

# Stat 328

## Part-1

### Statistical Analysis using Excel

There are many statistical analysis methods can be achieved using Excel

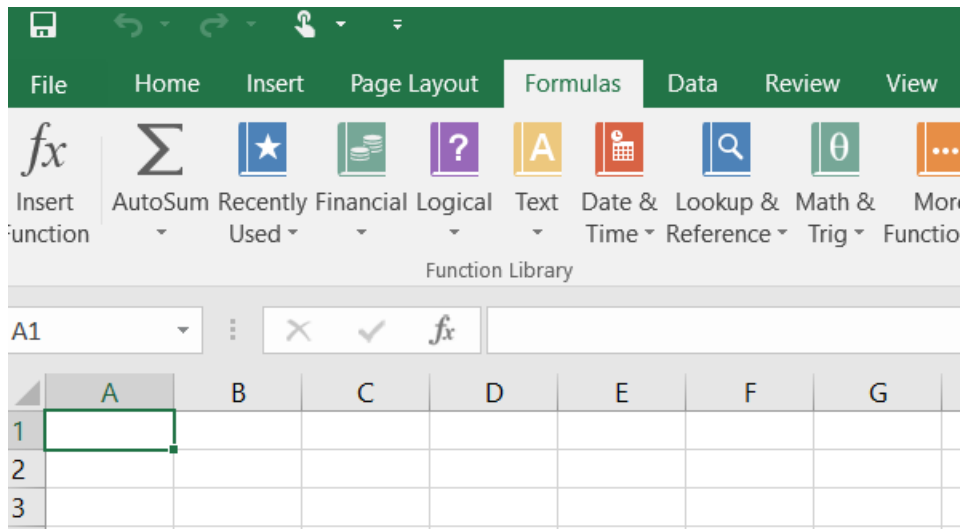
#### 1-1 Functions

Three different type of function can be used in statistics; they are:

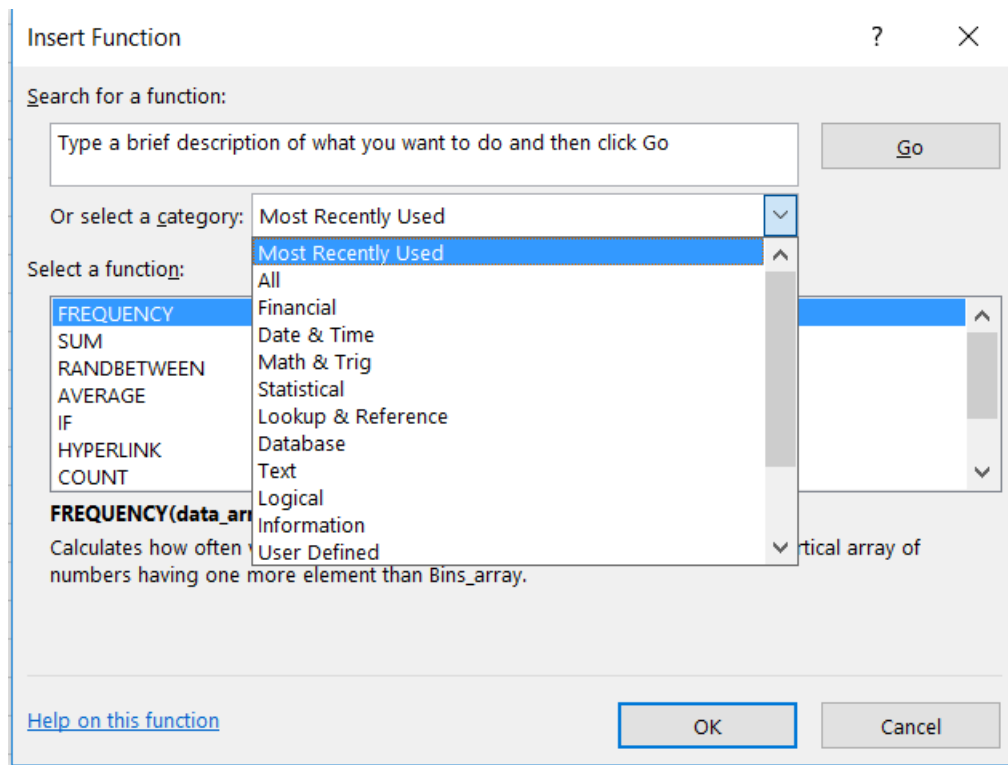
- (a) Statistical Functions
- (b) Mathematical Functions
- (c) Logical Functions

These function can be obtained from excel as:

Click the **Formulas** tab, then select the **Insert Function** command



Then, we get



So, if we select the statistical to get a list of possible statistical functions as follows:

#### Count & Frequency

|                                   |  |
|-----------------------------------|--|
| <a href="#"><u>COUNT</u></a>      | Returns the number of numerical values in a supplied set of cells or values  |
| <a href="#"><u>COUNTA</u></a>     | Returns the number of non-blanks in a supplied set of cells or values  |
| <a href="#"><u>COUNTBLANK</u></a> | Returns the number of blank cells in a supplied range  |
| <a href="#"><u>COUNTIF</u></a>    | Returns the number of cells (of a supplied range), that satisfy a given criteria                                   |
| <a href="#"><u>COUNTIFS</u></a>   | Returns the number of cells (of a supplied range), that satisfy a set of given criteria <i>(New in Excel 2007)</i> |
| <a href="#"><u>FREQUENCY</u></a>  | Returns an array showing the number of values from a supplied array, which fall into specified ranges              |

#### Finding the Largest & Smallest Values

|                               |  |
|-------------------------------|--|
| <a href="#"><u>MAX</u></a>    | Returns the largest value from a list of supplied numbers  |
| <a href="#"><u>MAXA</u></a>   | Returns the largest value from a list of supplied values, counting text and the logical value FALSE as the value 0 and counting the logical value TRUE as the value 1  |
| <a href="#"><u>MAXIFS</u></a> | Returns the largest value from a subset of values in a list that are specified according to one or more criteria. <i>(New in Excel 2016)</i>                           |
| <a href="#"><u>MIN</u></a>    | Returns the smallest value from a list of supplied numbers   |
| <a href="#"><u>MINA</u></a>   | Returns the smallest value from a list of supplied values, counting text and the logical value FALSE as the value 0 and counting the logical value TRUE as the value 1 |
| <a href="#"><u>MINIFS</u></a> | Returns the smallest value from a subset of values in a list that are specified according to one or more criteria. <i>(New in Excel 2016)</i>                          |
| <a href="#"><u>LARGE</u></a>  | Returns the Kth LARGEST value from a list of supplied numbers, for a given value K   |
| <a href="#"><u>SMALL</u></a>  | Returns the Kth SMALLEST value from a list of supplied numbers, for a given value K  |

