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## Chapter 4

## Describing Data: Displaying and Exploring Data

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## Learning Objectives

LO4-1 Construct and interpret a dot plot.
LO4-2 Identify and compute measures of position.
LO4-3 Construct and analyze a box plot.
LO4-4 Compute and interpret the coefficient of skewness.
LO4-5 Create and interpret a scatter diagram.
LO4-6 Compute and interpret the correlation coefficient.
LO4-7 Develop and explain a contingency table.

## Dot Plots

Dot Plot Summarizes the distribution of one variable by stacking dots as points on a number line that shows all the values.

Display a dot for each observation.
If there are identical values, the dots are "piled" on top of each other.

- See the shape of distribution.
- Values where the data cluster.
- Good for smaller data sets.


## Dot Plots <br> 2

- Example: The number of vehicles served at two dealers.

Tionesta Ford Lincoln

| Monday | Tuesday | Wednesday | Thursday | Friday | Saturday |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 23 | 33 | 27 | 28 | 39 | 26 |
| 30 | 32 | 28 | 33 | 35 | 32 |
| 29 | 25 | 36 | 31 | 32 | 27 |
| 35 | 32 | 35 | 37 | 36 | 30 |

Sheffield Motors, Inc.

| Monday | Tuesday | Wednesday | Thursday | Friday | Saturday |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 31 | 35 | 44 | 36 | 34 | 37 |
| 30 | 37 | 43 | 31 | 40 | 31 |
| 32 | 44 | 36 | 34 | 43 | 36 |
| 26 | 38 | 37 | 30 | 42 | 33 |

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- Example continued


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## Measures of Position

The standard deviation is the most widely used measure of dispersion.
We can also determine the location of values that divide a set of observations into parts.


Quartiles: Divide a set of observations into four equal parts.

- $Q_{1}$ : Value below which $25 \%$ of the observations occur.
- $Q_{2}$ : Value below which $50 \%$ of the observations occur (median).
- $Q_{3}$ : Value below which $70 \%$ of the observations occur.


## Measures of Position

- Deciles: Divide a set of observations into 10 equal parts.
- Percentiles: Divide a set of observations into 100 equal parts.
- Let $L_{p}$ refer to the location of a desired interval.
- For $n$ observations, the $p^{t h}$ percentile is given by:

$$
L_{p}=(n+1) \frac{p}{100}
$$

- Example: The 92nd percentile would be $L_{92}$


## Measures of Position

- Example: The commissions earned last month by a sample of 15 brokers.

| $\$ 2,038$ | $\$ 1,758$ | $\$ 1,721$ | $\$ 1,637$ | $\$ 2,097$ | 42,047 | $\$ 2,205$ | $\$ 1,787$ | $\$ 2,287$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 1,940 | 2,311 | 2,054 | 2,406 | 1,471 | 1,460 |  |  |  |

- Locate the median, the first quartile and the third quartile of the commissions.
- First, sort the data from smallest to largest.

| $\$ 1,460$ | $\$ 1,471$ | $\$ 1,637$ | $\$ 1,721$ | $\$ 1,758$ | $\$ 1,787$ | $\$ 1,940$ | $\$ 2,038$ | $\$ 2,047$ |
| ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 2,054 | 2,097 | 2,205 | 2,287 | 2,311 | 2,406 |  |  |  |

## Measures of Position

- Example continued
- $Q_{1}: L_{25}=(16+1) \frac{25}{100}=4$
- Median: $L_{50}=(16+1) \frac{50}{100}=8$
- $Q_{3}: L_{75}=(n+1) \frac{75}{100}=12$
$\begin{array}{lllllllll}\$ 1,460 & \$ 1,471 & \$ 1,637 & \$ 1,721 & \$ 1,758 & \$ 1,758 & \$ 1,940 & \$ 2,038 & \$ 2,047\end{array}$ $\begin{array}{llllll}2,054 & 2,097 & 2,205 & 2,287 & 2,311 & 2,406\end{array}$
- $Q_{1}=\$ 1,721$, Median $=\$ 2,038$ and $Q_{3}=\$ 2,205$


## Box Plots 1

Box Plot A graphic display that shows the general shape of a variable's distribution. It is based on five descriptive statistics: the maximum and minimum values, the first and third quartiles, and the median.


