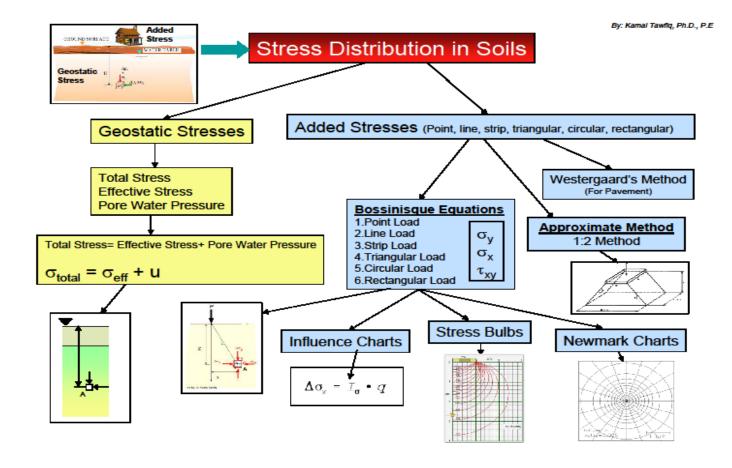
# CHAPTER 9 IN SITU STRESSES

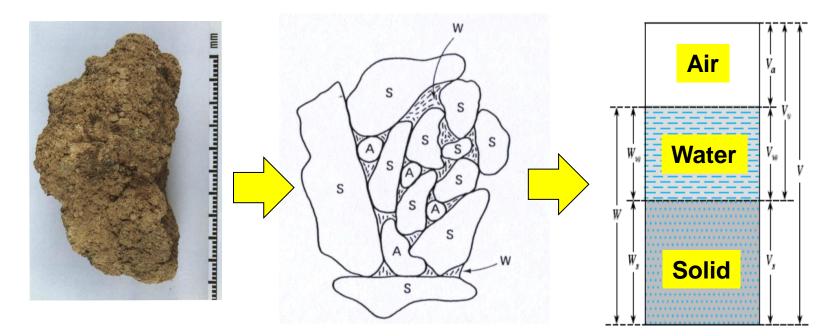
# **IN SITU STRESSES**

- **Concept of effective stress**
- Stresses in saturated soil without seepage, upward seepage, and downward seepage
- Seepage force per unit volume of soil
- Conditions for *heaving* or boiling for seepage under a hydraulic structure
- Use of filter to increase the stability against heaving or boiling
- **Effective stress in partially saturated soil**

# **TYPES OF STRESSES IN SOIL**



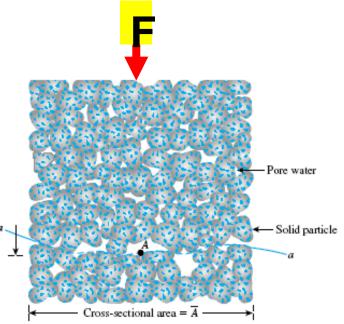
• Soils are multiphase systems. They consists of solid particles enclosing continuous voids which contain water and/or air.



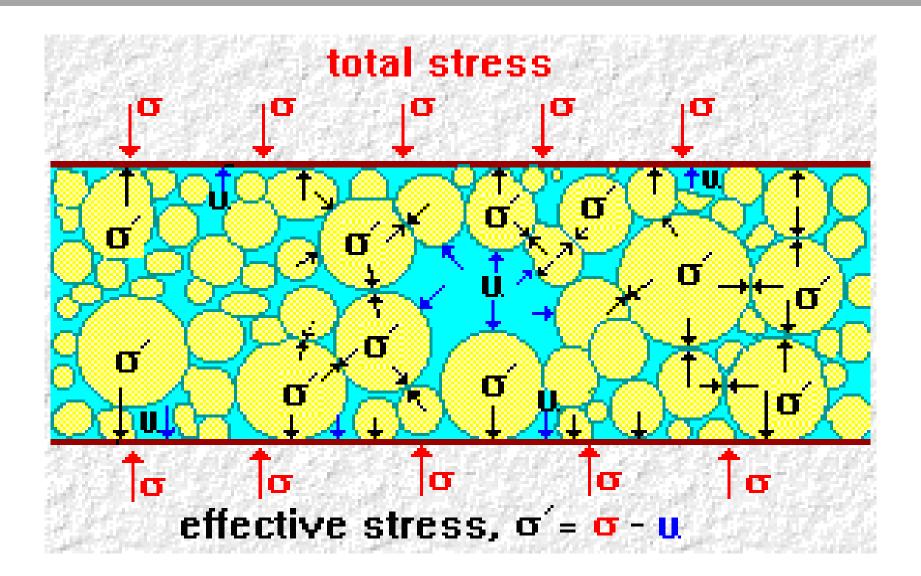
 When an external load is applied to soil it will be carried jointly by the <u>three systems</u>, solid, water, air.

- However, it is difficult, if not impossible to analyze such multiphase system.
- When the soil is fully saturated, then only water is presented in the voids and the problem becomes relatively simple.
- When an external load is applied to saturated soil it will be carried jointly by the <u>two systems</u>, solid grains and water in the pores.
- The increase in pressure within the pore water causes drainage (flow out of the soil), and the load is transferred to the solid grains.
- The rate of drainage depends on the permeability of the soil.

- If by any mean we can find the part of the load carried by the water for a given external load, then we can find the part carried by the solids.
- This is the theme of the <u>Principle of Effective</u> <u>Stress</u>. In other word the principle of effective stress determines the effect of a pore pressure on the behavior of a soil with a given TOTAL STRESS.



- It is probably <u>the single most important concept</u> in soil mechanics and geotechnical engineering.
- The compressibility and shearing resistance of a soil depend to a great extent on the effective stress.



### **STRESSES IN SATURATED SOILS**

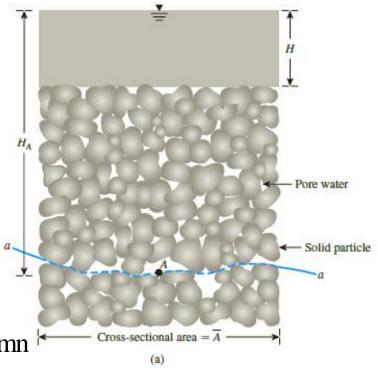
$$\sigma = H\gamma_w + (H_A - H)\gamma_{sat}$$

 $\sigma$  = Total stress @ the elevation of point A

 $\gamma_W$  = Unit weight of water

 $\gamma_{sat}$  = Saturated unit weight of the soil

- H = Height of water table from the top of soil column
- $H_A$  = Distance between point A and the water table



Cross-sectional area =

### **STRESSES IN SATURATED SOILS**

$$\sigma = \sigma' + u$$

 $\sigma$  = Total normal stress  $\sigma'$  = Effective normal stress u = Pore water pressure

The total stress can be divided into two parts:

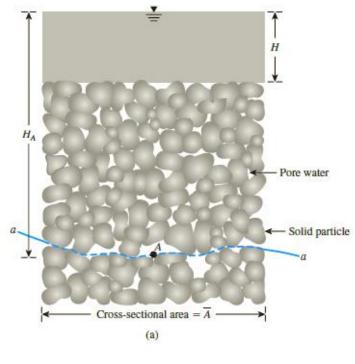
- 1. A portion is carried by water in the continuous void spaces. This portion acts with equal intensity in all directions.
- 2. The rest of the total stress is carried by the soil solids at their points of contact. The sum of the vertical components of the forces developed at the points of contact of the solid particles per unit cross-sectional area of the soil mass is called the *effective stress*.

