

Design of Flanged Sections:

$$b_e = \min \begin{cases} b_w + 16h_f \\ b_w + s_w \\ b_w + \frac{l_n}{4} \end{cases} \quad \rightarrow \text{Effective Flange width for T - section, SBC304 - 18, 6.3.2.1}$$

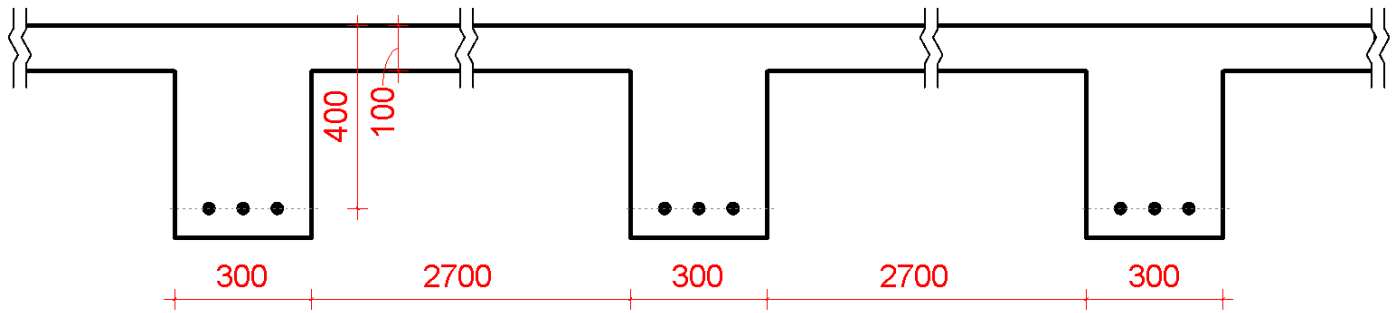
$$b_e = \min \begin{cases} b_w + 6h_f \\ b_w + \frac{s_w}{2} \\ b_w + \frac{l_n}{12} \end{cases} \quad \rightarrow \text{Effective Flange width for L - section, SBC304 - 18, 6.3.2.1}$$

$$h_f \geq \frac{b_w}{2} \quad b_e \leq 4b_w \quad \rightarrow \text{T section dimensions limitations, SBC304 - 18, 6.3.2.2}$$

$$A_{s,min} = \text{Max} \left(\frac{\sqrt{f'_c}}{4f_y} b_w d, \frac{1.4}{f_y} b_w d \right) \quad \rightarrow \text{minimum steel area, SBC304 - 9.6.1.2}$$

$$A_{sf} = \frac{0.85f'_c(b_e - b_w)h_f}{f_y} \quad \rightarrow \text{Area of steel balancing compression force in flange}$$

$$A_{sw} = A_s - A_{sf} \quad \rightarrow \text{Area of steel balancing compression force in web}$$



Design the T beam for the floor system shown below when subjected to an ultimate moment of 250 kN. m. Beam span is 4.8 m. b_w and d are given as 300 and 400 mm respectively (one layer expected). Use $f'_c = 25$ MPa, $f_y = 420$ MPa, $d_s = 10$ mm, and $d_b = 28$.

1- Calculate effective flange width b_e :

$$b_e = \min \begin{cases} b_w + 16h_f = 300 + 16 \times 100 = 1900 \text{ mm} \\ b_w + s_w = 300 + 2700 = 3000 \text{ mm} \\ b_w + \frac{l_n}{4} = 300 + \frac{4800}{4} = 1500 \text{ mm} \end{cases}$$

$$b_e = 1500 \text{ mm}$$

2- Find, ρ and $A_{s \min}$: and A_s

Assume steel is yielding and $\phi = 0.9$.

$$R_n = \frac{M_u}{\phi b_e d^2} = \frac{250 \times 10^6}{0.9 \times 1500 \times 400^2} = 1.1574$$

$$\rho = \frac{0.85f'_c}{f_y} \left(1 - \sqrt{1 - \frac{4R_n}{1.7f'_c}} \right) = \frac{0.85 \times 25}{420} \left(1 - \sqrt{1 - \frac{4 \times 1.1574}{1.7 \times 25}} \right) = 0.0028350$$

$$A_s = \rho b_e d = 0.0028350 \times 1500 \times 400 = 1701 \text{ mm}^2$$

$$A_{s, \min} = \text{Max} \left(\frac{\sqrt{f'_c}}{4f_y} b_w d, \frac{1.4}{f_y} b_w d \right) = \text{Max} \left(\frac{\sqrt{25}}{4 \times 420} \times 300 \times 400, \frac{1.4}{420} \times 300 \times 400 \right)$$

$$A_{s, \min} = 400 \text{ mm}^2$$

Use 3 ϕ 28 $A_{s \text{ provided}} = 3 \times \pi \frac{28^2}{4} = 1847 \text{ mm}^2$

