

**Date of Birth:** 01/01/1958,  
**Nationality:** Azerbaijani  
**Gender :** Male

Department of Mathematics, College of Science,  
King Saud University,  
Riyadh-11451 / Saudi Arabia  
mgarayev@ksu.edu.sa  
Tel : 00966550104728

## UNIVERSITY EDUCATION

	<b>PhD in Mathematics Leningrad Branch. Steklov Mathematical Institute</b> (LBMI), (Saint Petersburg/Russia) Scientific Advisors: Prof. N.K.Nikolski and Prof.V.I.Vasyunin
<b>1984- 1987</b>	<b>Thesis title :</b> Addition of spectral multiplicities and invariant subspaces
<b>1980-1983</b>	<b>M.S in Analysis , Leningrad Branch. Steklov Mathematical Institute</b> (LBMI), (Saint Petersburg/Russia) Scientific Advisors: Prof. N.K.Nikolski .
<b>1970-1974</b>	<b>B.S in Mathematics , Azerbaijan State University</b> (Baku / Azerbaijan)

## WORK EXPERIENCES

<b>2012- present</b>	<b>Professor of Mathematics in the Department of Mathematics, College of Science, King Saud University.</b>
<b>2001 -2012</b>	Professor, Department of Mathematics, Suleyman Demirel University, (Isparta/Turkey)
<b>2011( March- July)</b>	Visiting Professor, Department of Mathematics, Claude Bernard Lyon 1 University, (Lyon/ France)
<b>1996-2001</b>	Assoc.Prof., IMM Academy of Sciences of Azerbaijan, (Baku/ Azerbaijan)
<b>1988-1996</b>	Assistant Prof., IMM Academy of Sciences of Azerbaijan,(Baku/ Azerbaijan)

## LANGUAGE SKILLS

**Azerbaijani/Turkish :** Native langue      **English :** Upper intermediate  
**German:** Elementary      **Russian :** Upper intermediate

## RESEARCH INTERESTS

Functional analysis, operator theory, complex analysis

### **Published Talks (Abstracts)**

1. Karaev M.T. and Gürdal M., Some results for the weighted shift operators on the Banach spaces, International Conference Analysis and its applications (ICAA-08), India, November 3-5, sayfa , 2008.
2. Karaev, M.T., On the boundary behavior of Berezin Symbols, Mathematics Workshop Days, May 15-16, Istanbul Commerce University.
3. Karaev, M.T., On the Duhamel Algebras, ISAAC, 2009.Congress Imperial College London, July 13-18, 2009 .
4. Karaev,M.T. and Gurdal,M.,On some problems related with some special operator classes,21st International Workshop on Operator Theory and its Applications(IWOTA 2010),July 12-16,2010,TU Berlin,Germany.
5. Gurdal,M.andKaraev,M.T.,On some questions of operator theory,,21st International Workshop on Operator Theory and its Applications(IWOTA 2010),July 12-16,2010,TU Berlin,Germany.

### **Editorialship:**

1. Advances in Linear Algebra and Matrix Theory.(Editor-in Chief)
2. Journal of Mathematical Sciences: Advances and Applications
3. International Journal of Mathematical Archive.
- 4.Journal of Mathematical Analysis.
- 5.Proceedings of IMM .

### **REFEREE of the following journals:**

- 1.Proc.Amer.Math.Soc.
- 2.Positivity
- 3.J.Math.Anal.Appl.
- 4.Opuscula Mathematica
- 5.ArapJ.Math.Sci.
- 6.BanachJ.Math.Anal.
- 7.Proc.IMM
- 8.AbstractAppl.Anal.
- 9.TurkishJ.Math.
- 10.NumericalFunct.Anal.Optimization.

THE MEMBER IN ANALYSIS GROUP IN DEPARTMENT OF MATHEMATICS, COLLEGE OF SCIENCE, KSU.