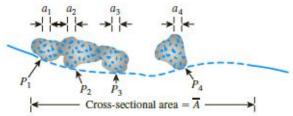
### THE PRINCIPLE OF EFFECTIVE STRESS

 $\sigma = \sigma' + u$   $\sigma' = \sigma - u$   $\sigma' = [H\gamma_w + (H_A - H)\gamma_{sat}] - H_A\gamma_w$   $\sigma' = (H_A - H)(\gamma_{sat} - \gamma_w)$  $\sigma' = (\text{Height of soil column}) \times \gamma'$ 

 $\gamma'$  = Submerged unit weight of the soil  $\sigma'$  = Effective stress at point A

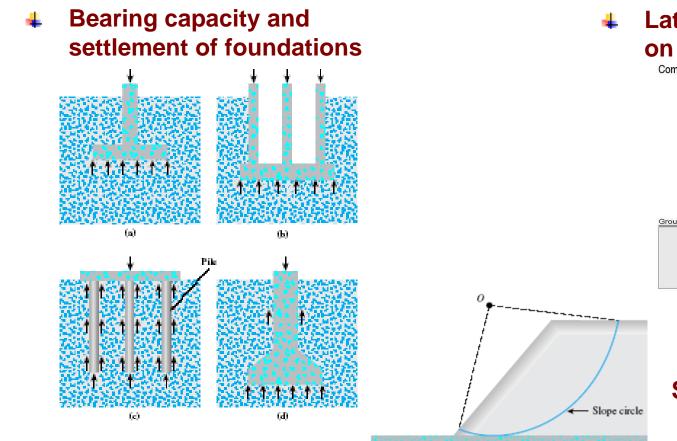
u = Pore water pressure at point A (Neutral stress)



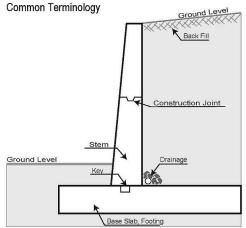


## THE PRINCIPLE OF EFFECTIVE STRESS

• The concept of effective stress is significant in solving geotechnical engineering problems, such as:



#### Lateral earth pressure on retaining structures



#### **Stability of earth slopes**

# **EVALUATION OF EFFECTIVE STRESS**

- We now know the importance of effective stress and that it is responsible for soil behavior and the dilemma that we cannot measure it.
- However, if we can find σ and *u*, then

$$\sigma' = \sigma - u \qquad (*)$$

**L** Therefore, our job now is to find  $\sigma$  and **u**.

I. Determination of total stress, σ

Where 
$$\sigma = \gamma . z$$
 (\*\*)

 $\gamma$  = Unit weight of the soil, the unit weight of the soil may be, wet, saturated, dry. (This depends on the degree of saturation of soil).

z = The vertical distance from the surface to the point at which  $\sigma$  is evaluated.

### **EVALUATION OF EFFECTIVE STRESS**

#### II. Determination of p.w.p, u

$$u = \gamma_w.z \qquad (***)$$

#### Where

 $\gamma_w$  = Unit weight of water

Therefore, by substituting Eq. (\*\*) and Eq.(\*\*\*) into Eq.(\*), we get

$$\sigma' = (\gamma - \gamma_w)z$$

# **HYDROSTATIC PRESSURE**

- The pressure exerted by water at a given point within the soil medium, due to the force of gravity.
- Hydrostatic pressure increases in proportion to depth measured from the surface because of the increasing weight of fluid exerting downward force from above.
- The level in the ground at which the pore pressure is zero (equal to atmospheric) is defined as the <u>water table</u> or <u>phreatic surface</u>.
- When there is no flow, the water surface will be at exactly the same level in any stand pipe placed in the ground below the water table.
- This is called a hydrostatic pressure condition.
- Pore water pressure (sometimes abbreviated to pwp) refers to the pressure of groundwater held within a soil or rock, in gaps between particles (pores).

#### STRESSES IN SATURATED SOILS WITHOUT UPWARD SEEPAGE

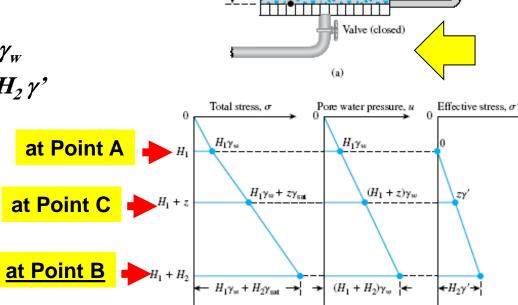
#### At point A,

- Total Stress:  $\sigma_A = H_1 \gamma_w$
- Pore water pressure:  $u_A = H_1 \gamma_w$
- Effective stress:  $\sigma'_A = \theta$

#### At point B,

- Total Stress:  $\sigma_B = H_1 \gamma_w + H_2 \gamma_{sat}$
- Pore water pressure:  $u_B = (H_1 + H_2) \gamma_w$

• Effective stress: 
$$\sigma'_B = H_2(\gamma_{sat} - \gamma_w) = H_2 \gamma'$$



(b)

Depth

(c)

Depth

(d)

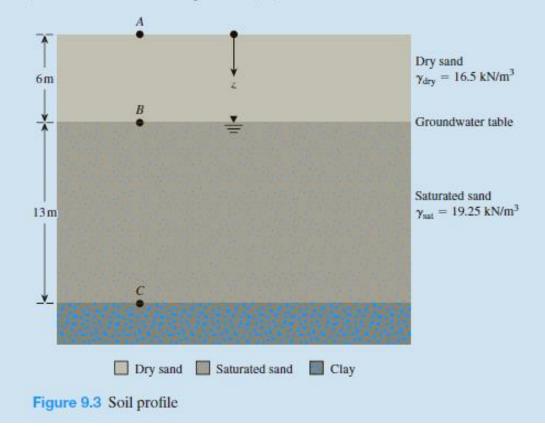
Depth

#### <u>At point C,</u>

- Total Stress:  $\sigma_C = H_1 \gamma_w + z \gamma_{sat}$
- Pore water pressure:  $u_C = (H_1 + z) \gamma_w$
- Effective stress:  $\sigma'_C = z(\gamma_{sat} \gamma_w) = z \gamma'$

#### Example 9.1

A soil profile is shown in Figure 9.3. Calculate the total stress, pore water pressure, and effective stress at points A, B, and C.



#### Solution

At Point A,

Total stress:  $\sigma_A = 0$ Pore water pressure:  $u_A = 0$ Effective stress:  $\sigma'_A = 0$ 

At Point B,

$$\sigma_B = 6\gamma_{dry(sand)} = 6 \times 16.5 = 99 \text{ kN/m}^2$$
$$u_B = 0 \text{ kN/m}^2$$
$$\sigma'_B = 99 - 0 = 99 \text{ kN/m}^2$$

At Point C,

$$\sigma_{C} = 6\gamma_{dry(sand)} + 13\gamma_{sat(sand)}$$
  
= 6 × 16.5 + 13 × 19.25  
- 99 + 250.25 - **349.25 kN/m<sup>2</sup>**  
 $u_{C} = 13\gamma_{w} = 13 \times 9.81 = 127.53 \text{ kN/m2}$   
 $\sigma_{C}' = 349.25 - 127.53 = 221.72 \text{ kN/m2}$ 

#### Example 9.2

Refer to Example 9.1. How high should the water table rise so that the effective stress at C is 190 kN/m<sup>2</sup>? Assume  $\gamma_{sat}$  to be the same for both layers (i.e., 19.25 kN/m<sup>2</sup>).