#### Percentiles, Quartiles & Rank

|  |   |
|--|---|
| <a href="#"><u>PERCENTILE</u></a>      | Returns the K'th percentile of values in a supplied range, where K is in the range 0 - 1 (inclusive) <i>(Replaced by Percentile.Inc function in Excel 2010)</i>   |
| <a href="#"><u>PERCENTILE.INC</u></a>  | Returns the K'th percentile of values in a supplied range, where K is in the range 0 - 1 (inclusive) <i>(New in Excel 2010 - replaces the Percentile function)</i>  |
| <a href="#"><u>PERCENTILE.EXC</u></a>  | Returns the K'th percentile of values in a supplied range, where K is in the range 0 - 1 (exclusive) <i>(New in Excel 2010)</i>   |
| <a href="#"><u>QUARTILE</u></a>        | Returns the specified quartile of a set of supplied numbers, based on percentile value 0 - 1 (inclusive) <i>(Replaced by Quartile.Inc function in Excel 2010)</i>   |
| <a href="#"><u>QUARTILE.INC</u></a>    | Returns the specified quartile of a set of supplied numbers, based on percentile value 0 - 1 (inclusive) <i>(New in Excel 2010 - replaces the Quartile function)</i>  |
| <a href="#"><u>QUARTILE.EXC</u></a>    | Returns the specified quartile of a set of supplied numbers, based on percentile value 0 - 1 (exclusive) <i>(New in Excel 2010)</i>   |
| <a href="#"><u>RANK</u></a>            | Returns the statistical rank of a given value, within a supplied array of values <i>(Replaced by Rank.Eq function in Excel 2010)</i>  |
| <a href="#"><u>RANK.EQ</u></a>         | Returns the Mode (the most frequently occurring value) of a list of supplied numbers (if more than one value has same rank, the top rank of that set is returned) <i>(New in Excel 2010 - replaces the Rank function)</i> |
| <a href="#"><u>RANK.AVG</u></a>        | Returns the statistical rank of a given value, within a supplied array of values (if more than one value has same rank, the average rank is returned) <i>(New in Excel 2010)</i>  |
| <a href="#"><u>PERCENTRANK</u></a>     | Returns the rank of a value in a data set, as a percentage (0 - 1 inclusive) <i>(Replaced by Percentrank.Inc function in Excel 2010)</i>  |
| <a href="#"><u>PERCENTRANK.INC</u></a> | Returns the rank of a value in a data set, as a percentage (0 - 1 inclusive) <i>(New in Excel 2010 - replaces the Percentrank function)</i>   |
| <a href="#"><u>PERCENTRANK.EXC</u></a> | Returns the rank of a value in a data set, as a percentage (0 - 1 exclusive) <i>(New in Excel 2010)</i>   |

## Averages

|                                   |  |
|-----------------------------------|--|
| <a href="#"><u>AVERAGE</u></a>    | Returns the Average of a list of supplied numbers  |
| <a href="#"><u>AVERAGEA</u></a>   | Returns the Average of a list of supplied numbers, counting text and the logical value FALSE as the value 0 and counting the logical value TRUE as the value 1 |
| <a href="#"><u>AVERAGEIF</u></a>  | Calculates the Average of the cells in a supplied range, that satisfy a given criteria <i>(New in Excel 2007)</i>  |
| <a href="#"><u>AVERAGEIFS</u></a> | Calculates the Average of the cells in a supplied range, that satisfy multiple criteria <i>(New in Excel 2007)</i>   |

|                                  |  |
|----------------------------------|--|
| <a href="#"><u>MEDIAN</u></a>    | Returns the Median (the middle value) of a list of supplied numbers  |
| <a href="#"><u>MODE</u></a>      | Returns the Mode (the most frequently occurring value) of a list of supplied numbers <i>(Replaced by Mode.Sngl function in Excel 2010)</i>   |
| <a href="#"><u>MODE.SNGL</u></a> | Returns the Mode (the most frequently occurring value) of a list of supplied numbers <i>(New in Excel 2010 - replaces the Mode function)</i> |
| <a href="#"><u>MODE.MULT</u></a> | Returns a vertical array of the most frequently occurring values in an array or range of data <i>(New in Excel 2010)</i>                     |
| <a href="#"><u>GEOMEAN</u></a>   | Returns the geometric mean of a set of supplied numbers  |
| <a href="#"><u>HARMEAN</u></a>   | Returns the harmonic mean of a set of supplied numbers   |
| <a href="#"><u>TRIMMEAN</u></a>  | Returns the mean of the interior of a supplied set of values   |

#### Deviation & Variance

|                                |  |
|--------------------------------|--|
| <a href="#"><u>AVEDEV</u></a>  | Returns the average of the absolute deviations of data points from their mean  |
| <a href="#"><u>DEVSQ</u></a>   | Returns the sum of the squares of the deviations of a set of data points from their sample mean  |
| <a href="#"><u>STDEV</u></a>   | Returns the standard deviation of a supplied set of values (which represent a sample of a population) <i>(Replaced by Stdev.S function in Excel 2010)</i>  |
| <a href="#"><u>STDEV.S</u></a> | Returns the standard deviation of a supplied set of values (which represent a sample of a population) <i>(New in Excel 2010 - replaces the Stdev function)</i>   |
| <a href="#"><u>STDEVA</u></a>  | Returns the standard deviation of a supplied set of values (which represent a sample of a population), counting text and the logical value FALSE as the value 0 and counting the logical value TRUE as the value 1 |
| <a href="#"><u>STDEV.P</u></a> | Returns the standard deviation of a supplied set of values (which represent an entire population) <i>(Replaced by Stdev.P function in Excel 2010)</i>  |
| <a href="#"><u>STDEV.P</u></a> | Returns the standard deviation of a supplied set of values (which represent an entire population) <i>(New in Excel 2010 - replaces the Stdevp function)</i>  |
| <a href="#"><u>STDEVPA</u></a> | Returns the standard deviation of a supplied set of values (which represent an entire population), counting text and the logical value FALSE as the value 0 and counting the logical value TRUE as the value 1     |
| <a href="#"><u>VAR</u></a>     | Returns the variance of a supplied set of values (which represent a sample of a population) <i>(Replaced by Var.S function in Excel 2010)</i>  |