## **Selected Recent Publications:**

1. Karaev, M.T., Berezin symbols and Schatten-von Neuman classes, (Russian) Matematicheskie Zametki, 72(2002), 207-215.
2. Karaev, M.T., Mustafayev, H.S., On some properties of Deddens algebras, Rocky Mountain J. Math., 33(3)(2003), 915-926.
3. Karaev, M.T. ,Tuna, H., Description of maximal ideal space of some Banach algebra with multiplication as Duhamel product, Complex variables: Theory and applications, 49, no.6, (2004), 449-457
4. Karaev, M.T., Pehlivan, S., Some results for quadratic elements of a Banach algebra, Glasgow Math. J., 46(3) (2004), 431-441.
5. Karaev, M.T., Closed ideals in  $C^1$  with the Duhamel product as multiplication, J. Math. Anal. Appl., 300(2)(2004), 297-302.
6. Karaev, M.T., New proofs of the Haagerup de Harpe inequality, Math. Notes, 75(5)(2004), 731-733. Translation from Matem. Zametki, 75(5)(2004), 787-788.
7. Karaev, M.T., Functional analysis proofs of Abel's theorems, Proc. Amer. Math. Soc., 132(8)(2004), 2327-2329.
8. Karaev, M.T., The numerical range of a nilpotent operator on a Hilbert space, Proc. Amer. Math. Soc., 132(8)(2004), 2321-2326.
9. Pehlivan, S., Karaev, M.T., Some results related with statistical convergence and Berezin symbols, J. Math. Anal. Appl., 299(2)(2004), 333-340.
10. Karaev, M.T. ,Saltan, S., Some results on Berezin symbols, Complex variables: Theory and applications. 50, no.3, (2005),185-193
11. Karaev, M.T., Saltan S., A Banach algebra structure for Wiener algebra  $W(D)$  of the disc, Complex variables: Theory and applications, v.50, no 4 (2005), 299-305.
12. Karaev, M.T., Invariant subspaces, cyclic vectors, commutant and extended eigenvectors of some convolution operators, (English) Methods of Functional Analysis and Topology, v.11, n1(2005), 48-59.
13. Karaev, M.T., On some applications of the ordinary and extended Duhamel products, Siberian Mathematical Journal, 46(3)(2005), 431-442.
14. Karaev, M.T., On some problems related to Berezin symbols, Comptes Rendus Acad. Sci. Paris Ser I, 340(2005), 715-718.
15. Karaev, M.T., Corrigendum to "On the Spectral Multiplicity of a Direct Sum of Operators, Colloquium Mathematicum, 104(1)(2006), 105-112:", Colloq. Math., 106(2); 2006; p.325:
16. Karaev, M.T., On the Spectral Multiplicity of a Direct Sum of Operators, Colloquium mathematicum, 104(1)(2006); 105 - 112:
17. Karaev, M.T., On extended eigenvalues and eigenvectors of some operator classes, Proc. Amer. Math. Soc.,134(2006), 2383-2392.
18. Karaev, M.T., New proof of Nagnibida's theorem, J. Function Spaces and Applications, 4(2006), 85-90.
19. Karaev, M.T., Tuna H., On some applications of Duhamel product, Linear and multilinear algebra, 54(4)(2006), 301-311.
20. Karaev, M.T., Berezin Symbol and Invertibility of Operators on the Functional Hilbert spaces, Journal of Functional Analysis, 238(2006), 181-192.
21. Karaev, M.T., On estimate for numerical radius of some contractions, Ukrainian Mathematical Journal, 58(10)(2006), 1512-1516.

