

# King Saud University College of Science Numerical Methods Course Syllabus Second Semester 1444 - 1445

# **1.** Course General Information:

Course Title: Numerical Methods	Course Code: MATH 351	
Course Level: 5	Course Prerequisite: (MATH107 or	
	MATH202 or MATH244) and (CSC101 or	
	CSC206 or CSC207).	
	Co-requisites for this course (if any): None	
Lecture Time: 10-11 AM.	Credit Hours: 3	

#### 2. Faculty Member Responsible for the Course:

Name	Rank	Office Number and Location	Office Hours	Email Address
Dr. Bandar Almohsen	Professor	2A284 Building 4 Main Campus	8 AM-1PM Monday and Wednesday	balmohsen@ksu.edu.sa

#### 3. Course Description:

Numerical Methods for Solving Nonlinear Equations: Bisection method, fixed point method, Newton's method, secant method, multiple roots, modified Newton's method, rate of convergence (error analysis), Newton's method for solving nonlinear systems. Solving Systems of Linear Equations: Gaussian elimination, Gaussian elimination with partial pivoting, LU-decomposition, Jacobi method, Gauss-Seidel method. Interpolation and Polynomial Approximations Lagrange interpolation formula, Newton's interpolation formula, interpolation using linear splines. Numerical Differentiation and Integration: Trapezoidal, and Simpson's rules. Numerical solutions of Ordinary Differential equations; Taylor methods and Runge-Kutta method of order two.

#### 4. Course Academic Calendar

Week	Topics to be Covered
1-3	Numerical Methods for Solving Nonlinear Equations: Bisection method, fixed point method, Newton's method, secant method, multiple roots, modified Newton's method, rate of convergence (error analysis), Newton's method for solving nonlinear systems.
4-7	Solving Systems of Linear Equations: Direct methods: Gaussian elimination, Gaussian elimination with partial pivoting, LU-decomposition. Iterative methods: Jacobi method, Gauss-Seidel method. Error analysis for solving Linear system

8-10	Interpolation and Polynomial Approximations Lagrange interpolation formula, divided differences, Newton's interpolation formula, error in polynomial interpolation, interpolation using linear splines.
11-13	Numerical Differentiation and Integration
	First derivative: two-point formulas (forward and backward) and three-point formulas
	(forward, central and backward).
	Second derivative: the central method.
	Trapezoidal, Simpson's rules, and the error bounds.
14-15	Numerical solutions of Ordinary Differential equations;
	Taylor methods, Runge-Kutta method of order two and the local truncation error for
	Euler's and Taylor's formulas.
16	Final exam

# 5. Course Objectives:

The main purpose for this course is to introduce the following concepts:

- The main purpose for this course is to introduce:
- Numerical methods for solving mathematical problems
- Analyze the error for these methods
- Write computer algorithms to implement these methods for solving certain mathematical problems using computer.

## 6. Course References:

#### 6.1 Textbooks:

An Introduction to Numerical Analysis using MATLAB, by Rizwan Butt, Infinity Science Press, Hingham, Massachusetts, New Delhi, 2008

## 6.2 Essential References Materials (Journals, Reports, etc.)

1-Numerical Analysis, Richard L. Burden and J. Douglass Faires, fifth edition, Brooks/Cole

2- An Introduction to Numerical Linear Algebra using MATLAB, Rizwan Butt, Heldermann Verlag, Germany, 2008.

#### 6.3 Recommended Textbooks and Reference Material (Journals, Reports, etc)

1-Numerical Analysis, Richard L. Burden and J. Douglass Faires, fifth edition, Brooks/Cole

2- An Introduction to Numerical Linear Algebra using MATLAB, Rizwan Butt, Heldermann Verlag, Germany, 2008.

#### 6.4 Websites:

- 1- KSU Learning Management System
- 2- Internet websites relevant to the course

# 6.5 Other learning material such as computer-based programs/CD, professional standards or regulations and software.

• None

# 7. Teaching Methods:

- At the beginning of studying each topic some examples will be laid out and discussed with the students encouraging them to discover the relevant concepts.
- At the beginning of each lecture, a discussion is conducted with the students about what has been done in the previous lecture in order to establish a link with the current lecture.
- Discussions in the class

- Homework assignments
- Independent study

#### 8. Learning Outcomes:

#### 8.1 Knowledge and Understanding:

After studying this course, the student will acquire the following knowledge and be able to:

- Define error, absolute error and relative error.
- Define a fixed point of a given function.
- State Newton's, Secant and Modified Newton's formulas.
- Define a multiple root of a nonlinear equation, and the order of convergence of an iterative scheme.
- Define the residual vector corresponding to an approximate solution of a given linear system.
- Define the condition number of a given nonsingular matrix.
- Define divided differences of a function and state Lagrange and Newton's interpolation formulas.
- State Taylor's and Runge Kutta methods for solving an initial value problem.

#### 8.2 Cognitive Skills (Thinking and Analysis):

After studying this course, the student will able to:

- 1) Solve a nonlinear equation numerically by different numerical methods and analyze the resulting error.
- 2) Compute the rate of convergence for iterative schemes.
- 3) Solve a system of linear equations by direct and indirect methods and analyze the resulting error.
- 4) Approximate a function or data using polynomial interpolation formulas and analyze the error in these formulas.
- 5) Apply difference formulas to approximate derivatives and analyzing the error in these formulas.
- 6) Approximate a definite integral using trapezoidal and Simpson's rules and analyzing the error in these methods.
- 7) Solve an initial value problem of ordinary differential equations using different methods.
- 8) Write mathematical algorithms for different numerical methods.

#### 8.3 Interpersonal Skills and Responsibility:

After studying this course, the student is expected to:

- To participate in the discussion
- Study, learn and work independently.
- Work effectively in teams.
- Meet deadlines and manage time properly.
- Exhibit ethical behaviour and respect different points of view.

#### 8.4 Communication, Information Technology and Numerical Skills

After studying this course, the student is expected to be able to:

- Present mathematics to others, both in oral and written form clearly and in a well-organized manner.
- Use IT facilities as an aid to mathematical processes and for acquiring available information
- Write algorithms and solve mathematical problems numerically.
- Use library to locate mathematical information.
- 9. Methods of Assessment:

Course Assessment	Mark
Class activates ( in class quizzes, and	10
homework)	
Midterm exams I	25
Midterm exams II	25
Final Examination	40
Total	100

# **10. Course Policies:**

- All exams are closed book.
- The final exam will be comprehensive.

#### **11. Attendance Policy:**

Absence from lectures and/or tutorials shall not exceed 25%. Students who exceed the 25% limit without an accepted medical or emergency excuse shall not be allowed to take the final examination and shall receive a grade of "DN" for the course.