derive the polar form of C-R equations and use it to show that $\log z$, is analytic. State the maximal possible domain of analyticity, then find the derivative and justify your answer.

QIV. Find all complex numbers $z$, such that $\cos z=2$.
QV. State the Cauchy integral formula and then prove it.
QVI. Let $f(z)=\frac{\cosh z^{2}-1}{z^{4}}$. Show that $z=0$ is a removable isolated singularity. Then find $f^{(80)}(0)$.

QVII. Use Residue Theorem to calculate

$$
\int_{0}^{\infty} \frac{d x}{x^{4}+1}
$$

QVIII. Use residues to calculate

$$
\int_{-\infty}^{\infty} \frac{x \sin x}{x^{4}+4} d x
$$