## Box Plots

- The interquartile range is $Q_{3}-Q_{1}$
- Range of values between the first and third quartiles.
- $50 \%$ of a distribution's values.

Outlier A data point that is unusually far from the other.

- Greater than upper boundary: $Q_{3}+1.5\left(Q_{3}-Q_{1}\right)$
- Lower than lower boundary: $Q_{3}-1.5\left(Q_{3}-Q_{1}\right)$
- Marked as asterisks beyond last value less than the boundary.
- Nor outliers: minimum or maximum should be the end lines.


## Box Plots

- Example: The Applewood Auto Group data and the buyer age variable.


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## Skewness

- There are four common shapes.


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## SKEMMESS

Pearson: $s_{k}=\frac{3(\bar{x}-\text { Median })}{s}$

- Between -3 and 3 .
- Near -3: considerable negative skewness.
- Near 0: symmetric.
- Near 3: considerable positive skewness.

Software skewness: $\quad s_{k}=\frac{n}{(n-1)(n-2)}\left[\sum\left(\frac{x-\bar{x}}{s}\right)^{3}\right]$

- Focus on the brackets with the mean and standard deviation.
- Called standardizing (discussed later).
- Values are larger than the mean: positive and skewed right.
- Values are less than the mean: negative and skewed left.


## Skewness

- Example: The earnings per share for software companies.

| $\$ 0.09$ | $\$ 0.13$ | $\$ 0.41$ | $\$ 0.51$ | $\$ 1.12$ | $\$ 1.20$ | $\$ 1.49$ | $\$ 3.18$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 3.50 | 6.36 | 7.83 | 8.92 | 10.13 | 12.99 | 16.40 |  |

- Compute the mean, median, and standard deviation.
- Find the coefficient of skewness using Pearson's estimate and the software methods.
- What is your conclusion regarding the shape of the distribution?


## SKEMMESS

- Example continued
- Mean: $\bar{x}=\$ 4.95$;

Median: the middle value of $\$ 3.18$

- Standard deviation: $s=\$ 5.22$.
- $s_{k}=\frac{n}{(n-1)(n-2)}\left[\sum\left(\frac{x-\bar{x}}{3}\right)^{3}\right]$

$$
\begin{aligned}
& =\frac{15}{(15-1)(15-2)}(11.8274) \\
& =0.975
\end{aligned}
$$

- Skewed right.
- Note the mean > median.

| Earnings per <br> Share | $\left(x-x^{-}\right) \div s$ | $\left(\left(x-x^{-}\right) \div s\right)^{3}$ |
| :---: | ---: | ---: |
| 0.09 | -0.9310 | -0.8070 |
| 013 | -0.9234 | -0.7873 |
| 0.41 | -0.8697 | -0.6579 |
| 0.51 | -0.8506 | -0.6154 |
| 1.12 | -0.7337 | -0.3950 |
| 1.20 | -0.7184 | -0.3708 |
| 1.49 | -0.6628 | -0.2912 |
| 3.18 | -0.3391 | -0.0390 |
| 3.50 | -0.2778 | -0.0214 |
| 6.36 | 0.2701 | 0.0197 |
| 7.83 | 0.5517 | 0.1679 |
| 8.92 | 0.7605 | 0.4399 |
| 10.13 | 0.9923 | 0.9772 |
| 12.99 | 1.5402 | 3.6539 |
| 16.40 | 2.1935 | 10.5537 |
|  |  | 11.8274 |

## Skewness



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## Describing the Relationship Between Two Variables

Scatter Diagram Graphical technique used to show the relationship between two variables measured with interval or ratio scales.

- Study the relationship between two variables (bivariate).
- Usually one variable on the other.



