

Analysis of Flanged Sections:

$$b_e = \min \begin{cases} b_w + 16h_f \\ b_w + s_w \\ b_w + \frac{l_n}{4} \end{cases} \quad \rightarrow \text{Effective Flange width for T – section, SBC304 – 18, 6.3.2.1}$$

$$b_e = \min \begin{cases} b_w + 6h_f \\ b_w + \frac{s_w}{2} \\ b_w + \frac{l_n}{12} \end{cases} \quad \rightarrow \text{Effective Flange width for L – section, SBC304 – 18, 6.3.2.1}$$

$$h_f \geq \frac{b_w}{2} \quad b_e \leq 4b_w \quad \rightarrow \text{T section dimensions limitations, SBC304 – 18, 6.3.2.2}$$

$$A_{s,min} = \text{Max} \left(\frac{\sqrt{f'_c}}{4f_y} b_w d, \frac{1.4}{f_y} b_w d \right) \quad \rightarrow \text{minimum steel area, SBC304 – 9.6.1.2}$$

$$a = \frac{A_s f_y}{0.85 f'_c b_e} \quad \rightarrow \text{depth of equiv. stress block, steel yielding, } a \leq h_f$$

$$c = \frac{-\beta \pm \sqrt{\beta^2 - 4\alpha\beta d}}{2\alpha} \quad \rightarrow \text{neutral axis depth, steel not yielding, } a \leq h_f$$

$$\alpha = 0.85 f'_c b \beta_1 \quad , \quad \beta = A_s E_s \varepsilon_{cu} \quad \rightarrow \text{factors}$$

$$M_n = T \left(d - \frac{a}{2} \right) \quad \rightarrow \text{nominal moment capacity, } a \leq h_f$$

$$C_{cf} = 0.85 f'_c (b_e - b_w) h_f \quad \rightarrow \text{Compression force in overhanging flange, } a > h_f$$

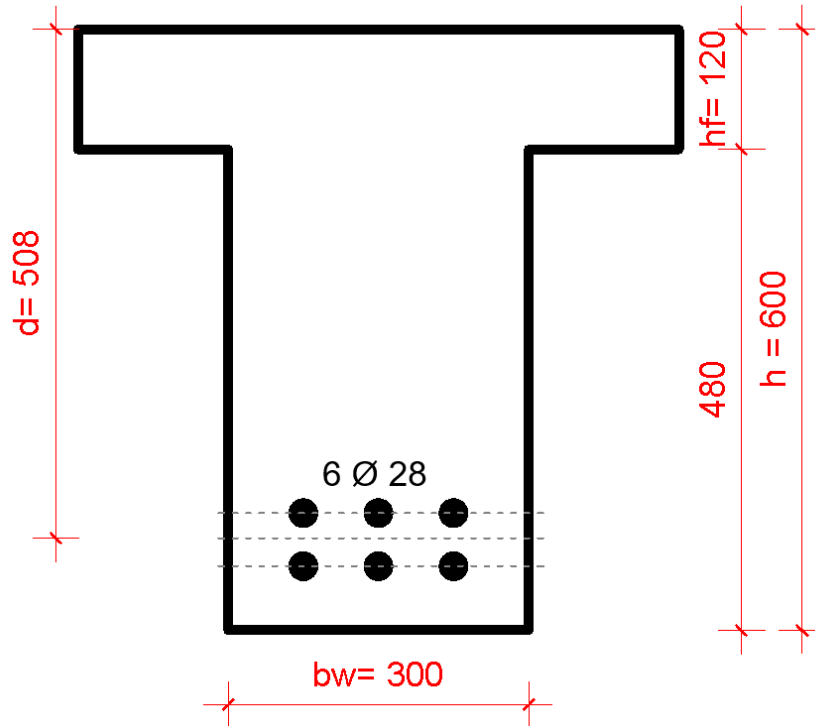
$$C_{cw} = 0.85 f'_c b_w a \quad \rightarrow \text{Compression force in web, } a > h_f$$

$$a = \frac{T - C_{cf}}{0.85 f'_c b_w} \quad \rightarrow \text{depth of equiv. stress block, steel yielding, } a > h_f$$