$A_s \geq A_{s \min} \rightarrow \checkmark$

3- Find Neutral axis depth (c) from top fibers assuming steel is yielding and $a \leq h_f$:

$$a = \frac{A_s f_y}{0.85 f'_c b_e} = \frac{1847 \times 420}{0.85 \times 25 \times 1500} = 24.33 \text{ mm}$$

$24.33 < 100 \rightarrow$ assumption satisfied. Design as rectangular.

$$f'_c = 25 \text{ MPa} < 28 \rightarrow \beta_1 = 0.85$$

$$c = \frac{a}{\beta_1} = \frac{24.33}{0.85} = 28.63 \text{ mm}$$

4- Check assumption (steel is yielding) at most top steel layer, d_{\min}

$$\text{one layer} \rightarrow d = d_t = d_{\min} = 400 \text{ mm}$$

$$\varepsilon_{\min} = \left(\frac{d_{\min} - c}{c} \right) \varepsilon_{cu} = \left(\frac{400 - 28.63}{28.63} \right) \times 0.003 = 0.0389 \geq \varepsilon_y$$

$0.0389 \geq 0.0021 \rightarrow$ steel is yielding

5- Find ϕ :

Check strain at bottom layer

$$\varepsilon_t = \left(\frac{d_t - c}{c} \right) \varepsilon_{cu} = \left(\frac{400 - 28.63}{28.63} \right) \times 0.003 = 0.0389$$

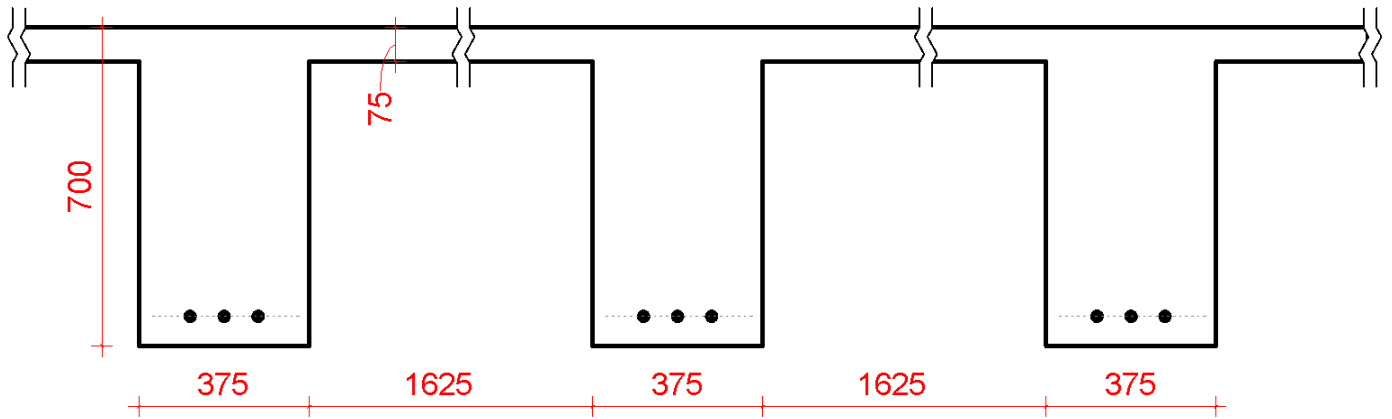
$0.0389 \geq 0.005 \rightarrow$ tension control $\rightarrow \phi = 0.9$

6- Check $\phi M_n \geq M_u$:

$$\phi M_n = \phi A_s f_y \left(d - \frac{a}{2} \right) = 0.9 \times 1847 \times 420 \left(400 - \frac{24.33}{2} \right) = 300.8 \times 10^6 \text{ N.mm}$$

$$\phi M_n = 300.8 \text{ kN.m} \geq M_u = 250 \text{ kN.m}$$

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Design the T beam for the floor system shown below when subjected to an ultimate moment of 1400 kN. m. Beam span is 4.5 m. b_w and h are given as 375 and 700 mm respectively. Use $f'_c = 25$ MPa, $f_y = 420$ MPa, $d_s = 10$ mm, $d_b = 36$. S_b and $S_l = 30$ mm.

