# MATH 151 

## Graph Lecture 8

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Exercise 1: Find the degree of each vertices of following graph so find the sequence degree


Exercise 2: Represent the graph by adjacency matrix


Exercise 3: Represent the graph by incidence matrix


Exercise 4: Determine whether the graph is bipartite. If so provide a bipartite graph representation.
i.

ii.

iii.

iv.

V.


Exercise 5: Let $G$ be the simple graph represented by the adjacency matrix $A$ below.
i. Draw the graph $G$

$$
A=\left[\begin{array}{lllll}
0 & 1 & 0 & 1 & 0 \\
1 & 0 & 1 & 0 & 1 \\
0 & 1 & 0 & 1 & 0 \\
1 & 0 & 1 & 0 & 1 \\
0 & 1 & 0 & 1 & 0
\end{array}\right]
$$

ii. Determine whether the graph is bipartite. If so, provide a bipartite representation.

Exercise 6: Let $G$ be a graph such that $V=\{a, b, c\}$ and $\operatorname{deg}(b)=2 \operatorname{deg}(a)$ $\operatorname{deg}(c)=3 \operatorname{deg}(a)$ where $|E|=9$. Find $\operatorname{deg}(a)$

Exercise 7: Let $G$ be a graph such that $V=\{a, b, c, d, f\}$ and $\operatorname{deg}(a)=\operatorname{deg}(b)=\operatorname{deg}(c)=\operatorname{deg}(d)=1$ where $|E|=4$. Find $\operatorname{deg}(f)$

Exercise 8: Is there a graph has degree sequence $0,1,1,2,3,4,5,5$. why?

Exercise 9: Is there a simple graph has degree sequence 1,2,3,3,5,6. why?

Exercise 10: Let $G$ be a graph has degree-sequence $n, n, n, n, 2 n, 2 n, 3 n$ and $E(G)=11$. Find $n$

Exercise 11: If $G$ is a graph with 9 edges and the degree-sequence 1,3, $x, x$ Find $x$

Exercise 12: Let $G$ be a graph with degree-sequence 1, $a, a, a^{2}$ knowing that $G$ has 8 edges, find all possible value of $a$.

Exercise 13: Determine the number of edges for the complement of $K_{10,14}$

Exercise 14: Find the number of edges of complement $K_{4,7}$

Exercise 15: Find the number $n$ of vertices of complete graph having $10 n$ edges.

Exercise 16: Find the number of vertices of complete graph have 55 edges

Exercise 17: If $K_{5, n}$ having the same number of edges of $K_{n}$. Find the value of $n$.

Exercise 18: If the number of vertices equal number of edges in $K_{n, n}$ find $n$

Exercise 19: If you know the number of vertices of $K_{m, m^{2}}$ is 42 . Find the number of edges

Exercise 20: Let $G$ be a graph represented by incidence matrix
Find $|E(G)|$ and $|E(\bar{G})|$
$\left[\begin{array}{lll}1 & 1 & 1 \\ 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1\end{array}\right]$

Exercise 21: Represent $\bar{K}_{2,3}$. Then determine whether $\bar{K}_{2,3}$ is bipartite graph or not

## Exercise 22: There is a graph has 8 vertices and 18 edges regular. why?

Exercise 23: If the number of edges of $K_{n}$ is $4 n$. Find $n$

Exercise 24: If $G$ be a graph with $3 n$ vertices, such that $n$ vertices have degree 2 and $2 n$ vertices have degree 1 . Find $n$ if you know $E(G)=20$

Exercise 25: If $G$ is a complete graph with 21 edges. How many vertices dose $G$ have?

Exercise 26: If $G$ is a complete graph with 45 edges. How many vertices dose $G$ have?

Exercise 27: If $G$ is a simple graph with 15 edges and $\bar{G}$ has 13 edges. How many vertices dose $G$ have?

Exercise 28: If $G$ is a simple graph with $n$ vertices and 30 edges and $\bar{G}$ has 36 edges. How many vertices dose $G$ have?

Exercise 29: If $G$ is a 4-reguler graph with 8 vertices. Find the number of edges for its complement $\bar{G}$.

Exercise 30: Find all possible numbers of vertices of complete bipartite graphs $K_{m, n}$ having 12 edges.

Exercise 31: Given an example of complete graph which is not complete bipartite.

Exercise 32: Given an example of complete bipartite graph which is not complete.

Exercise 33: For the graph below:
i. Find the adjacency matrix $A$ with respect to the ordering of vertices $a, b, c, d$

ii. Use the matrix $A$ to find the number of paths of length 3 between $a$ and $b$

Exercise 34: Determine whether the following graphs $H$ and $G$ are isomorphic i.

ii.


iv.



## Graph

vii.


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viii.