$$c = \frac{A + B}{2} \left(\sqrt{1 + \frac{4Ad}{(A + B)^2}} - 1 \right) \quad \rightarrow \text{neutral axis depth, steel not yielding, T beam } a > h_f$$

$$A = \frac{600 A_s}{0.85 f'_c b_w \beta_1} \quad , \quad B = \frac{(b_f - b_w) h_f}{b_w \beta_1} \quad \rightarrow \text{factors}$$

$$M_n = C_{cf} \left(d - \frac{h_f}{2} \right) + C_w \left(d - \frac{a}{2} \right) \quad \rightarrow \text{nominal moment capacity, } a > h_f$$



Determine the design moment and check minimum steel and tension control conditions. Use $f'_c = 22 \text{ MPa}$, $f_y = 420 \text{ MPa}$, $d_s = 10 \text{ mm}$, Agg. Size = 18 mm.

1- Find, A_s and $A_{s \text{ min}}$:

$$A_s = 6 \times \pi \frac{28^2}{4} = 3694.5 \text{ mm}^2$$

$$A_{s, \text{ min}} = \text{Max} \left(\frac{\sqrt{f'_c}}{4f_y} b_w d, \frac{1.4}{f_y} b_w d \right) = \text{Max} \left(\frac{\sqrt{22}}{4 \times 420} \times 300 \times 508, \frac{1.4}{420} \times 300 \times 508 \right)$$

$$A_{s, \text{ min}} = 508 \text{ mm}^2$$

$A_s \geq A_{s \text{ min}} \rightarrow \checkmark$

2- Find Neutral axis depth (c) from top fibers assuming steel is yielding and $a \leq h_f$:

$$a = \frac{A_s f_y}{0.85 f'_c b_e} = \frac{3694.5 \times 420}{0.85 \times 22 \times 600} = 276.6 \text{ mm}$$

$276.6 < 120 \rightarrow$ assumption not satisfied. Use decomposition method.

3- Calculate T , C_{cf} , a , c , and C_{cw}

$$T = A_s f_y = 3694.5 \times 420 = 1551690 \text{ N} = 1551.69 \text{ kN}$$

$$C_{cf} = 0.85 f'_c (b_e - b_w) h_f = 0.85 \times 22 \times (600 - 300) \times 120 = 673200 \text{ N} = 673.2 \text{ kN}$$

$$a = \frac{T - C_{cf}}{0.85 f'_c b_w} = \frac{1551690 - 673200}{0.85 \times 22 \times 300} = 156.59 \text{ mm}$$

$$f'_c = 22 \text{ MPa} < 28 \rightarrow \beta_1 = 0.85$$

$$c = \frac{a}{\beta_1} = \frac{156.59}{0.85} = 184.22 \text{ mm}$$

$$C_{cw} = 0.85f'_c b_w a = 0.85 \times 22 \times 300 \times 156.59 = 878469.9 \text{ N} = 878.4699 \text{ kN}$$

4- Check assumption (steel is yielding) at most top steel layer, d_{\min}

$$S_l = \max\left(\frac{4}{3} Agg, 25\right) = 25 \text{ mm}$$

$$d_t = h - \text{cover} - d_s - \frac{d_b}{2} = 600 - 40 - 10 - 14 = 536 \text{ mm}$$

$$d_{\min} = d_t - S - d_b = 536 - 25 - 28 = 483 \text{ mm}$$

$$\varepsilon_{\min} = \left(\frac{d_{\min} - c}{c}\right) \varepsilon_{cu} = \left(\frac{483 - 184.22}{184.22}\right) \times 0.003 = 0.00487 \geq \varepsilon_y$$

$0.00487 \geq 0.0021 \rightarrow$ steel is yielding

5- Find ϕ :

Check strain at bottom layer

$$\varepsilon_t = \left(\frac{d_t - c}{c}\right) \varepsilon_{cu} = \left(\frac{536 - 184.22}{184.22}\right) \times 0.003 = 0.00573 \geq 0.005 \geq \varepsilon_y$$