1- Calculate effective flange width b_e :

$$b_e = \min \begin{cases} b_w + 16h_f = 375 + 16 \times 75 = 1575 \text{ mm} \\ b_w + s_w = 375 + 1625 = 2000 \text{ mm} \\ b_w + \frac{l_n}{4} = 375 + \frac{4500}{4} = 1500 \text{ mm} \end{cases}$$

$$b_e = 1500 \text{ mm}$$

2- Find, ρ and $A_{s \min}$: and A_s

Assume steel is yielding, $\phi = 0.9$, and $d = 700 - 90 = 610$ mm

$$R_n = \frac{M_u}{\phi b_e d^2} = \frac{1400 \times 10^6}{0.9 \times 1500 \times 610^2} = 2.787$$

$$\rho = \frac{0.85 f'_c}{f_y} \left(1 - \sqrt{1 - \frac{4R_n}{1.7 f'_c}} \right) = \frac{0.85 \times 25}{420} \left(1 - \sqrt{1 - \frac{4 \times 2.787}{1.7 \times 25}} \right) = 0.00714$$

$$A_s = \rho b_e d = 0.00714 \times 1500 \times 610 = 6532.5 \text{ mm}^2$$

$$A_{s, \min} = \text{Max} \left(\frac{\sqrt{f'_c}}{4 f_y} b_w d, \frac{1.4}{f_y} b_w d \right) = \text{Max} \left(\frac{\sqrt{25}}{4 \times 420} \times 375 \times 610, \frac{1.4}{420} \times 375 \times 610 \right)$$

$$A_{s, \min} = 762.5 \text{ mm}^2$$

Use 7 ϕ 36 $A_{s \text{ provided}} = 7 \times \pi 36^2 / 4 = 7125 \text{ mm}^2$

$A_s \geq A_{s \min} \rightarrow \checkmark$

3- Check number of layers:

$$n_{max} = \frac{b + S_b - 6d_s + d_b - 2cover}{d_b + S_b} = \frac{375 + 30 - 6 \times 10 + 36 - 2 \times 40}{36 + 30} = 4.56 \approx 4$$

Seven rebars need two layers. Four rebars are in bottom and three are in top.

4- Find effective depth, d :

$$d_t = h - cover - d_s - \frac{d_b}{2} = 700 - 40 - 10 - 18 = 632 \text{ mm}$$

$$d_{min} = d_t - S - d_b = 632 - 30 - 36 = 566 \text{ mm}$$

$$A_{s1} = 4 \times \pi 36^2 / 4 = 4071.5 \text{ mm}^2 \quad y_1 = 68 \text{ mm.}$$

$$A_{s2} = 3 \times \pi 36^2 / 4 = 3053.5 \text{ mm}^2 \quad y_2 = 134 \text{ mm.}$$

$$g = \frac{\sum A_{si} y_i}{A_{si}} = \frac{[4071.5 \times 68] + [3053.5 \times 134]}{(7125)} = 96.3 \text{ mm}$$

$$d = h - g = 700 - 96.3 = 603.7 \text{ mm}$$

Actual $d = 603.7$ mm is less than assumed $d = 610$ mm. ϕM_n must be checked.

5- Find Neutral axis depth (c) from top fibers assuming steel is yielding and $a \leq h_f$:

$$a = \frac{A_s f_y}{0.85 f'_c b_e} = \frac{7125 \times 420}{0.85 \times 25 \times 1500} = 93.88 \text{ mm}$$

$93.88 > 75 \rightarrow$ assumption not satisfied. Use decomposition method.