|                                     |  |
|-------------------------------------|--|
| <a href="#"><u>VAR.S</u></a>        | Returns the variance of a supplied set of values (which represent a sample of a population) <i>(New in Excel 2010 - replaces the Var function)</i>   |
| <a href="#"><u>VARA</u></a>         | Returns the variance of a supplied set of values (which represent a sample of a population), counting text and the logical value FALSE as the value 0 and counting the logical value TRUE as the value 1 |
| <a href="#"><u>VARP</u></a>         | Returns the variance of a supplied set of values (which represent an entire population) <i>(Replaced by Var.P function in Excel 2010)</i>  |
| <a href="#"><u>VAR.P</u></a>        | Returns the variance of a supplied set of values (which represent an entire population) <i>(New in Excel 2010 - replaces the Varp function)</i>  |
| <a href="#"><u>VARPA</u></a>        | Returns the variance of a supplied set of values (which represent an entire population), counting text and the logical value FALSE as the value 0 and counting the logical value TRUE as the value 1     |
| <a href="#"><u>COVAR</u></a>        | Returns population covariance (i.e. the average of the products of deviations for each pair within two supplied data sets) <i>(Replaced by Covariance.P function in Excel 2010)</i>                      |
| <a href="#"><u>COVARIANCE.P</u></a> | Returns population covariance (i.e. the average of the products of deviations for each pair within two supplied data sets) <i>(New in Excel 2010 - replaces the Covar function)</i>                      |
| <a href="#"><u>COVARIANCE.S</u></a> | Returns sample covariance (i.e. the average of the products of deviations for each pair within two supplied data sets) <i>(New in Excel 2010)</i>  |

#### Confidence Intervals

|  |  |
|--|--|
| <a href="#"><u>CONFIDENCE</u></a>      | Returns the confidence interval for a population mean, using a normal distribution <i>(Replaced by Confidence.Norm function in Excel 2010)</i>   |
| <a href="#"><u>CONFIDENCE.NORM</u></a> | Returns the confidence interval for a population mean, using a normal distribution <i>(New in Excel 2010 - replaces the Confidence function)</i> |
| <a href="#"><u>CONFIDENCE.T</u></a>    | Returns the confidence interval for a population mean, using a Student's t distribution <i>(New in Excel 2010)</i>                               |

#### Trend Line Functions

|                                  |   |
|----------------------------------|---|
| <a href="#"><u>FORECAST</u></a>  | Predicts a future point on a linear trend line fitted to a supplied set of x- and y- values   |
| <a href="#"><u>INTERCEPT</u></a> | Calculates the best fit regression line, through a supplied series of x- and y- values and returns the value at which this line intercepts the y-axis |
| <a href="#"><u>LINEST</u></a>    | Returns statistical information describing the trend of the line of best fit, through a supplied series of x- and y- values                           |

|                               |  |
|-------------------------------|--|
| <a href="#"><u>SLOPE</u></a>  | Returns the slope of the linear regression line through a supplied series of x- and y- values                                |
| <a href="#"><u>TREND</u></a>  | Calculates the trend line through a given set of y-values and returns additional y-values for a supplied set of new x-values |
| <a href="#"><u>GROWTH</u></a> | Returns numbers in a exponential growth trend, based on a set of supplied x- and y- values                                   |
| <a href="#"><u>LOGEST</u></a> | Returns the parameters of an exponential trend for a supplied set of x- and y- values  |
| <a href="#"><u>STEYX</u></a>  | Returns the standard error of the predicted y-value for each x in the regression line for a set of supplied x- and y- values |

|                                     |  |
|-------------------------------------|--|
| <a href="#"><u>PERMUT</u></a>       | Returns the number of permutations for a given number of objects   |
| <a href="#"><u>PERMUTATIONA</u></a> | Returns the number of permutations for a given number of objects (with repetitions) that can be selected from the total objects <i>(New in Excel 2013)</i> |

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#### Distribution & Tests of Probability

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|-----------------------------------|--|
| <a href="#"><u>BETADIST</u></a>   | Returns the cumulative beta probability density function <i>(Replaced by Beta.Dist function in Excel 2010)</i>   |
| <a href="#"><u>BETA.DIST</u></a>  | Returns the cumulative beta distribution function or the beta probability density function <i>(New in Excel 2010 - replaces the Betadist function)</i> |
| <a href="#"><u>BETAINV</u></a>    | Returns the inverse of the cumulative beta probability density function <i>(Replaced by Beta.Inv function in Excel 2010)</i>                           |
| <a href="#"><u>BETA.INV</u></a>   | Returns the inverse of the cumulative beta probability density function <i>(New in Excel 2010 - replaces the Betainv function)</i>                     |
| <a href="#"><u>BINOMDIST</u></a>  | Returns the individual term binomial distribution probability <i>(Replaced by Binom.Dist function in Excel 2010)</i>                                   |
| <a href="#"><u>BINOM.DIST</u></a> | Returns the individual term binomial distribution probability <i>(New in Excel 2010 - replaces the Binomdist function)</i>                             |