$0.00573 \geq 0.005 \rightarrow$ tension control $\rightarrow \phi = 0.9$

5- Find design moment capacity ϕM_n

$$M_n = C_{cf} \left(d - \frac{h_f}{2}\right) + C_w \left(d - \frac{a}{2}\right)$$

$$M_n = 673200 \left(508 - \frac{120}{2}\right) + 878469.9 \left(508 - \frac{156.59}{2}\right) = 679.08 \times 10^6 \text{ N.mm}$$

$$\phi M_n = 0.9 \times 679.08 = 611.17 \text{ kN.m}$$

Alternative Solution:

1- Find, A_s and $A_{s\ min}$:

$$A_s = 6 \times \pi \frac{28^2}{4} = 3694.5 \text{ mm}^2$$

$$A_{s,\min} = \text{Max} \left(\frac{\sqrt{f'_c}}{4f_y} b_w d, \frac{1.4}{f_y} b_w d \right) = \text{Max} \left(\frac{\sqrt{22}}{4 \times 420} \times 300 \times 508, \frac{1.4}{420} \times 300 \times 508 \right)$$

$$A_{s,\min} = 508 \text{ mm}^2$$

$A_s \geq A_{s\ \min} \rightarrow \checkmark$

2- Find Neutral axis depth (c) from top fibers assuming steel is yielding and $a \leq h_f$:

$$a = \frac{A_s f_y}{0.85 f'_c b_e} = \frac{3694.5 \times 420}{0.85 \times 22 \times 600} = 276.6 \text{ mm}$$

$276.6 < 120 \rightarrow$ assumption not satisfied. Use decomposition method.

3- Find A_{sf} and A_{sw}

$$A_{sf} = \frac{0.85 f'_c (b_e - b_w) h_f}{f_y} = \frac{0.85 \times 22 \times (600 - 300) \times 120}{420} = 1602.86 \text{ mm}^2$$

$$A_s = A_{sf} + A_{sw} \rightarrow A_{sw} = A_s - A_{sf} = 3694.5 - 1602.86 = 2091.64 \text{ mm}^2$$

4- Find Neutral axis depth (c) from top fibers assuming steel is yielding and $a > h_f$:

$$a = \frac{A_{sw} f_y}{0.85 f'_c b_w} = \frac{2091.64 \times 420}{0.85 \times 22 \times 300} = 156.59 \text{ mm}$$

$f'_c = 22 \text{ MPa} < 28 \rightarrow \beta_1 = 0.85$

$$c = \frac{a}{\beta_1} = \frac{156.59}{0.85} = 184.22 \text{ mm}$$

Check assumption (steel is yielding) at most top steel layer, d_{\min}

$$S_l = \max \left(\frac{4}{3} \text{Agg}, 25 \right) = 25 \text{ mm}$$

$$d_t = h - \text{cover} - d_s - \frac{d_b}{2} = 600 - 40 - 10 - 14 = 536 \text{ mm}$$

$$d_{\min} = d_t - S - d_b = 536 - 25 - 28 = 483 \text{ mm}$$

$$\varepsilon_{\min} = \left(\frac{d_{\min} - c}{c} \right) \varepsilon_{cu} = \left(\frac{483 - 184.22}{184.22} \right) \times 0.003 = 0.00487 \geq \varepsilon_y$$

$0.00487 \geq 0.0021 \rightarrow$ steel is yielding

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Check strain at bottom layer

$$\varepsilon_t = \left(\frac{d_t - c}{c} \right) \varepsilon_{cu} = \left(\frac{536 - 184.22}{184.22} \right) \times 0.003 = 0.00573 \geq 0.005 \geq \varepsilon_y$$

$0.00573 \geq 0.005 \rightarrow$ tension control $\rightarrow \phi = 0.9$

5- Find design moment capacity ϕM_n

$$M_n = A_{sf} f_y \left(d - \frac{h_f}{2} \right) + A_{sw} f_y \left(d - \frac{a}{2} \right)$$

$$M_n = 1602.86 \times 420 \left(508 - \frac{120}{2} \right) + 2091.64 \times 420 \left(508 - \frac{156.59}{2} \right) = 679.08 \times 10^6 \text{ N.m}$$

$$\phi M_n = 0.9 \times 679.08 = 611.17 \text{ kN.m}$$

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