22. Karaev, M.T., On the proof of Beurling's theorem on  $z$ -invariant subspaces, *Expositiones Mathematicae*, 25(2007), 265-267.
23. Karaev, M.T., Banach Algebra Technique for Proving an Addition Formula for Spectral Multiplicities of Sets of Operators, *Functional Analysis and Its Applications*, 41(1)(2007), 76-78.
24. Karaev, M.T., On Beurling-Arveson type theorem for some functional Hilbert spaces and related questions, *Integral Equat. Oper. Theory*, 62(1)(2008), 77-84.
25. Karaev, M.T., On the Riccati equations, *Monatshefte für Mathematik*, 155(2)(2008), 161-166.
26. Karaev, M.T., Banach Algebra Techniques for spectral multiplicity, *Archiv der Math.*, 93(2009), 147-152.
27. Karaev,M.T.,e-convergence and related problem, *Comptes Rendus Mathematique*, 348(2010), 1059-1062.
28. Karaev, M.T., On the numerical radius of some  $C_00$  contractions, *Linear Algebra and its Applications*, 431(5-7)(2009), 818-822.
29. Karaev,M.T.,Iskenderov, Numerical range and numerical radius for some operators, *Linear Algebra and its Applications*, 432(2010), 3149-3158.
30. Karaev,M.T.,Zeltser,M.,On Abel convergence of double sequences, *Numerical Functional Analysis and Optimization*, 31(2010), 1185-1190.
31. Karaev,M.T., Gürdal,M., Saltan,S., Some applications of Banach algebra techniques, *Math.Nachrishten*, 284(2011), 1678-1689.
32. Karaev, M.T., Gürdal,M., Strongly splitting weighted shift operators on Banach spaces and unicellularity, *Operators and Matrices*, 1(2011), 157-171.
33. Karaev,M.T., Domination conditions and spectral multiplicity of operators, *Acta Math.Hungarica*, 134(2012), 79-98.
34. Karaev,M.T., A characterization of some function classes, *J.Function Spaces and Applications*, ArticleID 796798, 1-5, 2012.
35. Karaev,M.T., Use of reproducing kernels and Berezin symbols technique in some questions of operator theory, *Forum Math.(to appear)*.
36. Ash,J.M., Karaev,M.T., On the boundary behavior of special classes of  $C^\infty$ - functions and analytic functions, *International Math.Forum*.7(2012), n.4., 153 -166.
37. Chalendar,I.,Fricain,E.,Gürdal,M.,and Karaev M.T., Compactness and Berezin symbols, *Acta Sci.Math.(Szeged)*, 78 (2012), no. 1-2, 315–329.
- 38.Gürdal, Mehmet; Garayev, Mübariz T.; Saltan, Suna Some concrete operators and their properties. *Turkish J. Math.* 39 (2015), no. 6, 970–989.
- 39.Guediri, Hocine; Garayev, Mubariz T.; Sadraoui, Houcine The Bergman space as a Banach algebra. *New York J. Math.* 21 (2015), 339–350
- 40.Garayev, Mubariz T. Two applications of the Nordgren-Rosenthal theorem. *Numer. Funct. Anal. Optim.* 36 (2015), no. 7, 856–866
- 41.Gürdal, Mehmet; Garayev, Mübariz T.; Saltan, Suna; Yamancı, Ulaşdist -formulas and Toeplitz operators. *Ann. Funct. Anal.* 6 (2015), no. 1, 221–226.
- 42.Gürdal, M.; Garayev, M. T.; Saltan, S.; Yamancı, U. On some numerical characteristics of operators. *Arab J. Math. Sci.* 21 (2015), no. 1, 118–126.
- 43.Karaev, Mubariz T.; Saltan, Suna; Kunt, Tevfik Discrete Duhamel product, restriction of weighted shift operators and related problems. *New York J. Math.* 20 (2014), 831–843.