|                                |  |
|--------------------------------|--|
| <u><b>BINOM.DIST.RANGE</b></u> | Returns the probability of a trial result using a binomial distribution <i>(New in Excel 2013)</i>   |
| <u><b>NEGBINOMDIST</b></u>     | Returns the negative binomial distribution <i>(Replaced by Negbinom.Dist function in Excel 2010)</i>   |
| <u><b>NEGBINOM.DIST</b></u>    | Returns the negative binomial distribution <i>(New in Excel 2010 - replaces the Negbinomdist function)</i>   |
| <u><b>CRITBINOM</b></u>        | Returns the smallest value for which the cumulative binomial distribution is greater than or equal to a criterion value <i>(Replaced by Binom.Inv function in Excel 2010)</i>        |
| <u><b>BINOM.INV</b></u>        | Returns the smallest value for which the cumulative binomial distribution is greater than or equal to a criterion value <i>(New in Excel 2010 - replaces the Critbinom function)</i> |
| <u><b>CHIDIST</b></u>          | Returns the right-tailed probability of the chi-squared distribution <i>(Replaced by Chisq.Dist.Rt function in Excel 2010)</i>   |
| <u><b>CHISQ.DIST.RT</b></u>    | Returns the right-tailed probability of the chi-squared distribution <i>(New in Excel 2010 - replaces the Chidist function)</i>  |
| <u><b>CHISQ.DIST</b></u>       | Returns the chi-squared distribution (probability density or cumulative distribution function) <i>(New in Excel 2010)</i>  |
| <u><b>CHIINV</b></u>           | Returns the inverse of the right-tailed probability of the chi-squared distribution <i>(Replaced by Chisq.Inv.Rt function in Excel 2010)</i>   |
| <u><b>CHISQ.INV.RT</b></u>     | Returns the inverse of the right-tailed probability of the chi-squared distribution <i>(New in Excel 2010 - replaces the Chiinv function)</i>  |
| <u><b>CHISQ.INV</b></u>        | Returns the inverse of the left-tailed probability of the chi-squared distribution <i>(New in Excel 2010)</i>  |
| <u><b>CHITEST</b></u>          | Returns the chi-squared statistical test for independence <i>(Replaced by Chisq.Test function in Excel 2010)</i>   |
| <u><b>CHISQ.TEST</b></u>       | Returns the chi-squared statistical test for independence <i>(New in Excel 2010 - replaces the Chitest function)</i>   |
| <u><b>CORREL</b></u>           | Returns the correlation coefficient between two sets of values   |
| <u><b>EXPONDIST</b></u>        | Returns the exponential distribution <i>(Replaced by Expon.Dist function in Excel 2010)</i>  |
| <u><b>EXPON.DIST</b></u>       | Returns the exponential distribution <i>(New in Excel 2010 - replaces the Expondist function)</i>  |
| <u><b>FDIST</b></u>            | Returns the right-tailed F probability distribution for two data sets <i>(Replaced by F.Dist.Rt function in Excel 2010)</i>  |



|                               |  |
|-------------------------------|--|
| <u><b>F.DIST.RT</b></u>       | Returns the right-tailed F probability distribution for two data sets <i>(New in Excel 2010 - replaces the Fdist function)</i>   |
| <u><b>F.DIST</b></u>          | Returns the F probability distribution (probability density or cumulative distribution function) <i>(New in Excel 2010)</i>  |
| <u><b>FINV</b></u>            | Returns the inverse of the right-tailed F probability distribution for two data sets <i>(Replaced by F.Inv.Rt function in Excel 2010)</i>                              |
| <u><b>F.INV.RT</b></u>        | Returns the inverse of the right-tailed F probability distribution for two data sets <i>(New in Excel 2010 - replaces the Finv function)</i>                           |
| <u><b>F.INV</b></u>           | Returns the inverse of the Cumulative F distribution <i>(New in Excel 2010)</i>  |
| <u><b>FISHER</b></u>          | Returns the Fisher transformation  |
| <u><b>FISHERINV</b></u>       | Returns the inverse of the Fisher transformation   |
| <u><b>FTEST</b></u>           | Returns the result of an F-Test for 2 supplied data sets <i>(Replaced by F.Test function in Excel 2010)</i>  |
| <u><b>F.TEST</b></u>          | Returns the result of an F-Test for 2 supplied data sets <i>(New in Excel 2010 - replaces the Ftest function)</i>  |
| <u><b>GAMMADIST</b></u>       | Returns the gamma distribution <i>(Replaced by Gamma.Dist function in Excel 2010)</i>  |
| <u><b>GAMMA.DIST</b></u>      | Returns the gamma distribution <i>(New in Excel 2010 - replaces the Gammadist function)</i>  |
| <u><b>GAMMAINV</b></u>        | Returns the inverse gamma cumulative distribution <i>(Replaced by Gamma.Inv function in Excel 2010)</i>  |
| <u><b>GAMMA.INV</b></u>       | Returns the inverse gamma cumulative distribution <i>(New in Excel 2010 - replaces the Gammainv function)</i>  |
| <u><b>GAMMA</b></u>           | Return the gamma function value for a supplied number <i>(New in Excel 2013)</i>   |
| <u><b>GAMMALN</b></u>         | Calculates the natural logarithm of the gamma function for a supplied value  |
| <u><b>GAMMALN.PRECISE</b></u> | Returns the natural logarithm of the gamma function for a supplied value <i>(New in Excel 2010)</i>  |
| <u><b>GAUSS</b></u>           | Calculates the probability that a member of a standard normal population will fall between the mean and z standard deviations from the mean <i>(New in Excel 2013)</i> |
| <u><b>HYPGEOMDIST</b></u>     | Returns the hypergeometric distribution <i>(Replaced by Hypgeom.Dist function in Excel 2010)</i>   |
| <u><b>HYPGEOM.DIST</b></u>    | Returns the hypergeometric distribution <i>(New in Excel 2010 - replaces the Hypgeomdist function)</i>   |