#### Solution

Let the groundwater table rise be h above the present groundwater table shown in Figure 9.3 with

$$\sigma_{c} = (6 - h)\gamma_{dry} + h\gamma_{sat} + 13\gamma_{sat}$$
$$u = (h + 13)\gamma_{w}$$

So

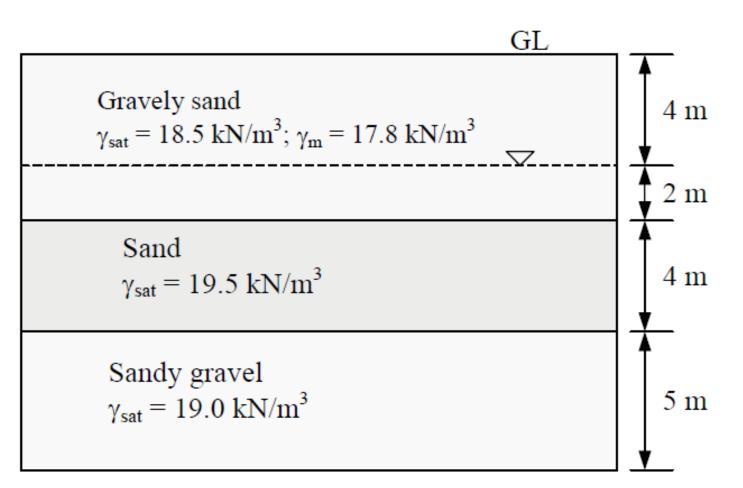
$$\begin{aligned} r_c' &= \sigma_c - u = (6 - h)\gamma_{dry} + h\gamma_{sat} + 13\gamma_{sat} - h\gamma_w - 13\gamma_w \\ &= (6 - h)\gamma_{dry} + h(\gamma_{sat} - \gamma_w) + 13(\gamma_{sat} - \gamma_w) \end{aligned}$$

or

$$190 = (6 - h)16.5 + h(19.25 - 9.81) + 13(19.25 - 9.81)$$
$$h = 4.49 \text{ m}$$



Plot the variation of total, effective vertical stresses, and pore water pressure with depth for the soil profile shown below.



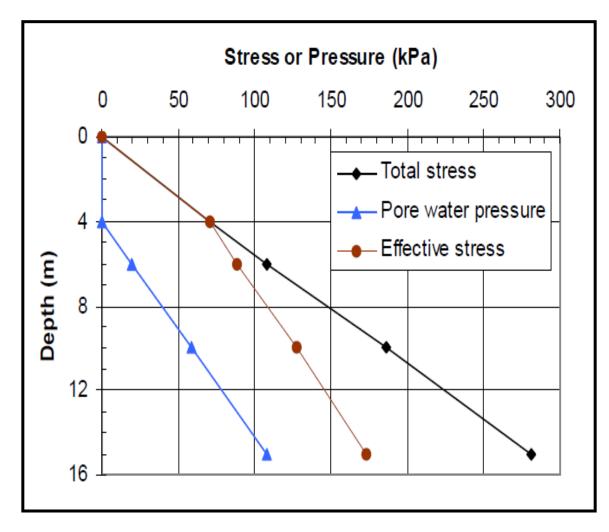


### **Solution**

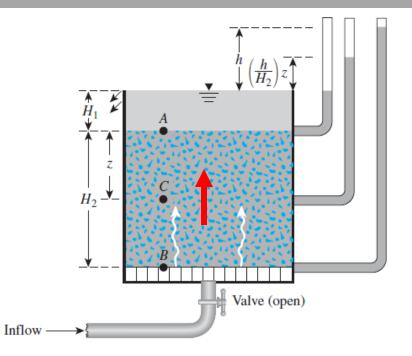
	GL	
At the ground level, $\sigma_v = 0$ ; $\sigma_v' = 0$ ; and u=0	Gravely sand $\gamma_{sat} = 18.5 \text{ kN/m}^3; \gamma_m = 17.8 \text{ kN/m}^3$	<b>4</b> m
At 4 m depth,	¥	<b>1</b> 2 m
$\sigma_v = (4)(17.8) = 71.2 \text{ kPa}; u = 0$ $\therefore \sigma_v' = 71.2 \text{ kPa}$	Sand $\gamma_{sat} = 19.5 \text{ kN/m}^3$	4 m
At 6 m depth,		<b>→</b>
$\sigma_v = (4)(17.8) + (2)(18.5) = 108.2 \text{ kPa}$ u = (2)(9.81) = 19.6  kPa $\therefore \sigma_v' = 108.2 - 19.6 = 88.6 \text{ kPa}$	Sandy gravel $\gamma_{sat} = 19.0 \text{ kN/m}^3$	5 m
At 10 m depth, $\sigma_v = (4)(17.8) + (2)(18.5) + (4)(19.5) = 18$ u = (6)(9.81) = 58.9 kPa $\therefore \sigma_v' = 186.2 - 58.9 = 127.3$ kPa	86.2 kPa	
At 15 m depth, $\sigma_v = (4)(17.8) + (2)(18.5) + (4)(19.5) + (5)(110)(10)(10)(10)(10)(10)(10)(10)(10)(1$	5)(19.0) = 281.2 kPa	



#### **Solution**



## **UPWARD SEEPAGE**

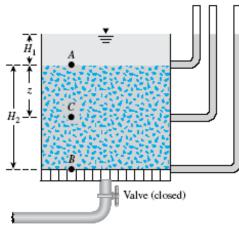


# So we directly can apply $u = \gamma_w h_p$

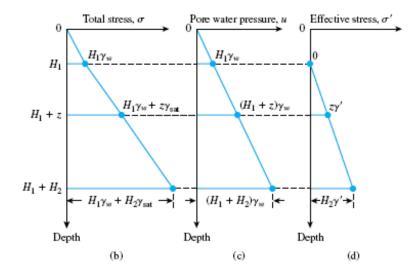
$$u_{A} = \gamma_{w}h_{p} = \gamma_{w}H_{1}$$
$$u_{B} = \gamma_{w}h_{p} = \gamma_{w}(H_{2} + H_{1} + h)$$
$$u_{c} = \gamma_{w}h_{p} = \gamma_{w}(z + H_{1} + \frac{h}{H_{2}}z)$$

### **ONE-DIMENSIONAL FLOW**

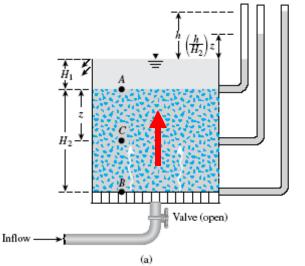
#### WITHOUT SEEPAGE

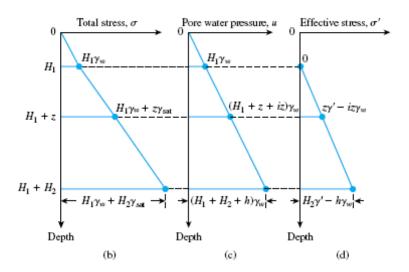






#### **UPWARD SEEPAGE**



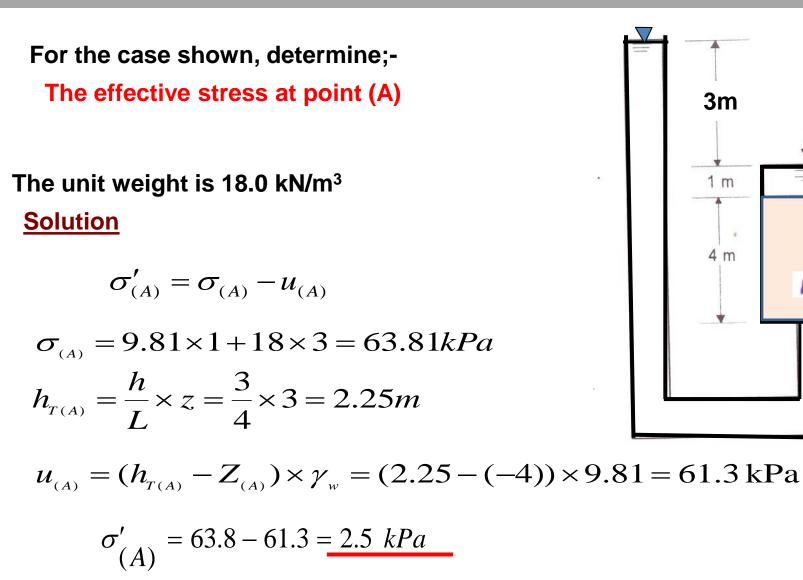




Datum

1 m

A.