- 44.Gürdal, M.; Garayev, M. T.; Saltan, S.Basisity problem and weighted shift operators.*Acta4Math. Sci. Ser. B Engl. Ed.*34 (2014), no. 5, 1655–1660.
- 45.Karaev, Mubariz T.; Gürdal, Mehmet; Yamancı, Ulaş Some results related with Berezin symbols and Toeplitz operators. *Math. Inequal. Appl.*17 (2014), no. 3, 1031–1045
- 46.Karaev, Mubariz T. Erratum: Use of reproducing kernels and Berezin symbols technique in some questions of operator theory [Forum Math., DOI 10.1515/FORM.2011.073]]. *Forum Math.*25 (2013), no. 5, 1107.
- 47.Karaev, M. T. Reproducing kernels and Berezin symbols techniques in various questions of operator theory. *Complex Anal. Oper. Theory*7 (2013), no. 4, 983–1018.
- 48.Karaev, Mubariz T.Tauberian-type theorem for (e) -convergent sequences. *C. R. Math. Acad. Sci. Paris*351 (2013), no. 5-6, 177–179
- 49.Karaev, Mubariz T.; Iskenderov, Nizameddin Sh.Berezin number of operators and related questions. *Methods Funct. Anal. Topology*19 (2013), no. 1, 68–72
- 50.Karaev, Mübariz Tapdigoğlu; Gürdal, Mehmet; Yamancı, Ulaş Special operator classes and their properties. *Banach J. Math. Anal.*7 (2013), no. 2, 74–85.
51. Gürdal, M., Yamancı, U., and Garayev, M., Some results for operators on a model space, *Frontiers of Mathematics in China*, 13 (2018), no. 2, 287-300.
52. Altwajry, N., Baazeem, A.S., and Garayev, M., Distance estimates, norm of Hankel operators and related questions, *Operators and Matrices*, 12 (2018) no. 1, 157--168.
53. Karaev, M.T., Duhamel Algebras and Applications, *Funktional. Anal. i Prilozhen.*, 52 (2018), no. 1, 3–12.
55. Garayev, M.T., Gürdal, M. and TilkiHavva, On some Deddens subspaces of Banach algebras, *Filomat*, in press, 2018.
56. Gürdal M. and Garayev, M.T., Remarks on the zero Toeplitz product problem in the Bergman and Hardy spaces, *Turkish journal of Mathematics*, in press, 2018.
57. Garayev, Mubariz T. Berezin symbols, Hölder-McCarthy and Young inequalities and their applications. *Proc. Inst. Math. Mech. Natl. Acad. Sci. Azerb.* 43 (2017), no. 2, 287--295.
58. Garayev, Mubariz T.; Gürdal, Mehmet; Saltan, Suna Hardy type inequaltiy for reproducing kernel Hilbert space operators and related problems. *Positivity* 21 (2017), no. 4, 1615--1623.
59. Garayev, M. T.; Gürdal, M.; Yamancı, U. Berezin symbols and Borelsummability. *Quaest. Math.* 40 (2017), no. 3, 403--411.
60. Yamancı, U., Gürdal, M. and Garayev, M. T., Berezin Number Inequality for Convex Function in Reproducing Kernel Hilbert Space, *Filomat*, 31 (2017), no. 18, 5711--5717.
61. Garayev, Mubariz T.; Gürdal, Mehmet; Yamancı, Ulaş Description of Bloch spaces, weighted Bergman spaces and invariant subspaces, and related questions. *Kuwait J. Sci.* 43 (2016), no. 3, 70--77.

