

254 MATH (Numerical Methods)

Textbook:

An Introduction to Numerical Methods and Analysis Using MATLAB

by Rizwan Butt.

Chapter	Sections	Exercises
1	1.2, 1.3	<p>1) Find the absolute and relative errors in approximating π by 3.1416. What are the corresponding errors in the approximation $100\pi \approx 314.16$?</p> <p>2) Calculate the error, relative error, and number of significant digits in the following approximations, with $p \approx x$:</p> <p>a) $x = 25.234$, $p = 25.255$.</p> <p>b) $x = e$, $p = 19/7$.</p> <p>c) $x = \sqrt{2}$, $p = 1.414$.</p>
2	2.1, 2.2, 2.3, 2.4, 2.5	<p>Textbook:</p> <p>Example: 2.4, 2.63.</p> <p>Exercises: page 76: 1(a,c), 2(b), 3 -15.</p>
3	3.1, 3.2, 3.3, 3.4, 3.5, 3.6, 3.7	<p>Textbook:</p> <p>Example: 3.20, 3.26, 3.41, 3.43, 3.51, 3.55</p> <p>Exercises: page 178: 2 -16.</p> <p>1) Consider the following system of equations:</p> $\begin{aligned} 4x_1 + 2x_2 + x_3 &= 1 \\ x_1 + 7x_2 + x_3 &= 4 \\ x_1 + x_2 + 20x_3 &= 7 \end{aligned}$ <p>a) Show that the Jacobi method converges using $\ T_J\ _\infty < 1$.</p> <p>b) Compute the second approximation $x^{(2)}$, starting with $x^{(0)} = [0, 0, 0]^T$.</p> <p>c) Compute an error estimate $\ x - x^{(2)}\ _\infty$ for your approximation.</p>



		<p>2) Consider the following system of equations:</p> $\begin{aligned} 4x_1 + 2x_2 + x_3 &= 11 \\ -x_1 + 2x_2 + &= 3 \\ 2x_1 + x_2 + 4x_3 &= 16 \end{aligned}$ <p>a) Show that the Gauss-Seidel method converges using $\ T_G\ _\infty < 1$.</p> <p>b) Compute the second approximation $x^{(2)}$, starting with $x^{(0)} = [1, 1, 1]^T$.</p> <p>c) Compute an error estimate $\ x - x^{(2)}\ _\infty$ for your approximation.</p> <p>3) Consider the following system of equations:</p> $\begin{aligned} 4x_1 - 2x_2 - x_3 &= 1 \\ -x_1 + 4x_2 + &- x_4 = 2 \\ -x_1 &+ 4x_3 - x_4 = 0 \\ &- x_2 - x_3 + 4x_4 = 1 \end{aligned}$ <p>Using $x^{(0)} = 0$, how many iterations are required to approximate the solution to within five decimal places using: (a) Jacobi method, (b) Gauss-Seidel method.</p>															
4	4.1, 4.2, 4.3	Textbook: page 236: 1 -19.															
5	5.1, 5.2, 5.3, 5.4, 5.5	<p>Textbook: page 293: 1 -21.</p> <p>1) Use the most accurate formula to determine approximations that will complete the following table:</p> <table border="1" data-bbox="635 1377 1121 1646"> <thead> <tr> <th>x</th> <th>f(x)</th> <th>df/dx</th> </tr> </thead> <tbody> <tr> <td>2.1</td> <td>- 1.709847</td> <td></td> </tr> <tr> <td>2.2</td> <td>-1.373823</td> <td></td> </tr> <tr> <td>2.3</td> <td>- 1.11921</td> <td></td> </tr> <tr> <td>2.4</td> <td>- 0.916014</td> <td></td> </tr> </tbody> </table> <p>2) Evaluate $\int_0^1 e^{x^2} dx$ by Simpson's rule choosing h small enough to guarantee five decimal accuracy. How large can h be?</p>	x	f(x)	df/dx	2.1	- 1.709847		2.2	-1.373823		2.3	- 1.11921		2.4	- 0.916014	
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