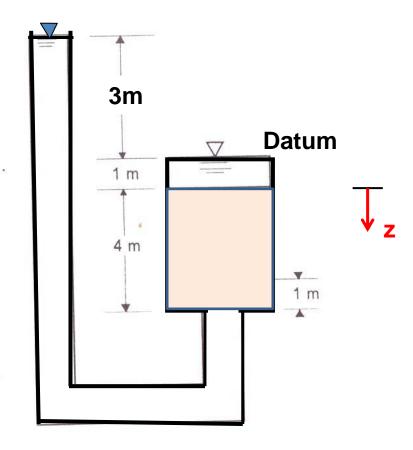




# We can apply the following equation directly

$$\sigma_c'=z\gamma'-iz\gamma_w$$

$$\sigma'_{(A)} = 3 \times (18 - 9.81) - \frac{3}{-} \times 3 \times 9.81 = 2.5 \ kPa$$



# **Quick Condition (Boiling)**

For the case of upward seepage, what happen if the hydraulic gradient gradually increased. At a certain value of hydraulic gradient the effective stress  $\sigma'$  will be zero (Note that  $\sigma'$  cannot be less than zero).

$$\sigma_{c}' = z\gamma' - iz\gamma_{w}$$

$$i_{c} = \frac{\gamma'}{\gamma_{w}}$$

- *i<sub>c</sub>* is called the <u>CRITICAL HYDRAULIC GRADIENT</u>. It is the value of *i* when a quick condition occurs.
- Recall that

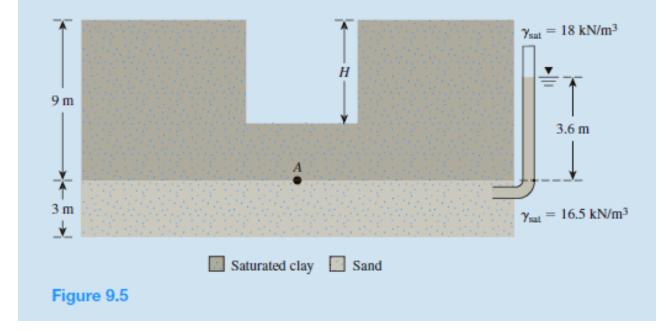
$$\gamma' = \gamma_{sub} = \frac{G_s - 1}{1 + e} \gamma_w$$

Note: fully saturated soil

$$i_c = \frac{G_s - 1}{1 + e}$$

#### Example 9.3

A 9-m-thick layer of stiff saturated clay is underlain by a layer of sand (Figure 9.5). The sand is under artesian pressure. Calculate the maximum depth of cut H that can be made in the clay.



#### Solution

Due to excavation, there will be unloading of the overburden pressure. Let the depth of the cut be H, at which point the bottom will heave. Let us consider the stability of point A at that time:

$$\sigma_A - (9 - H)\gamma_{\text{sat(clay)}}$$
$$u_A = 3.6\gamma_w$$

For heave to occur,  $\sigma'_A$  should be 0. So

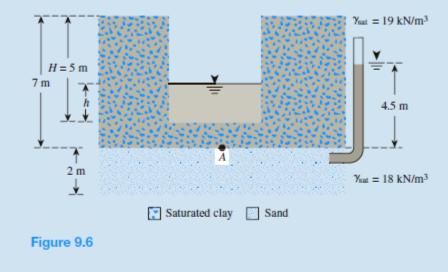
$$\sigma_A - u_A = (9 - H)\gamma_{\rm sat(clay)} - 3.6\gamma_w$$

or

$$(9 - H)18 - (3.6)9.81 = 0$$
  
$$H = \frac{(9)18 - (3.6)9.81}{18} = 7.04 \text{ m}$$

#### Example 9.4

A cut is made in a stiff, saturated clay that is underlain by a layer of sand (Figure 9.6). What should be the height of the water, h, in the cut so that the stability of the saturated clay is not lost?



#### Solution

At point A,

 $\sigma_A = (7 - 5)\gamma_{\text{sat(clay)}} + h\gamma_w = (2)(19) + (h)(9.81) = 38 + 9.81h \text{ (kN/m}^2)$  $u_A = 4.5\gamma_w = (4.5)(9.81) = 44.15 \text{ kN/m}^2$ 

For loss of stability,  $\sigma_A' = 0$ . So,

$$\sigma_A - u_A = 0$$
  
38 + 9.81h - 44.15 = 0  
h = 0.63 m

# **DOWNWARD SEEPAGE**

#### At A,

- Total Stress:  $\sigma_A = H_1 \gamma_w$
- Pore water pressure:  $u_A = H_1 \gamma_w$
- Effective stress:  $\sigma'_A = \sigma_A uA = \theta$

#### At B,

- Total Stress:  $\sigma_B = H_1 \gamma_w + H_2 \gamma_{sat}$
- Pore water pressure:  $u_B = (H_1 + H_2 h) \gamma_w$
- Effective stress:  $\sigma'_B = H_2(\gamma_{sat} \gamma_w) \bigoplus \gamma_w$

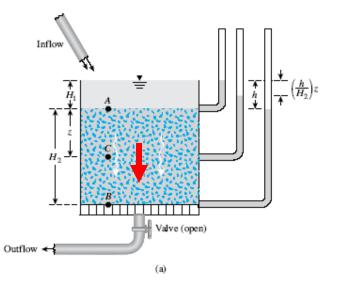
#### <u>At C,</u>

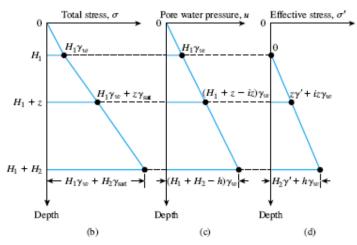
- Total Stress:  $\sigma_C = H_1 \gamma_w + z \gamma_{sat}$
- Pore water pressure:  $u_C = (H_1 + z h/H_2 z) \gamma_w$

$$= (H_1 + z - iz) \gamma_w$$

• Effective stress:  $\sigma'_C = z(\gamma_{sat} - \gamma_w) + iz \gamma_w$ 

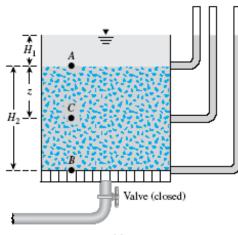
$$= z\gamma' + iz \gamma_w$$
$$= z\gamma' + iz \gamma_w$$