62. Gürdal, Mehmet; Garayev, Mübariz T.; Değer, HasretBerezin symbols and Abel convergence of sequences and series. Proc. Rom. Acad. Ser. A Math. Phys. Tech. Sci. Inf. Sci. 17 (2016), no. 3, 203--209.
63. Garayev, M. T.; Guediri, H.; Sadraoui, H. On some problems in the space  $C(n)[0,1]$ . Politehn. Univ. Bucharest Sci. Bull. Ser. A Appl. Math. Phys. 78 (2016), no. 1, 147--156.
64. Garayev, Mubariz T.; Gürdal, Mehmet; Okudan, Arzu Hardy-Hilbert's inequality and power inequalities for Berezin numbers of operators. Math. Inequal. Appl. 19 (2016), no. 3, 883--891.
65. Garayev, Mubariz T.; Guediri, Hocine; Sadraoui, Houcine Applications of reproducing kernels and Berezin symbols. New York J. Math. 22 (2016), 583--604.
66. Karaev, Mubariz T.; Gürdal, Mehmet; Huban, MuallaBirgül Reproducing kernels, English algebras and some applications. Studia Math. 232 (2016), no. 2, 113--141.
67. Gürdal, Mehmet; Garayev, Mübariz T.; Saltan, SunaSome concrete operators and their properties. Turkish J. Math. 39 (2015), no. 6, 970--989.
68. Garayev, Mubariz T. The Berezin number, norm of a Hankel operator and related topics. Operator algebras and mathematical physics, 87--100, Oper. Theory Adv. Appl., 247, Birkhäuser/Springer, Cham, 2015.
69. Guediri, Hocine; Garayev, Mubariz T.; Sadraoui, HoucineThe Bergman space as a Banach algebra. New York J. Math. 21 (2015), 339--350.
70. Garayev, Mubariz T. Two applications of the Nordgren-Rosenthal theorem. Numer. Funct. Anal. Optim. 36 (2015), no. 7, 856--866.
71. Gürdal, Mehmet; Garayev, Mübariz T.; Saltan, Suna; Yamancı, Ulaşdist-formulas and Toeplitz operators. Ann. Funct. Anal. 6 (2015), no. 1, 221--226.
72. Gürdal, M.; Garayev, M. T.; Saltan, S.; Yamancı, U. On some numerical characteristics of operators. Arab J. Math. Sci. 21 (2015), no. 1, 118--126.
73. M.T.Karaev, Duhamel algebras and applications, *Funct. Anal. Applications*, 2018.
74. M.T.Garayev, H.Guediri and H.Sadraoui, New characterizations of Bloch spaces, Bers-type and Zygmund-type spaces and related questions, *Ufa Math.J.*, 10(2018), 131-141.
75. M.T.Garayev, M.Gurdal, U.Yamancı, B.Halouani, Boundary behavior of Berezin symbols and related results, *Filomat*, 33:14(2019), 4433-4440.
76. F.Bouzeffour, M.T.Garayev, Duhamel convolution product in the setting of quantum calculus, *Ramanujan J.*, 46(2018), 345-356.
77. M.T.Garayev, U.Yamancı, Cebysev type inequalities and power inequalities for the Berezin number of operators, *Filomat*, 33:8(2019), 2307-2316.
78. Ulaş Yamancı, Mubariz T. Garayev and Ceren Çelik ,Hardy–Hilbert type inequality in reproducing kernel Hilbert space: its applications and related results, *LINEAR AND MULTILINEAR ALGEBRA* 2019, VOL. 67, NO. 4, 830-842.
79. M.T.Garayev, H.Guediri, M.Gurdal, G.Alsahli, On some problems for operators on the reproducing kernel Hilbert space, *LINEAR AND MULTILINEAR ALGEBRA*  
<https://doi.org/10.1080/03081087.2019.1659220>

80. M.T. GARAYEV , M. GURDAL , Remarks on the zero Toeplitz product problem in the Bergman and Hardy spaces,42(2018),1504-1508.