|                     |   |
|---------------------|---|
| <u>KURT</u>         | Returns the kurtosis of a data set  |
| <u>LOGNORMDIST</u>  | Returns the cumulative log-normal distribution <i>(Replaced by Lognorm.Dist function in Excel 2010)</i>   |
| <u>LOGNORM.DIST</u> | Returns the log-normal probability density function or the cumulative log- normal distribution <i>(New in Excel 2010 - replaces the Lognormdist function)</i> |
| <u>LOGINV</u>       | Returns the inverse of the lognormal distribution <i>(Replaced by Lognorm.Inv function in Excel 2010)</i>   |
| <u>LOGNORM.INV</u>  | Returns the inverse of the lognormal distribution <i>(New in Excel 2010 - replaces the Loginv function)</i>   |
| <u>NORMDIST</u>     | Returns the normal cumulative distribution <i>(Replaced by Norm.Dist function in Excel 2010)</i>  |
| <u>NORM.DIST</u>    | Returns the normal cumulative distribution <i>(New in Excel 2010 - replaces the Normdist function)</i>  |
| <u>NORMINV</u>      | Returns the inverse of the normal cumulative distribution <i>(Replaced by Norm.Inv function in Excel 2010)</i>  |
| <u>NORM.INV</u>     | Returns the inverse of the normal cumulative distribution <i>(New in Excel 2010 - replaces the Norminv function)</i>  |
| <u>NORMSDIST</u>    | Returns the standard normal cumulative distribution <i>(Replaced by Norm.S.Dist function in Excel 2010)</i>   |
| <u>NORM.S.DIST</u>  | Returns the standard normal cumulative distribution <i>(New in Excel 2010 - replaces the Normsdist function)</i>  |
| <u>NORMSINV</u>     | Returns the inverse of the standard normal cumulative distribution <i>(Replaced by Norm.S.Inv function in Excel 2010)</i>                                     |
| <u>NORM.S.INV</u>   | Returns the inverse of the standard normal cumulative distribution <i>(New in Excel 2010 - replaces the Normsinv function)</i>                                |
| <u>PEARSON</u>      | Returns the Pearson product moment correlation coefficient  |
| <u>RSQ</u>          | Returns the square of the Pearson product moment correlation coefficient  |
| <u>PHI</u>          | Returns the value of the density function for a standard normal distribution, for a supplied number <i>(New in Excel 2013)</i>                                |
| <u>POISSON</u>      | Returns the Poisson distribution <i>(Replaced by Poisson.Dist function in Excel 2010)</i>   |
| <u>POISSON.DIST</u> | Returns the Poisson distribution <i>(New in Excel 2010 - replaces the Poisson function)</i>   |
| <u>PROB</u>         | Returns the probability that values in a supplied range are within given limits   |

|                                     |   |
|-------------------------------------|---|
| <u><a href="#">SKEW</a></u>         | Returns the skewness of a distribution  |
| <u><a href="#">SKEW.P</a></u>       | Returns the skewness of a distribution based on a population <i>(New in Excel 2013)</i>                                   |
| <u><a href="#">STANDARDIZE</a></u>  | Returns a normalized value  |
| <u><a href="#">TDIST</a></u>        | Returns the Student's T-distribution <i>(Replaced by T.Dist.2t &amp; T.Dist.Rt functions in Excel 2010)</i>               |
| <u><a href="#">T.DIST.2T</a></u>    | Returns the two-tailed Student's T-distribution <i>(New in Excel 2010 - replaces the Tdist function)</i>                  |
| <u><a href="#">T.DIST.RT</a></u>    | Returns the right-tailed Student's T-distribution <i>(New in Excel 2010 - replaces the Tdist function)</i>                |
| <u><a href="#">T.DIST</a></u>       | Returns the Student's T-distribution (probability density or cumulative distribution function) <i>(New in Excel 2010)</i> |
| <u><a href="#">TINV</a></u>         | Returns the two-tailed inverse of the Student's T-distribution <i>(Replaced by T.Inv.2t function in Excel 2010)</i>       |
| <u><a href="#">T.INV.2T</a></u>     | Returns the two-tailed inverse of the Student's T-distribution <i>(New in Excel 2010 - replaces the Tinv function)</i>    |
| <u><a href="#">T.INV</a></u>        | Returns the left-tailed inverse of the Student's T-distribution <i>(New in Excel 2010)</i>                                |
| <u><a href="#">TTEST</a></u>        | Returns the probability associated with a Student's T-Test <i>(Replaced by T.Test function in Excel 2010)</i>             |
| <u><a href="#">T.TEST</a></u>       | Returns the probability associated with a Student's T-Test <i>(New in Excel 2010 - replaces the Ttest function)</i>       |
| <u><a href="#">WEIBULL</a></u>      | Returns the Weibull distribution <i>(Replaced by Weibull.Dist function in Excel 2010)</i>                                 |
| <u><a href="#">WEIBULL.DIST</a></u> | Returns the Weibull distribution <i>(New in Excel 2010 - replaces the Weibull function)</i>                               |
| <u><a href="#">ZTEST</a></u>        | Returns the one-tailed probability value of a z-test <i>(Replaced by Z.Test function in Excel 2010)</i>                   |
| <u><a href="#">Z.TEST</a></u>       | Returns the one-tailed probability value of a z-test <i>(New in Excel 2010 - replaces the Ztest function)</i>             |

Similarly, if we select the Math& Trig  
We get a list of possible Mathematical  
functions as follows:

#### Basic Numeric Information

|                             |   |
|-----------------------------|---|
| <a href="#"><u>ABS</u></a>  | Returns the absolute value (i.e. the modulus) of a supplied number  |
| <a href="#"><u>SIGN</u></a> | Returns the sign (+1, -1 or 0) of a supplied number                 |
| <a href="#"><u>GCD</u></a>  | Returns the Greatest Common Divisor of two or more supplied numbers |
| <a href="#"><u>LCM</u></a>  | Returns the Least Common Multiple of two or more supplied numbers   |

#### Basic Mathematical Operations

|                                  |   |
|----------------------------------|---|
| <a href="#"><u>SUM</u></a>       | Returns the sum of a supplied list of numbers   |
| <a href="#"><u>PRODUCT</u></a>   | Returns the product of a supplied list of numbers   |
| <a href="#"><u>POWER</u></a>     | Returns the result of a given number raised to a supplied power   |
| <a href="#"><u>SQRT</u></a>      | Returns the positive square root of a given number  |
| <a href="#"><u>QUOTIENT</u></a>  | Returns the integer portion of a division between two supplied numbers  |
| <a href="#"><u>MOD</u></a>       | Returns the remainder from a division between two supplied numbers  |
| <a href="#"><u>AGGREGATE</u></a> | Performs a specified calculation (e.g. the sum, product, average, etc.) for a list or database, with the option to ignore hidden rows and error values ( <i>New in Excel 2010</i> ) |
| <a href="#"><u>SUBTOTAL</u></a>  | Performs a specified calculation (e.g. the sum, product, average, etc.) for a supplied set of values  |