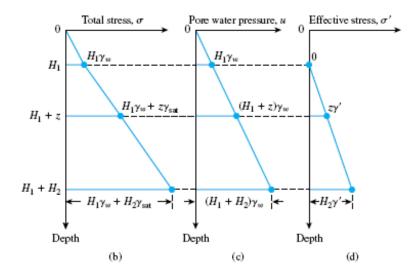


# **ONE-DIMENSIONAL FLOW**

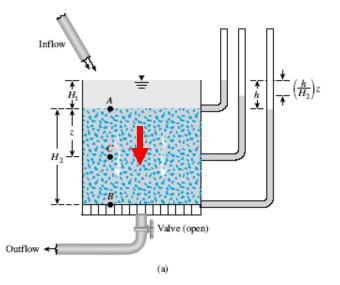
#### WITHOUT SEEPAGE

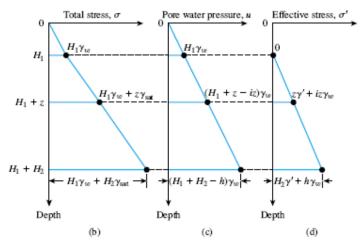






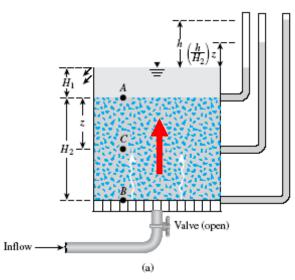
#### **DOWNWORD SEEPAGE**

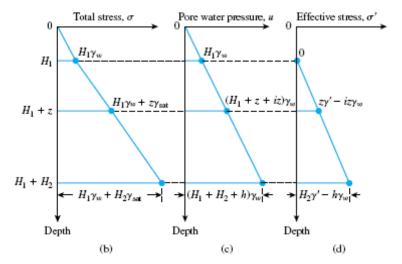




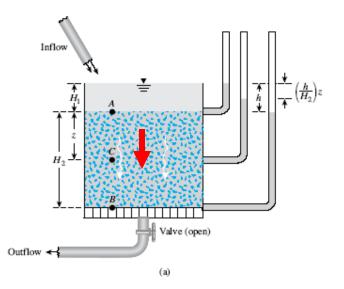
# **ONE-DIMENSIONAL FLOW**

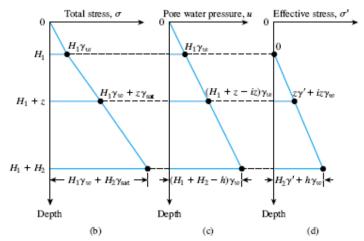
#### **UPWARD SEEPAGE**



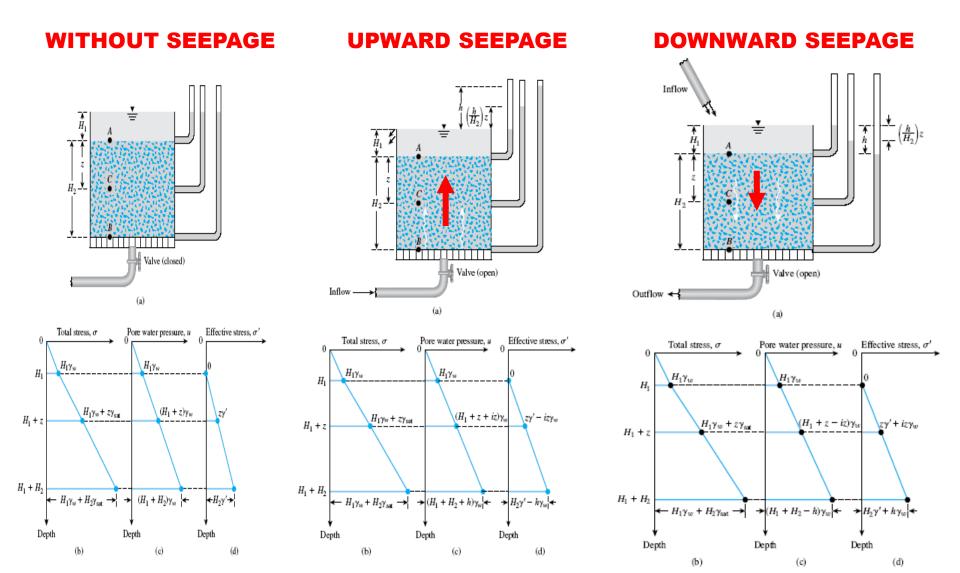


#### **DOWNWORD SEEPAGE**

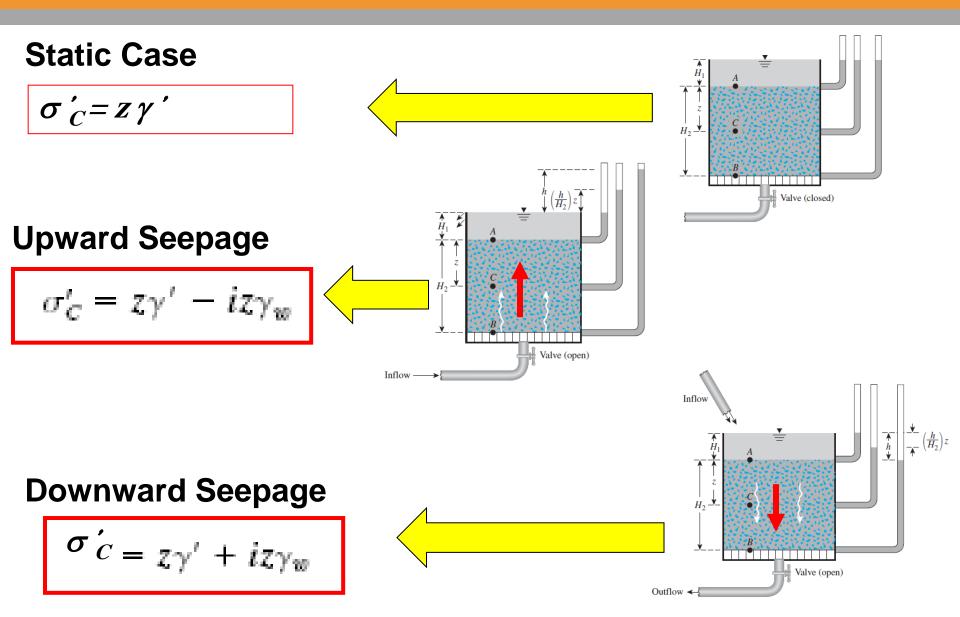




# **SUMMARY**









#### **EFFECT OF SEEPAGE**

#### UPWARD SEEPAGE

#### **DECREASES EFFECTIVE STRESS**

**DOWNWARD SEEPAGE** 

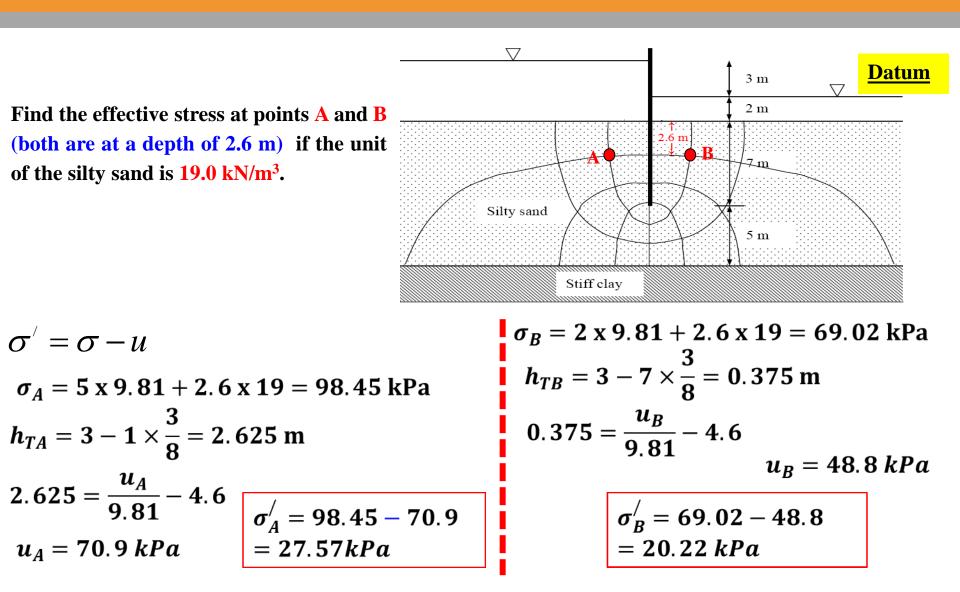
#### **INCREASES EFFECTIVE STRESS**

# **TWO-DIMENSIONAL FLOW**

- We have seen from the previous chapter how the total head is obtained by solving Laplace equation, for the specific boundary conditions.
- The problem can be solved graphically using flow net.
- Knowing the total head, the pressure head can be calculated from Bernoulli's equation.
- Effective stress is obtained from effective stress principle.