81. M. Bakherad and M.T. Garayev, Berezin number inequalities for operators,6(2019),33-43.

## Very recent publications :

- On the Essential Norm Formulas for Some Operators 2023  
MT Garayev  
Complex Analysis and Operator Theory 17 (2), 23
- Some applications of the -Duhamel product 2022  
M Gürdal, M Garayev, R Tapdigoglu, M Altıntaş  
The Journal of Analysis, 1-16
- On the fractional Bessel operator 2022  
F Bouzeffour, M Garayev  
Integral Transforms and Special Functions 33 (3), 230-246
- On some problems for reproducing Kernel Hilbert space operators via the Berezin transform 2022  
MT Karaev, R Tapdigoglu  
Mediterranean Journal of Mathematics 19, 1-16
- Berezin symbol inequalities via Grüss type inequalities and related questions 2022  
R TAPDIGOĞLU, M GARAYEV, N Altwaijry  
Turkish Journal of Mathematics 46 (3), 991-1003
- On hyponormality of Toeplitz operators 2021  
H Sadraoui, M Garayev, H Guediri  
Rocky Mountain Journal of Mathematics 51 (5), 1821-1831
- Reverse inequalities for the Berezin number of operators 2021  
M Garayev, H Guediri, N Altwaijry  
arXiv preprint arXiv:2109.09012
- On some problems for operators on the reproducing kernel Hilbert space 2021  
MT Garayev, H Guediri, M Gürdal, GM Alsahli  
Linear and Multilinear Algebra 69 (11), 2059-2077
- Inequalities for the Berezin number of operators and related questions 2021  
MT Garayev, MW Alomari  
Complex Analysis and Operator Theory 15, 1-30
- Fractional supersymmetric quantum mechanics and lacunary Hermite polynomials 2021  
F Bouzeffour, M Garayev  
Analysis and Mathematical Physics 11, 1-16
- The Hartley Transform Via Susy Quantum Mechanics 2021  
F Bouzeffour, M Garayev  
Memoirs on Differential Equations and Mathematical Physics 83, 31-41
- Some applications of Berezin θ-sequences and Berezin symbols 2021  
N Altwaijry, M Garayev, A Baazeem  
Filomat 35 (11), 3703-3712
- On hyponormality on a weighted annulus 2021

- Multiple big -Jacobi polynomials 2020  
F Bouzeffour, M Garayev  
Bulletin of Mathematical Sciences 10 (02), 2050013
- Hyponormality on a Weighted Bergman Space 2020  
H Sadraoui, B Halouani, MT Garayev, A AlShehri  
Journal of Function Spaces 2020, 1-7
- A generalization of the 2D Slepian functions 2020  
F Bouzeffour, M Garayev  
Mathematical Methods in the Applied Sciences
- Some inequalities involving Berezin symbols of operator means and related questions 2020  
M Garayev, S Saltan, F Bouzeffour, B Aktan  
Revista de la Real Academia de Ciencias Exactas, Físicas y Naturales.  
Serie ...
- Extended arithmetic functions 2020  
F Bouzeffour, W Jedidi, M Garayev  
The Ramanujan Journal 51, 593-609
- On the Zeros of the Big  $q$ -Bessel Functions and Applications 2020  
F Bouzeffour, H Ben Mansour, M Garayev  
Mathematics 8 (2), 237
- Refinements of Kantorovich type, Schwarz and Berezin number inequalities 2020  
M Garayev, F Bouzeffour, M Gürdal, CM Yangoz  
Extracta mathematicae 35 (1), 1-20
- Skew-symmetric and essentially unitary operators via Berezin symbols 2020  
N Altwaijry, M Garayev, H Guediri, A Baazeem  
Open Mathematics 18 (1), 1760-1770
- Hardy–Hilbert type inequality in reproducing kernel Hilbert space: its applications and related results 2019  
U Yamancı, MT Garayev, C Çelik  
Linear and Multilinear Algebra 67 (4), 830-842
- Some properties and applications of convolution algebras 2019  
MT Garayev  
Adv. Mathem. Models Appl 4 (3), 188-197
- Čebyšev's type inequalities and power inequalities for the Berezin number of operators 2019  
MT Garayev, U Yamancı  
Filomat 33 (8), 2307-2316
- Boundary behavior of Berezin symbols and related results 2019  
MT Garayev, M Gürdal, U Yamancı, B Halouani  
Filomat 33 (14), 4433-4439
- Berezin number inequalities for operators 2019  
M Bakherad, MT Garayev  
Concrete Operators 6 (1), 33-43