6- Find A_{sf} and A_{sw}

$$A_{sf} = \frac{0.85 f'_c (b_e - b_w) h_f}{f_y} = \frac{0.85 \times 25 \times (1500 - 375) \times 75}{420} = 4269 \text{ mm}^2$$

$$A_s = A_{sf} + A_{sw} \rightarrow A_{sw} = A_s - A_{sf} = 7125 - 4269 = 2856 \text{ mm}^2$$

7- Find Neutral axis depth (c) from top fibers assuming steel is yielding and $a > h_f$:

$$a = \frac{A_{sw} f_y}{0.85 f'_c b_w} = \frac{2856 \times 420}{0.85 \times 25 \times 375} = 150.53 \text{ mm}$$

$f'_c = 25 \text{ MPa} < 28 \rightarrow \beta_1 = 0.85$

$$c = \frac{a}{\beta_1} = \frac{150.53}{0.85} = 177.1 \text{ mm}$$

8- Check assumption (steel is yielding) at most top steel layer, d_{min}

$$\varepsilon_{min} = \left(\frac{d_{min} - c}{c} \right) \varepsilon_{cu} = \left(\frac{566 - 177.1}{177.1} \right) \times 0.003 = 0.00659 \geq \varepsilon_y$$

$0.00659 \geq 0.0021 \rightarrow$ steel is yielding

9- Find ϕ :

Check strain at bottom layer, d_t

$$\varepsilon_t = \left(\frac{d_t - c}{c} \right) \varepsilon_{cu} = \left(\frac{632 - 177.1}{177.1} \right) \times 0.003 = 0.0077$$

$0.0077 \geq 0.005 \rightarrow$ tension control $\rightarrow \phi = 0.9$

10- Find design moment capacity ϕM_n

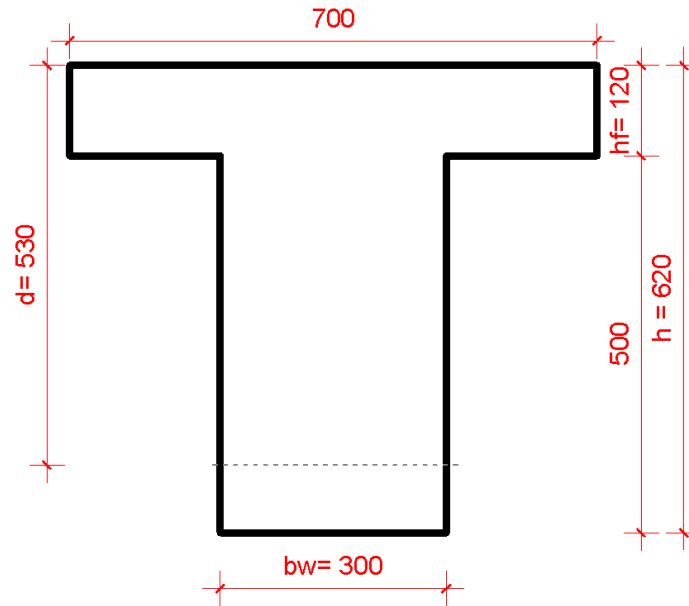
$$M_n = A_{sf} f_y \left(d - \frac{h_f}{2} \right) + A_{sw} f_y \left(d - \frac{a}{2} \right)$$

$$M_n = 4269 \times 420 \left(603.7 - \frac{75}{2} \right) + 2856 \times 420 \left(603.7 - \frac{155.53}{2} \right) = 1646.05 \times 10^6 \text{ N.mm}$$

$$\phi M_n = 0.9 \times 1646.05 = 1481.5 \text{ kN.m}$$

$\phi M_n \geq M_u \rightarrow \checkmark$

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Assuming tension control condition satisfied, design the T beam shown below when subjected to an ultimate moment of 800 kN. m. Use $f'_c = 25$ MPa, $f_y = 420$ MPa, $d_s = 10$ mm, $d_b = 36$. S_b and $S_l = 30$ mm.

Assume $d = 530$

1- Find, ρ and $A_{s\ min}$: and A_s

Assume steel is yielding and $\phi = 0.9$,

$$R_n = \frac{M_u}{\phi b_e d^2} = \frac{800 \times 10^6}{0.9 \times 700 \times 530^2} = 4.521$$

$$\rho = \frac{0.85 f'_c}{f_y} \left(1 - \sqrt{1 - \frac{4 R_n}{1.7 f'_c}} \right) = \frac{0.85 \times 25}{420} \left(1 - \sqrt{1 - \frac{4 \times 4.521}{1.7 \times 25}} \right) = 0.0122$$

$$A_s = \rho b_e d = 0.0122 \times 700 \times 530 = 4543 \text{ mm}^2$$

$$A_{s,\min} = \text{Max} \left(\frac{\sqrt{f'_c}}{4 f_y} b_w d, \frac{1.4}{f_y} b_w d \right) = \text{Max} \left(\frac{\sqrt{25}}{4 \times 420} \times 375 \times 610, \frac{1.4}{420} \times 375 \times 610 \right)$$