$$\sigma' = \sigma - u$$





- We have seen in the preceding sections that the effective stress at a point in a soil layer would increase or decrease due to seepage.
- For the hydrostatic case the effective stress at depth z measured from the surface of the soil layer is given by

$$\sigma' = \gamma'.z$$

Therefore, the effective force on an area A is

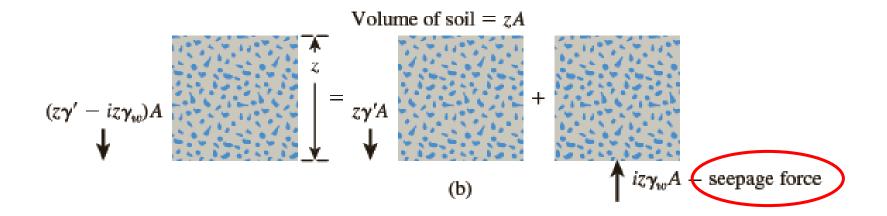
$$P_1' = \gamma'.z.A$$

$$z\gamma'A$$

If there is an <u>upward</u> seepage of water in the <u>vertical</u> direction through the same soil layer, the effective force on an area A at a depth z is given by,

$$\sigma' = \gamma' z - i z \gamma_w$$

$$P_2' = (\gamma'.z - i.z.\gamma_w)A$$



Hence, the decrease in the total force because of seepage is

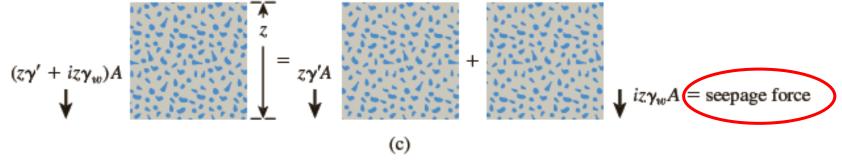
$$P_1' - P_2' = i z \gamma_w A$$

It is often convenient to express the seepage force per unit volume. Hence the seepage force per unit volume of soil is

$$\frac{P'_1 - P'_2}{\text{(Volume of soil)}} = \frac{iz\gamma_w A}{zA} = i\gamma_w$$

• The force per unit volume,  $i\gamma_w$ , for this case acts in the upward direction—that is, in the direction of flow.

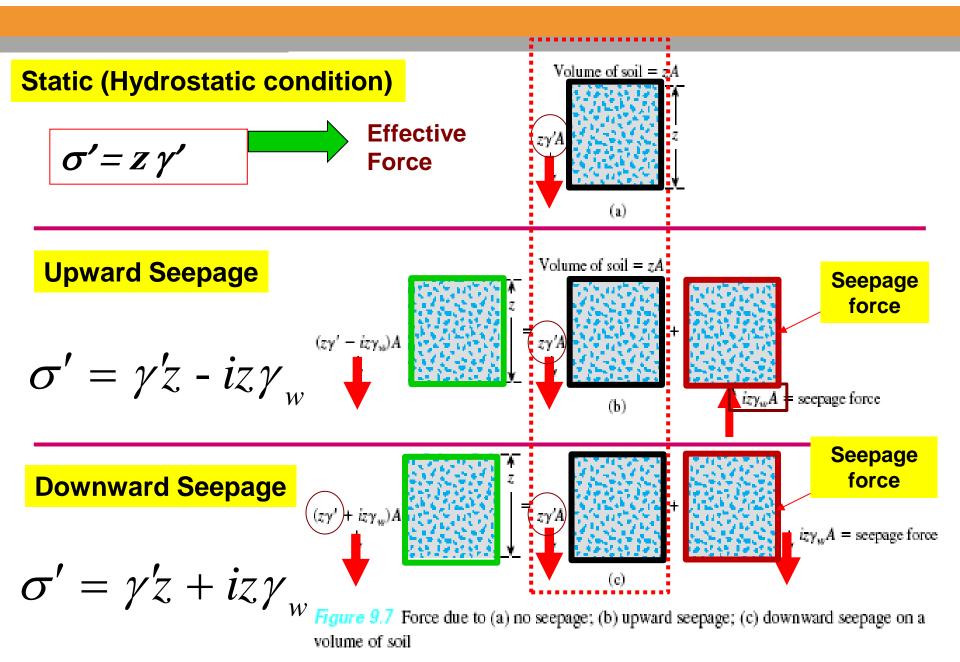
Similarly, for downward seepage, it can be shown that the seepage force in the downward direction per unit volume of soil is iγ<sub>w.</sub>



#### **Remarks**

- Flow nets can be used to find *i* at any point and, thus, seepage force per unit volume of soil. This is important in analyzing the stability of structures where heave is of a problem.
- In an isotropic soils, the force acts in the same direction as the direction of flow.

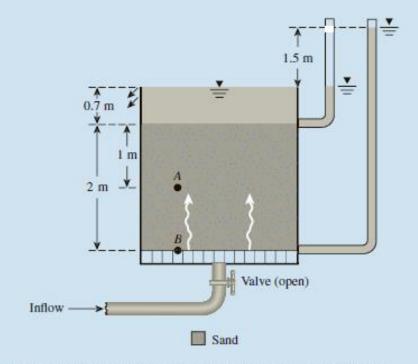
# **SUMMARY**



#### Example 9.5

Consider the upward flow of water through a layer of sand in a tank as shown in Figure 9.10. For the sand, the following are given: void ratio (e) = 0.52 and specific gravity of solids = 2.67.

- a. Calculate the total stress, pore water pressure, and effective stress at points *A* and *B*.
- b. What is the upward seepage force per unit volume of soil?





#### Solution

#### Part a

The saturated unit weight of sand is calculated as follows:

$$\gamma_{\text{sat}} = \frac{(G_s + e)\gamma_w}{1 + e} = \frac{(2.67 + 0.52)9.81}{1 + 0.52} = 20.59 \text{ kN/m}^3$$

Now, the following table can be prepared:

Point	Total           stress           Total stress, σ (kN/m²)	p.w.p Pore water pressure, <i>u</i> (kN/m <sup>2</sup> )	Effective stress, $\sigma' = \sigma - u$ (kN/m <sup>2</sup> )
Α	$0.7\gamma_w + 1\gamma_{sat} = (0.7)(9.81) + (1)(20.59) = 27.46$	$\left[(1+0.7)+\left(\frac{1.5}{2}\right)(1)\right]\gamma_w$	3.43
В	$0.7\gamma_w + 2\gamma_{sat} = (0.7)(9.81) + (2)(20.59) = 48.05$	$= (2.45)(9.81) = 24.03$ $(2 + 0.7 + 1.5)\gamma_w$ $= (4.2)(9.81) = 41.2$	6.85

# $\begin{array}{c} & & & \\ & & & & \\ & & & \\ & & & & & \\ & & & & \\ & & & & \\ & & & & & \\ & & & & & \\ & & & & & \\ & & &$

#### Part b

Hydraulic gradient (i) = 1.5/2 = 0.75. Thus, the seepage force per unit volume can be calculated as

 $i\gamma_w = (0.75)(9.81) = 7.36 \text{ kN/m}^3$ 

## HEAVING

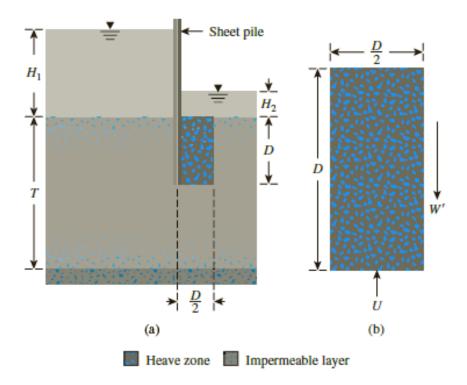
#### **Heaving in Soil Due to Flow around Sheet Piles**

$$FS = \frac{\gamma'}{i_{\rm av}\gamma_w}$$

$$FS = \frac{D\gamma'}{C_o \gamma_w (H_1 - H_2)}$$

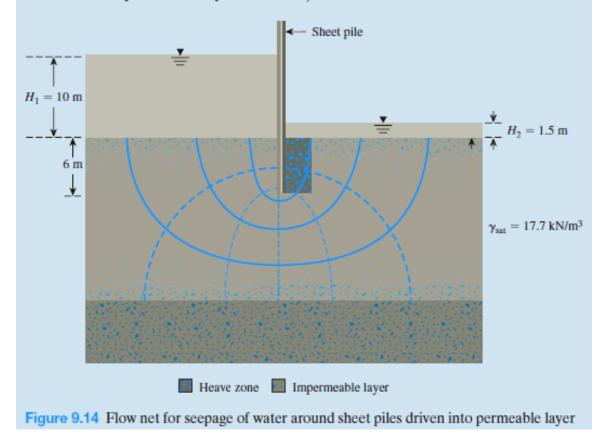
**Table 9.1** Variation of  $C_o$  with D/T

D/T	$C_o$
0.1	0.385
0.2	0.365
0.3	0.359
0.4	0.353
0.5	0.347
0.6	0.339
0.7	0.327
0.8	0.309
0.9	0.274



#### Example 9.6

Figure 9.14 shows the flow net for seepage of water around a single row of sheet piles driven into a permeable layer. Calculate the factor of safety against downstream heave, given that  $\gamma_{sat}$  for the permeable layer = 17.7 kN/m<sup>3</sup>. (*Note:* Thickness of permeable layer T = 18 m)



#### Solution

From the dimensions given in Figure 9.14, the soil prism to be considered is  $6 \text{ m} \times 3 \text{ m}$  in cross section.