#### Rounding Functions

|  |  |
|--|--|
| <a href="#"><u>CEILING</u></a>         | Rounds a number <u>away from zero</u> (i.e. rounds a positive number up and a negative number down), to a multiple of significance |
| <a href="#"><u>CEILING.PRECISE</u></a> | Rounds a number <u>up</u> , regardless of the sign of the number, to a multiple of significance ( <i>New in Excel 2010</i> )       |

|                                      |  |
|--------------------------------------|--|
| <a href="#"><u>ISO.CEILING</u></a>   | Rounds a number <u>up</u> , regardless of the sign of the number, to a multiple of significance. <i>(New in Excel 2010)</i>        |
| <a href="#"><u>CEILING.MATH</u></a>  | Rounds a number up to the nearest integer or to the nearest multiple of significance <i>(New in Excel 2013)</i>                    |
| <a href="#"><u>EVEN</u></a>          | Rounds a number <u>away from zero</u> (i.e. rounds a positive number up and a negative number down), to the next even number       |
| <a href="#"><u>FLOOR</u></a>         | Rounds a number <u>towards zero</u> , (i.e. rounds a positive number down and a negative number up), to a multiple of significance |
| <a href="#"><u>FLOOR.PRECISE</u></a> | Rounds a number <u>down</u> , regardless of the sign of the number, to a multiple of significance <i>(New in Excel 2010)</i>       |
| <a href="#"><u>FLOOR.MATH</u></a>    | Rounds a number down, to the nearest integer or to the nearest multiple of significance <i>(New in Excel 2013)</i>                 |
| <a href="#"><u>INT</u></a>           | Rounds a number <u>down</u> to the next integer  |
| <a href="#"><u>MROUND</u></a>        | Rounds a number <u>up or down</u> , to the nearest multiple of significance  |
| <a href="#"><u>ODD</u></a>           | Rounds a number <u>away from zero</u> (i.e. rounds a positive number up and a negative number down), to the next odd number        |
| <a href="#"><u>ROUND</u></a>         | Rounds a number <u>up or down</u> , to a given number of digits  |
| <a href="#"><u>ROUNDDOWN</u></a>     | Rounds a number <u>towards zero</u> , (i.e. rounds a positive number down and a negative number up), to a given number of digits   |
| <a href="#"><u>ROUNDUP</u></a>       | Rounds a number <u>away from zero</u> (i.e. rounds a positive number up and a negative number down), to a given number of digits   |
| <a href="#"><u>TRUNC</u></a>         | Truncates a number <u>towards zero</u> (i.e. rounds a positive number down and a negative number up), to the next integer.         |

---

#### Matrix Functions

|                                 |  |
|---------------------------------|--|
| <a href="#"><u>MDETERM</u></a>  | Returns the matrix determinant of a supplied array                           |
| <a href="#"><u>MINVERSE</u></a> | Returns the matrix inverse of a supplied array                               |
| <a href="#"><u>MMULT</u></a>    | Returns the matrix product of two supplied arrays                            |
| <a href="#"><u>MUNIT</u></a>    | Returns the unit matrix for a specified dimension <i>(New in Excel 2013)</i> |

---

#### Random Numbers

|                             |   |
|-----------------------------|---|
| <a href="#"><u>RAND</u></a> | Returns a random number between 0 and 1 |
|-----------------------------|---|