$$A_{s,\min} = 530 \text{ mm}^2$$

Use 5Ø36 $A_{s\ provided} = 5 \times \pi 36^2 / 4 = 5090 \text{ mm}^2$

$A_s \geq A_{s\ min} \rightarrow \checkmark$

2- Check number of layers:

$$n_{max} = \frac{b + S_b - 6d_s + d_b - 2cover}{d_b + S_b} = \frac{300 + 30 - 6 \times 10 + 36 - 2 \times 40}{36 + 30} = 3.42 \approx 3$$

Five rebars need two layers. Three rebars are in bottom and two are in top.

3- Find Neutral axis depth (c) from top fibers assuming steel is yielding and $a \leq h_f$:

$$a = \frac{A_s f_y}{0.85 f'_c b_e} = \frac{5090 \times 420}{0.85 \times 25 \times 700} = 143.72 \text{ mm}$$

143.71 > 120 → assumption not satisfied. Use decomposition method.

4- Find A_{sf} and A_{sw}

$$A_{sf} = \frac{0.85 f'_c (b_e - b_w) h_f}{f_y} = \frac{0.85 \times 25 \times (700 - 300) \times 120}{420} = 2428.5 \text{ mm}^2$$

$$A_s = A_{sf} + A_{sw} \rightarrow A_{sw} = A_s - A_{sf} = 5090 - 2428.5 = 2661.5 \text{ mm}^2$$

5- Find Neutral axis depth (c) from top fibers assuming steel is yielding and $a > h_f$:

$$a = \frac{A_{sw} f_y}{0.85 f'_c b_w} = \frac{2661.5 \times 420}{0.85 \times 25 \times 300} = 175.35 \text{ mm}$$

$f'_c = 25 \text{ MPa} < 28 \rightarrow \beta_1 = 0.85$

$$c = \frac{a}{\beta_1} = \frac{175.35}{0.85} = 206.3 \text{ mm}$$

6- Find effective depth: d , d_{min} and d_t :

$$d_t = h - cover - d_s - \frac{d_b}{2} = 620 - 40 - 10 - 18 = 552 \text{ mm}$$

$$d_{min} = d_t - S - d_b = 552 - 30 - 36 = 486 \text{ mm}$$

$$A_{s1} = 3 \times \pi 36^2 / 4 = 3054 \text{ mm}^2 \quad y_1 = 66 \text{ mm.}$$

$$A_{s2} = 2 \times \pi 36^2 / 4 = 2036 \text{ mm}^2 \quad y_2 = 132 \text{ mm.}$$

$$g = \frac{\sum A_{si} y_i}{A_{si}} = \frac{[3054 \times 66] + [2036 \times 132]}{(5090)} = 92.4 \text{ mm}$$

$$d = h - g = 620 - 92.4 = 527.6 \text{ mm}$$

Actual $d = 527.6 \text{ mm}$ is less than assumed $d = 530 \text{ mm}$. ϕM_n must be checked.

7- Check assumption (steel is yielding) at most top steel layer, d_{min}

$$\epsilon_{min} = \left(\frac{d_{min} - c}{c} \right) \epsilon_{cu} = \left(\frac{486 - 206.3}{206.3} \right) \times 0.003 = 0.0041 \geq \epsilon_y$$

0.0041 \geq 0.0021 → steel is yielding

9- Find ϕ : Check strain at bottom layer, d_t

$$\epsilon_t = \left(\frac{d_t - c}{c} \right) \epsilon_{cu} = \left(\frac{552 - 206.3}{206.3} \right) \times 0.003 = 0.00503$$

0.00503 \geq 0.005 → tension control → $\phi = 0.9$

10- Find design moment capacity ϕM_n

$$M_n = A_{sf} f_y \left(d - \frac{h_f}{2} \right) + A_{sw} f_y \left(d - \frac{a}{2} \right)$$

$$M_n = 2428.5 \times 420 \left(527.6 - \frac{120}{2} \right) + 2661.5 \times 420 \left(527.6 - \frac{175.35}{2} \right) = 968.7 \times 10^6 \text{ N.mm}$$

$$\phi M_n = 0.9 \times 968.7 = 871.83 \text{ kN.m}$$

$$\phi M_n \geq M_u \rightarrow \checkmark$$