The soil prism is drawn to an enlarged scale in Figure 9.15. By use of the flow net, we can calculate the head loss through the prism.

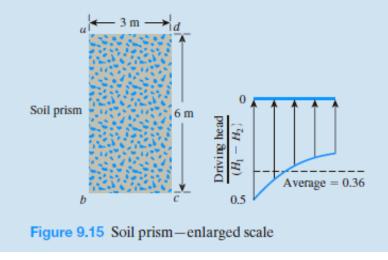
At b,

Driving head 
$$=\frac{3}{6}(H_1 - H_2)$$

At c,

Driving head 
$$\approx \frac{1.6}{6} (H_1 - H_2)$$

Similarly, for other intermediate points along bc, the approximate driving heads have been calculated and are shown in Figure 9.15.



The average value of the head loss in the prism is  $0.36(H_1 - H_2)$ , and the average hydraulic gradient is

$$i_{av} = \frac{0.36(H_1 - H_2)}{D}$$

Thus, the factor of safety [Eq. (9.20)] is

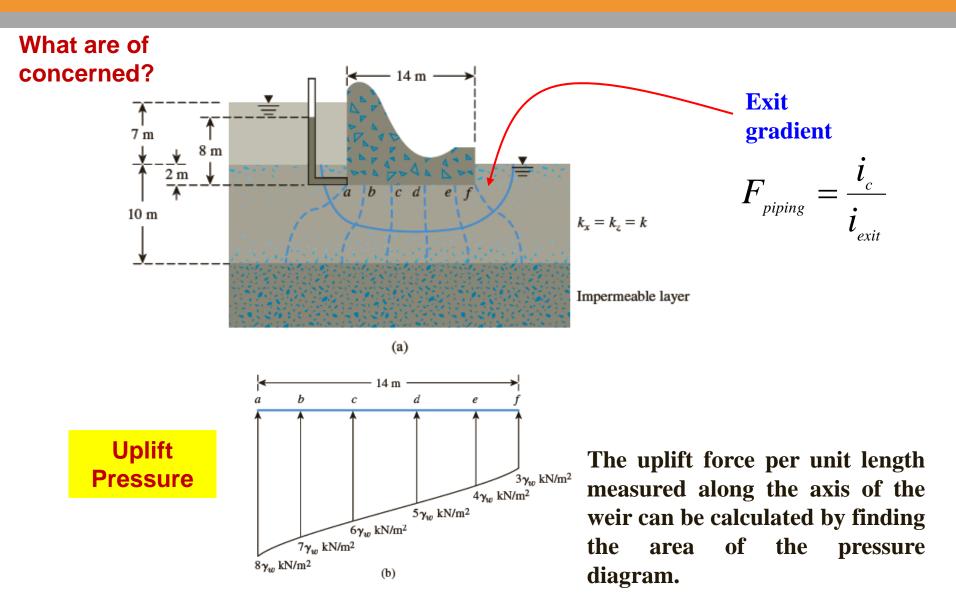
$$FS = \frac{\gamma'}{i_{av}\gamma_w} = \frac{\gamma'D}{0.36(H_1 - H_2)\gamma_w} = \frac{(17.7 - 9.81)6}{0.36(10 - 1.5) \times 9.81} = 1.58$$

#### **Alternate Solution**

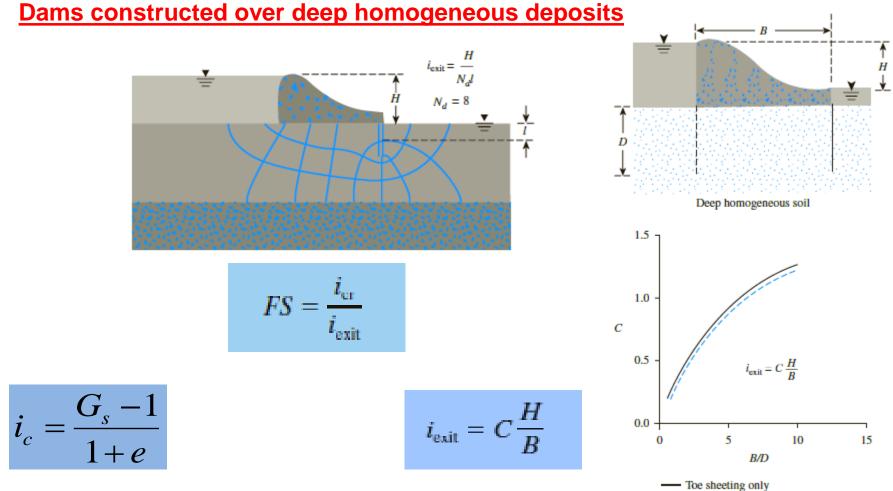
For this case, D/T = 1/3. From Table 9.1, for D/T = 1/3, the value of  $C_o = 0.357$ . Thus, from Eq. (9.22),

$$FS = \frac{D\gamma'}{C_o \gamma_w (H_1 - H_2)} = \frac{(6)(17.7 - 9.81)}{(0.357)(9.81)(10 - 1.5)} = 1.59 \text{ Low}$$

# PIPING



# HEAVING



--- Heel and toe sheeting

#### Example 9.7

Refer to Figure 9.16. For the flow under the weir, estimate the factor of safety against piping.

#### Solution

We can scale the following:

H = 4.2 m I = 1.65 m I = 1.65 m I = 0.55 m

From the flow net, note that  $N_d = 8$ . So

$$\Delta h = \frac{H}{N_d} = \frac{4.2}{8} = 0.525 \text{ m}$$
$$\Delta h = 0.525$$

$$i_{\text{exit}} = \frac{\Delta h}{l} = \frac{0.525}{1.65} = 0.318$$

From Eq. (9.24),

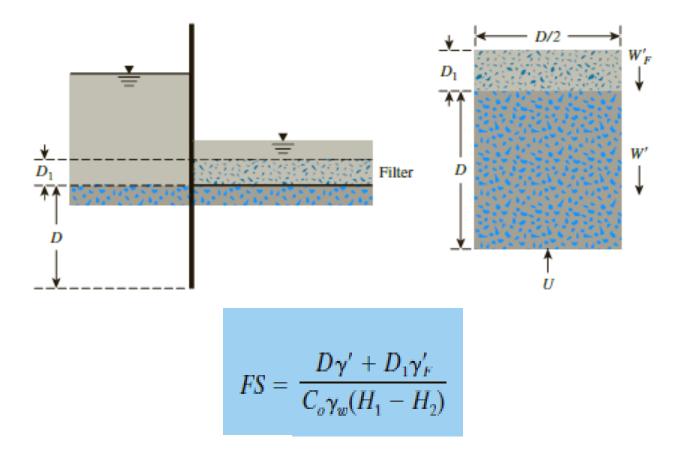
$$i_{\rm cr} = \frac{G_s - 1}{1 + e} = \frac{2.68 - 1}{1 + 0.55} = 1.08$$