**RANDBETWEEN** Returns a random number between two given integers

### Conditional Sums

**SUMIF** Adds the cells in a supplied range, that satisfy a given criteria

**SUMIFS** Adds the cells in a supplied range, that satisfy multiple criteria (*New in Excel 2007*)

### Advanced Mathematical Operations

**SUMPRODUCT** Returns the sum of the products of corresponding values in two or more supplied arrays

**SUMSQ** Returns the sum of the squares of a supplied list of numbers

**SUMX2MY2** Returns the sum of the difference of squares of corresponding values in two supplied arrays

**SUMX2PY2** Returns the sum of the sum of squares of corresponding values in two supplied arrays

**SUMXMY2** Returns the sum of squares of differences of corresponding values in two supplied arrays

**SERIESSUM** Returns the sum of a power series

### Trigonometry Functions

**PI** Returns the constant value of pi

**SQRTPI** Returns the square root of a supplied number multiplied by pi

**DEGREES** Converts Radians to Degrees

**RADIANS** Converts Degrees to Radians

**COS** Returns the Cosine of a given angle

**ACOS** Returns the Arccosine of a number

**COSH** Returns the hyperbolic cosine of a number

**ACOSH** Returns the inverse hyperbolic cosine of a number

**SEC** Returns the secant of an angle (*New in Excel 2013*)

**SECH** Returns the hyperbolic secant of an angle (*New in Excel 2013*)

**SIN** Returns the Sine of a given angle

**ASIN** Returns the Arcsine of a number

|                                    |   |
|------------------------------------|---|
| <a href="#"><u>SINH</u></a>        | Returns the Hyperbolic Sine of a number   |
| <a href="#"><u>ASINH</u></a>       | Returns the Inverse Hyperbolic Sine of a number   |
| <a href="#"><u>CSC</u></a>         | Returns the cosecant of an angle <i>(New in Excel 2013)</i>   |
| <a href="#"><u>CSCH</u></a>        | Returns the hyperbolic cosecant of an angle <i>(New in Excel 2013)</i>  |
| <a href="#"><u>TAN</u></a>         | Returns the Tangent of a given angle  |
| <a href="#"><u>ATAN</u></a>        | Returns the Arctangent of a given number  |
| <a href="#"><u>ATAN2</u></a>       | Returns the Arctangent of a given pair of x and y coordinates   |
| <a href="#"><u>TANH</u></a>        | Returns the Hyperbolic Tangent of a given number  |
| <a href="#"><u>ATANH</u></a>       | Returns the Inverse Hyperbolic Tangent of a given number  |
| <a href="#"><u>COT</u></a>         | Returns the cotangent of an angle <i>(New in Excel 2013)</i>  |
| <a href="#"><u>COTH</u></a>        | Returns the hyperbolic cotangent of an angle <i>(New in Excel 2013)</i>   |
| <a href="#"><u>ACOT</u></a>        | Returns the arccotangent of a number <i>(New in Excel 2013)</i>   |
| <a href="#"><u>ACOTH</u></a>       | Returns the hyperbolic arccotangent of a number <i>(New in Excel 2013)</i>                                      |
| <b>Exponents &amp; Logarithms</b>  |   |
| <a href="#"><u>EXP</u></a>         | Returns $e$ raised to a given power   |
| <a href="#"><u>LN</u></a>          | Returns the natural logarithm of a given number   |
| <a href="#"><u>LOG</u></a>         | Returns the logarithm of a given number, to a specified base  |
| <a href="#"><u>LOG10</u></a>       | Returns the base 10 logarithm of a given number   |
| <b>Factorials</b>                  |   |
| <a href="#"><u>FACT</u></a>        | Returns the Factorial of a given number   |
| <a href="#"><u>FACTDOUBLE</u></a>  | Returns the Double Factorial of a given number  |
| <a href="#"><u>MULTINOMIAL</u></a> | Returns the Multinomial of a given set of numbers   |
| <b>Miscellaneous</b>               |   |
| <a href="#"><u>BASE</u></a>        | Converts a number into a text representation, with the supplied base <i>(New in Excel 2013)</i>                 |
| <a href="#"><u>DECIMAL</u></a>     | Converts a text representation of a number in a specified base into a decimal number <i>(New in Excel 2013)</i> |
| <a href="#"><u>COMBIN</u></a>      | Returns the number of combinations (without repetitions) for a given number of objects                          |
| <a href="#"><u>COMBINA</u></a>     | Returns the number of combinations (with repetitions) for a given number of items <i>(New in Excel 2013)</i>    |
| <a href="#"><u>ARABIC</u></a>      | Converts a Roman numeral to an Arabic numeral <i>(New in Excel 2013)</i>  |

**ROMAN**

Returns a text string depicting the roman numeral for a given number

Also, if we select the Logical, we get a list of possible logical functions as follows:

| Function                                | Description   |
|---|---|
| <a href="#"><u>AND function</u></a>     | Returns TRUE if all of its arguments are TRUE   |
| <a href="#"><u>FALSE function</u></a>   | Returns the logical value FALSE   |
| <a href="#"><u>IF function</u></a>      | Specifies a logical test to perform   |
| <a href="#"><u>IFERROR function</u></a> | Returns a value you specify if a formula evaluates to an error; otherwise, returns the result of the formula  |
| <a href="#"><u>IFNA function</u></a>    | Returns the value you specify if the expression resolves to #N/A, otherwise returns the result of the expression  |
| <a href="#"><u>IFS function</u></a>     | Checks whether one or more conditions are met and returns a value that corresponds to the first TRUE condition.   |
| <a href="#"><u>NOT function</u></a>     | Reverses the logic of its argument  |
| <a href="#"><u>OR function</u></a>      | Returns TRUE if any argument is TRUE  |
| <a href="#"><u>SWITCH function</u></a>  | Evaluates an expression against a list of values and returns the result corresponding to the first matching value. If there is no match, an optional default value may be returned. |
| <a href="#"><u>TRUE function</u></a>    | Returns the logical value TRUE  |
| <a href="#"><u>XOR function</u></a>     | Returns a logical exclusive OR of all arguments   |



# Examples

## 1- Math & Tri functions

| No | Function | syntax      | Description  | Examples                  |
|----|----------|-------------|--|---------------------------|
| 1  | ABS      | ABS(number) | Valuate the absolute value of a number             | Abs(6) = 6<br>Abs(-5) = 5 |
| 2  | Combin   | Combin(n;x) | Calculate the binomial coefficients $\binom{n}{x}$ | Combin(5;3)=10            |
| 3  |          |             |  |                           |
| 4  |          |             |  |                           |
| 5  |          |             |  |                           |
| 6  |          |             |  |                           |

## 2-Statistical functions

| No | Function | syntax  | Description   | Examples                             |
|----|----------|---|---|--------------------------------------|
| 1  | Average  | average(a1; a2; ... an)                           | Calculate the mean of a1, a2, ....an  | AVERAGE(1,8,9,2)=5                   |
| 2  | normdist | Normdist(x; mean; standard deviation; cumulative) | Calculate the cumulative probability function on normal distribution with given mean and standard derivation) | Normdist( 1.96; 0; 1; True) = 0.9750 |
| 3  | Norminv  |   |   |                                      |
|    |          |   |   |                                      |

## 3-Logical statements

| No | Function | syntax   | Description   | Examples  |
|----|----------|--|---|---|
| 1  | If       | If( logical test; statment1 if true; statement 2 if false) | If statement; do statement 1 if true, do statement 2 if false | Let x be a column of values 1, 2, 3. write the following statement in the first cell of the column y if(x2<=1; 1; 2). The output of the column y will be 1,2,3. |
| 2  |          |  |   |   |

## Some other examples on the statistical functions

### Examples

- 1- Calculate the mean, median, variance, standard deviation and mode(s) for the following data

2, 3, 2, 2, 0, 2, 3, 6, 3, 2, 2, 4, 3, 1, 3, 3, 3, 2, 1, 5

To achieve this in excel put the data in a column (A1:A20) or row and use the following commands

=AVERAGE(A1:A20)

=MEDIAN(A1:A20)

=STDEV.S(A1:A20)

=STDEV.P(A1:A20)

=VAR.P(A1:A20)

=VAR.S(A1:A20)

### 2- Frequency Table (Frequency-example)

### 3- Probability distributions

If  $X \sim N(2, 7)$  , *then Calculate*

$$P(X < 1.5), \quad f(3), \quad P(X < k) = 0.25, \quad k ?$$

### Some other examples on the mathematical functions

#### Example

Calculate  $\exp(-1.5)$ ,  $\text{Log}(25)$  and  $\ln(25)$

#### Example on the logical functions

Use if statement to print the status of the student ( $Pass \geq 60$ ,  $fail < 60$ )

In creation exam using the following marks

Marks

70

85

83

25

80

98

80

72

42

If(A1<60,"F","P")