## Describing the Relationship Between Two Variables

Compute a statistic called the correlation coefficient.
Measures the direction and strength of the relationship.

$$
r=\frac{\sum(x-\bar{x})(y-\bar{y})}{(n-1) s_{y} s_{x}}
$$

- Ranges from -1.0 to +1.0 .
- The closer the coefficient is to -1.0 or +1.0 , the stronger the relationship.
- If $r$ is close to 0.0 , we can say that there is no relationship between the variables.
- Positive indicates a positive relationship.
- Negative indicates a negative relationship.


## Describing the Relationship Between Two Variables




## Describing the Relationship Between Two Variables



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## Describing the Relationship Between Two Variables

- Example: The relationship between vehicle profit and age.
- The correlation is 0.26 .


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## Contingency Tables

Contingency Table A table used to classify observations according to two identifiable characteristics.

- It is a cross-tabulation that simultaneously summarizes two variables of interest.
- Both variables need only be nominal or ordinal.


## Contingency Tables

- Example: The profit for four dealerships.

Contingency Table Showing the Relationship between Profit and Dealership

| Above/Below <br> Median Profit | Kane | Olean | Sheffield | Tionesta | Total |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Above | 25 | 20 | 19 | 26 | 90 |
| Below | 27 | 20 | 26 | 17 | 30 |
| Total | 52 | 40 | 45 | 43 | 180 |

## Chapter 4 Practice Problems

## Question 3

Consider the following chart.

a. What is this chart called?
b. How many observations are in the study?
c. What are the maximum and the minimum values?
d. Around what values do the observations tend to cluster?

## Question 7

The Thomas Supply Company Inc. is a distributor of gaspowered generators. As with any business, the length of time customers take to pay their invoices is important. Listed below, arranged from smallest to largest, is the time, in days, for a sample of the Thomas Supply Company Inc. invoices.

| 13 | 13 | 13 | 20 | 26 | 27 | 31 | 34 | 34 | 34 | 35 | 35 | 36 | 37 | 38 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 41 | 41 | 41 | 45 | 47 | 47 | 47 | 50 | 51 | 53 | 54 | 56 | 62 | 67 | 82 |

a. Determine the first and third quartiles.
b. Determine the second decile and the eighth decile.
c. Determine the 67th percentile.

## Question 9

The box plot below shows the amount spent for books and supplies per year by students at four-year public colleges.

a. Estimate the median amount spent.
b. Estimate the first and third quartiles for the amount spent.
c. Estimate the interquartile range for the amount spent.
d. Beyond what point is a value considered an outlier?
e. Identify any outliers and estimate their values.
f. Is the distribution symmetrical or positively or negatively skewed?

## Question 15

Listed below are the commissions earned (\$000) last year by the 15 sales representatives at Furniture Patch Inc.

```
$3.9 $5.7 $7.3 $10.6 $13.0
17.4
```

a. Determine the mean, median, and the standard deviation.
b. Determine the coefficient of skewness using Pearson's method.
c. Determine the coefficient of skewness using the software method.

## Question 17

Create a scatter diagram and compute a correlation coefficient. How would you describe the relationship between the values?

| $x$-Value | $y$-Value | $x$-Value | $y$-Value |
| :---: | :---: | :---: | :---: |
| 10 | 6 | 11 | 6 |
| 8 | 2 | 10 | 5 |
| 9 | 6 | 7 | 2 |
| 11 | 5 | 7 | 3 |
| 13 | 7 | 11 | 7 |

## Question 19

The Director of Planning for Devine Dining Inc. wishes to study the relationship between the time of day a customer dined and whether the guest orders dessert. To investigate the relationship, the manager collected the following information on 200 recent customers.
a. What is the level of measurement of the two variables?

| Time of Day |  |  |  |
| :--- | ---: | ---: | ---: |
| Dessert Ordered | Lunch | Dinner | Total |
| Yes | 32 | 85 | 117 |
| No | $\underline{68}$ | $\underline{15}$ | $\underline{83}$ |
| Total | 100 | 100 | 200 |

b. What is the above table called?
c. Does the data suggest that customer are more likely to order dessert? Explain why.
d. Does the data suggest that customers at lunch time are more likely to order dessert? Explain why.
e. Does the data suggest that customers at dinner time are more likely to order dessert? Explain why.

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