From Eq. (9.23),

$$FS = \frac{i_{\rm cr}}{i_{\rm exit}} = \frac{1.08}{0.318} = 3.14$$



#### **USE OF FILTERS TO INCREASE FS AGAINST HEAVING**





#### **USE OF FILTERS TO INCREASE FS AGAINST HEAVING**

#### WITH FILTER

$$FS = \frac{\gamma' + (\frac{D_1}{D})\gamma_F'}{i_{av}\gamma_W}$$

$$FS = \frac{D\gamma' + D_1 \gamma_F'}{C_0 \gamma_W (H_1 - H_2)}$$

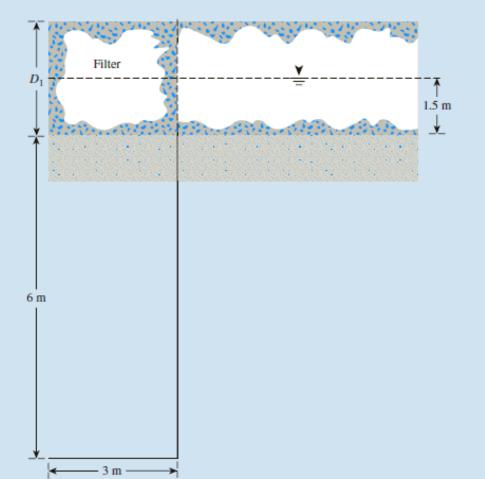
#### **NO FILTER**

$$FS = \frac{\gamma'}{i_{av}\gamma_{W}}$$

$$FS = \frac{D\gamma'}{C_o \gamma_w (H_1 - H_2)}$$

#### Example 9.8

Refer to Example 9.6. If the factor of safety against heaving needs to be increased to 2.5 by laying a filter layer on the downstream side, what should be the thickness of the layer? Given: dry and saturated unit weights of the filter material are 16 kN/m<sup>3</sup> and 20 kN/m<sup>3</sup>, respectively.



#### Solution

Refer to Figure 9.18. The filter material has a thickness of  $D_1$ . The top  $(D_1 - 1.5 \text{ m})$  of the filter is dry, and the bottom 1.5 m of the filter is submerged. Now, from Eq. (9.27),

$$FS = \frac{D\gamma' + (D_1 - 1.5)\gamma_{d(F)} + 1.5\gamma'_F}{C_o\gamma_w(H_1 - H_2)}$$

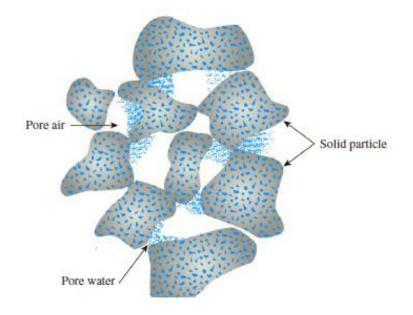
$$2.5 = \frac{(6)(17.7 - 9.81) + (D_1 - 1.5)(16) + (1.5)(20 - 9.81)}{(0.375)(9.81)(10 - 1.5)}$$
$$D_1 \approx 2.47 \text{ m}$$

#### **EFFECTIVE STRESS IN PARTIALLY SATURATED SOIL**

$$\sigma' = \sigma - u_a + x(u_a - u_w)$$

 $\sigma'$  = Effective stress

- $\sigma$  = Total stress
- $u_a =$  Pore air pressure
- $u_w =$  Pore water pressure
- x = fraction of cross sectional area of the soil occupied by water
- x = 0 dry soil
- x = 1 saturated soil



- □ The continuous void spaces in soil can behave as bundles of capillary tubes of variable cross section.
- □ Because of surface tension force, water may rise above the phreatic surface.

**Height of Rise in a Capillary Tube** 

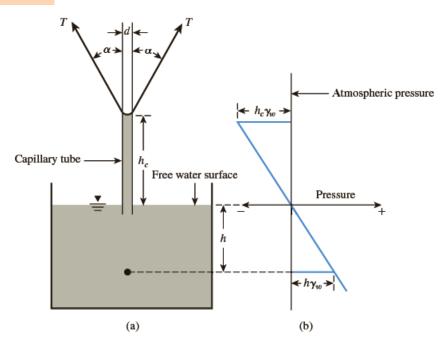
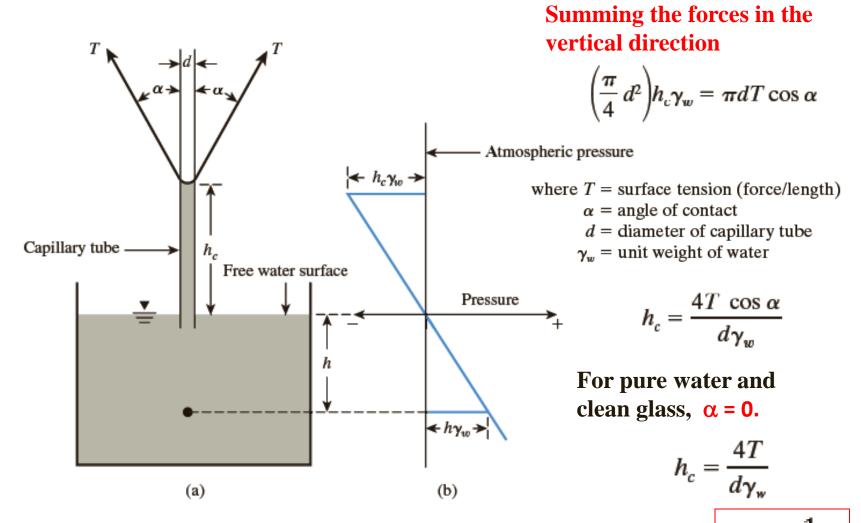


Figure 9.21 (a) Rise of water in the capillary tube; (b) pressure within the height of rise in the capillary tube (atmospheric pressure taken as datum)



 $h_c$ 

00

Figure 9.21 (a) Rise of water in the capillary tube; (b) pressure within the height of rise in the capillary tube (atmospheric pressure taken as datum)

□ The capillary tubes formed in soils because of the continuity of voids have variable cross sections.

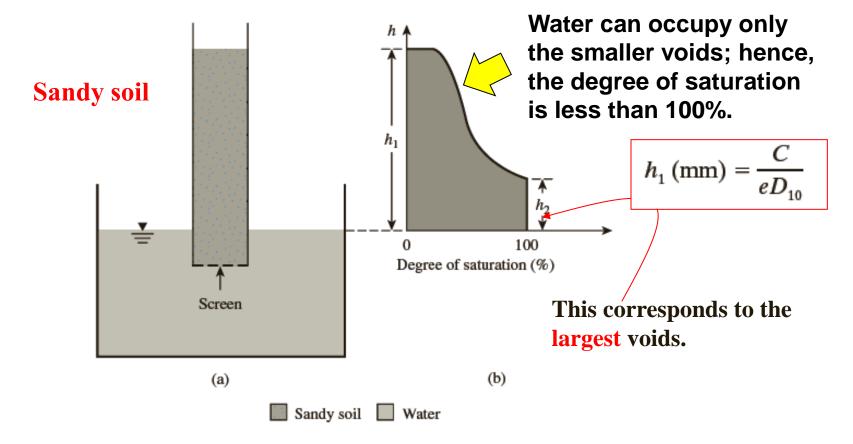


Figure 9.22 Capillary effect in sandy soil: (a) a soil column in contact with water; (b) variation of degree of saturation in the soil column

$$h_1 \,(\mathrm{mm}) = \frac{C}{e D_{10}}$$

 $C_1$  = a constant that varies from 10 to 50 mm<sup>2</sup>

	Range of capillary rise		
Soil type	m		
Coarse sand	0.1-0.2		
Fine sand	0.3-1.2		
Silt	0.75-7.5		
Clay	7.5–23		

 Table 9.2
 Approximate Range of Capillary Rise in Soils

$$\sigma = \sigma' + u$$

□ The pore water pressure u at a point in a layer of soil fully saturated by capillary rise is equal to

$$u = -\gamma_w h$$

□ Where h is the height of the point under consideration measured from the groundwater table.

□ In case of partial saturation, p.w.p. is approximately given by

$$u = -\left(\frac{S}{100}\right)\gamma_w h$$

where S degree of saturation, in percent.

A soil profile is shown in Figure 9.23. Given:  $H_1 = 1.83$  m,  $H_2 = 0.91$  m,  $H_3 = 1.83$  m. Plot the variation of  $\sigma$ , u, and  $\sigma'$  with depth.

