King Saud University: Mathematics Department Math-254 First Semester 1446 H Second Midterm Exam. Maximum Marks = 25 Time: 90 mins.

Questions: (6+7+6+6) Marks

## Question 1:

Compute the determinant of the matrix A and the solution of the following linear system using the Gaussian elimination with partial pivoting

$$x_1 + x_2 + x_3 = 0.5$$
  
 $2x_1 - 3x_2 + x_3 = -1$   
 $-x_1 - 1.5x_2 + 2.5x_3 = -1$ 

## Question 2:

Use LU-factorization method with Doolittle's method ( $l_{ii}=1$ ) to find the solution of the consistent system for  $\alpha \neq 3$ .

## Question 3:

Consider the following linear system of equations

Find the matrix form of Gauss-Seidel method. If  $\mathbf{x}^{(0)} = [0.5, 0.5, 0.5]^T$ , then compute an error bound  $||x - x^{(10)}||$ .

## Question 4:

Let  $f(x) = e^{3x} + \cos 2x$  (x is in radian) and  $x_0 = 0.1$ ,  $x_1 = 0.2$ ,  $x_2 = 0.4$ ,  $x_3 = 0.5$ . Then find the best approximation of f(0.45) using the quadratic Lagrange interpolation formula and also estimate an error bound and the absolute error for the approximation.