

MATH 151

**Tree**

Lecture 9

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**Exercise 1:** The graph represented by adjacency matrix. Is a tree why?

$$\begin{bmatrix} 0 & 1 & 1 & 0 \\ 1 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}$$

**Exercise 2:** Let  $G$  be a graph with 7 edges and vertices  $a, b, c, d, e, f$  whose respective degree are  $x, 2x, 2x, 2x, 3x, 4x$

- i. Find  $x$
- ii. Can  $G$  be a tree? (justify your answer)

**Exercise 3:** Let  $G$  be a graph with 7 edges and vertices  $a, b, c, d, e, f$  whose respective degree are  $x, 2x, 2x, 2x, 3x, 4x$

- i. Find  $x$
- ii. Can  $G$  be a tree? (justify your answer)

**Exercise 4:** Represent all non isomorphic graphs whose 4 vertices

**Exercise 5:** If  $T$  is a tree and degree of its 5 vertices are  $1, 1, 1, 2, d$ . Find the value of  $d$ .

**Exercise 6:** If  $T$  is a tree whose sequence-degree  $1, 1, 1, 1, 3, d$ . Find the value of  $d$ .

**Exercise 7:** Find  $k$  if you know there is a tree with sequence-degree  $1, 1, 1, 1, 2, 2, k, 2k$

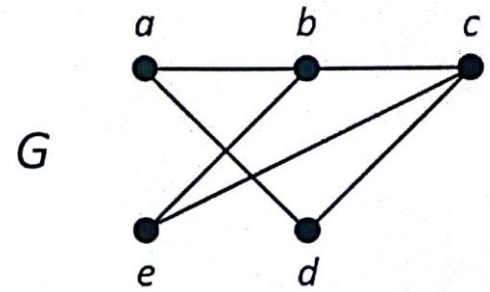
**Exercise 8:** Let  $T$  be a tree with  $n$  vertices  $v_1, v_2, \dots, v_n$  where  $n > 2$ . Find  $\deg(v_n)$  if you know that  $\deg(v_1) = \deg(v_2) = \dots = \deg(v_{n-1}) = 1$

**Exercise 9:** Is there a tree with  $v$  vertices and  $e$  edges such that  $3v = 5e$  (justify your answer)

**Exercise 10:** Given an example of graph  $G$  which is complete, complete bipartite and tree.

**Exercise 11:** For the graph  $G$  below, find spanning tree with root  $a$

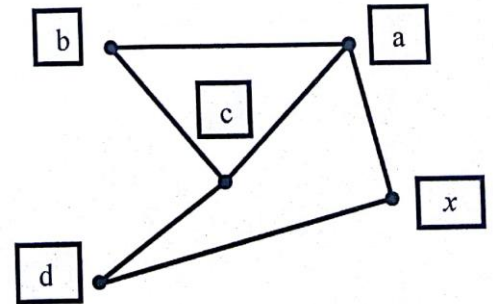
i. Using depth-first search



ii. Using breadth-first search

**Exercise 12:** Let  $G$  be the following graph

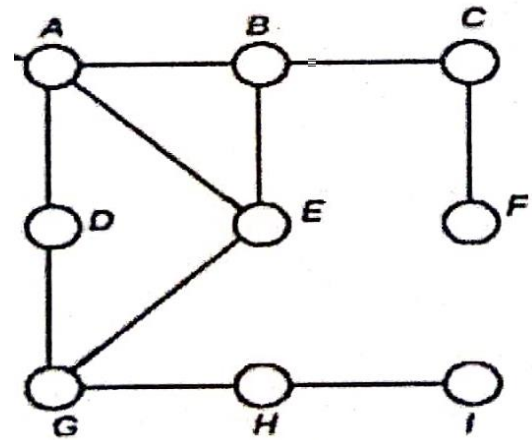
- i. Find depth first search tree with the vertex  $x$  to be the root



- ii. Find breadth first search tree with the vertex  $x$  to be the root

**Exercise 13:** Let  $G$  be the following graph

- i. Find depth first search tree with the vertex  $A$  to be the root

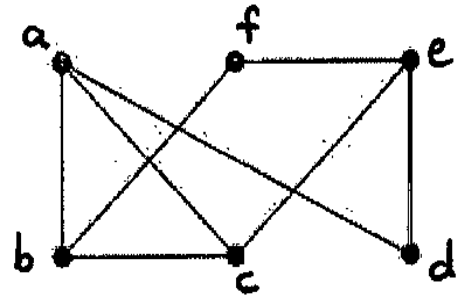


- ii. Find breadth first search tree with the vertex  $A$  to be the root



**Exercise 14:** Let  $G$  be the following graph

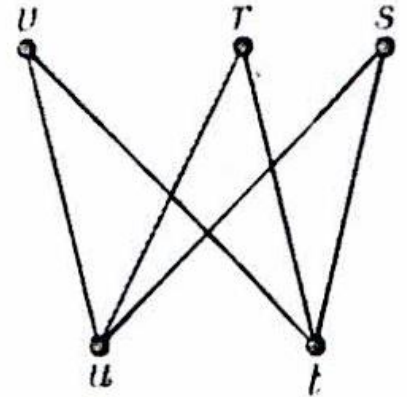
- i. Find depth first search tree with the vertex  $a$  to be the root



- ii. Find breadth first search tree with the vertex  $a$  to be the root

**Exercise 15:** For the graph  $G$  below, find spanning tree with root  $r$

i. Using depth-first search

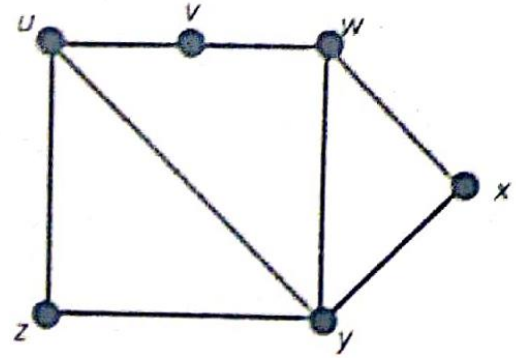


ii. Using breadth-first search

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**Exercise 16:** For the graph  $G$  below, find spanning tree with root  $v$

i. Using depth-first search



ii. Using breadth-first search

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**Exercise 16:** From a binary search tree for the words: **mathematics-physics-geography- statistics- engineering- meteorology- geology- zoology- chemistry.**

**Exercise 16:** From a binary search tree for the words: **beetle- fly- ant- butterfly- bee- termite.**

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**Exercise 16:** From a binary search tree for the words: **jeans- sweater- dress- skirt- socks- coat- gloves- shoes- boots- belt- scarf**

**Exercise 16:** From a binary search tree for the words: **orange- blue- red- green- purple- black- pink**

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