## Some mathematical, statistical and logical functions in excel

### Some Examples on the Mathematical Function

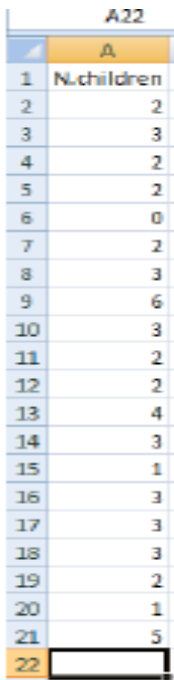
|                 |                     |             |
|-----------------|---------------------|-------------|
| $e^{-1.5}$      | =EXP(-1.5)          | 0.22313016  |
| $\log(25)$      | =LOG(25)            | 1.397940009 |
| $\ln(25)$       | =LN(25)             | 3.218875825 |
| $\binom{10}{2}$ | =COMBIN(10,2)       | 45          |
| $\sqrt{25}$     | =SQRT(25)           | 5           |
| $ -10 $         | =ABS(-10)           | 10          |
| $3^2$           | =POWER(3,2)<br>=3^2 | 9           |

### Some Examples on the Statistical Function

#### Example

Suppose we are interested in the number of children that a Saudi woman has and we take a sample of 20 women and obtain the following data on the number of children

2, 3, 2, 2, 0, 2, 3, 6, 3, 2, 2, 4, 3, 1, 3, 3, 3, 2, 1, 5



|    | A          |
|----|------------|
| 1  | N.children |
| 2  | 2          |
| 3  | 3          |
| 4  | 2          |
| 5  | 2          |
| 6  | 0          |
| 7  | 2          |
| 8  | 3          |
| 9  | 6          |
| 10 | 3          |
| 11 | 2          |
| 12 | 2          |
| 13 | 4          |
| 14 | 3          |
| 15 | 1          |
| 16 | 3          |
| 17 | 3          |
| 18 | 3          |
| 19 | 2          |
| 20 | 1          |
| 21 | 5          |
| 22 |            |

- Calculate the mean, median, variance, standard deviation, total, maximum, minimum and mode(s)

To achieve this in excel put the data in a column (A2:A21) or row and use the following commands

|          |                  |                   |          |
|----------|------------------|-------------------|----------|
| Total    | =SUM(A2:A21)     |                   | 52       |
| Mean     | =AVERAGE(A2:A21) |                   | 2.6      |
| Median   | =MEDIAN(A2:A21)  |                   | 2.5      |
| Max      | =MAX(A2:A21)     |                   | 6        |
| Min      | =MIN (A2:A21)    |                   | 0        |
| Standard | =STDEV(A2:A21)   | New in Excel 2010 | 1.353358 |

|                                   |                   |                                       |          |
|-----------------------------------|-------------------|---------------------------------------|----------|
| deviation for sample              |                   | =STDEV.S(A2:A21)                      |          |
| Standard deviation for population | = STDEV P(A2:A21) | New in Excel 2010<br>=STDEV.P(A2:A21) | 1.319091 |
| Variance for sample               | =VAR(A2:A21)      | New in Excel 2010<br>=VAR.S(A2:A21)   | 1.831579 |
| Variance for population           | =VARP (A2:A21)    | New in Excel 2010<br>=VAR.S(A2:A21)   | 1.74     |

### - Frequency Table

| N.children |                      | Frequency |
|------------|----------------------|-----------|
| 0          | =COUNTIF(A2:A21,"0") | 1         |
| 1          | =COUNTIF(A2:A21,"1") | 2         |
| 2          | =COUNTIF(A2:A21,"2") | 7         |
| 3          | =COUNTIF(A2:A21,"3") | 7         |
| 4          | =COUNTIF(A2:A21,"4") | 1         |
| 5          | =COUNTIF(A2:A21,"5") | 1         |
| 6          | =COUNTIF(A2:A21,"6") | 1         |

### - Probability distributions

If  $X \sim N(2,7)$ , then Calculate

|                       |                         |          |
|-----------------------|-------------------------|----------|
| $P(X < 1.5)$          | =NORMDIST(1.5,2,7,TRUE) | 0.471528 |
| $P(X < k) = 0.25, k?$ | =NORMINV(0.25,2,7)      | -2.72143 |

### Example on the Logical Functions

Use if statement to print the status of the student ( $Pass \geq 60, Fail < 60$ ). In creation exam using the following marks

|   | A     |                          |       |
|---|-------|--------------------------|-------|
| 1 | Marks | Function                 | Grade |
| 2 | 70    | =IF(A2<60,"Fail","Pass") | Pass  |
| 3 | 85    | =IF(A3<60,"Fail","Pass") | Pass  |
| 4 | 83    | =IF(A4<60,"Fail","Pass") | Pass  |
| 5 | 25    | =IF(A5<60,"Fail","Pass") | Fail  |
| 6 | 80    | =IF(A6<60,"Fail","Pass") | Pass  |
| 7 | 98    | =IF(A7<60,"Fail","Pass") | Pass  |

|    |    |                           |      |
|----|----|---------------------------|------|
| 8  | 80 | =IF(A8<60,"Fail","Pass")  | Pass |
| 9  | 72 | =IF(A9<60,"Fail","Pass")  | Pass |
| 10 | 42 | =IF(A10<60,"Fail","Pass") | Fail |
| 11 | 32 | =IF(A11<60,"Fail","Pass") | Fail |

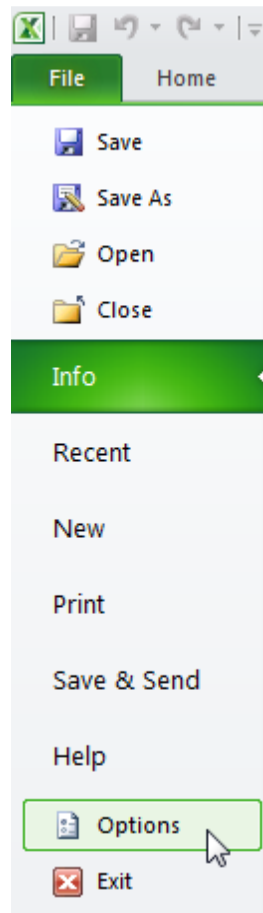
## Descriptive statistics using excel

### - Data Analysis

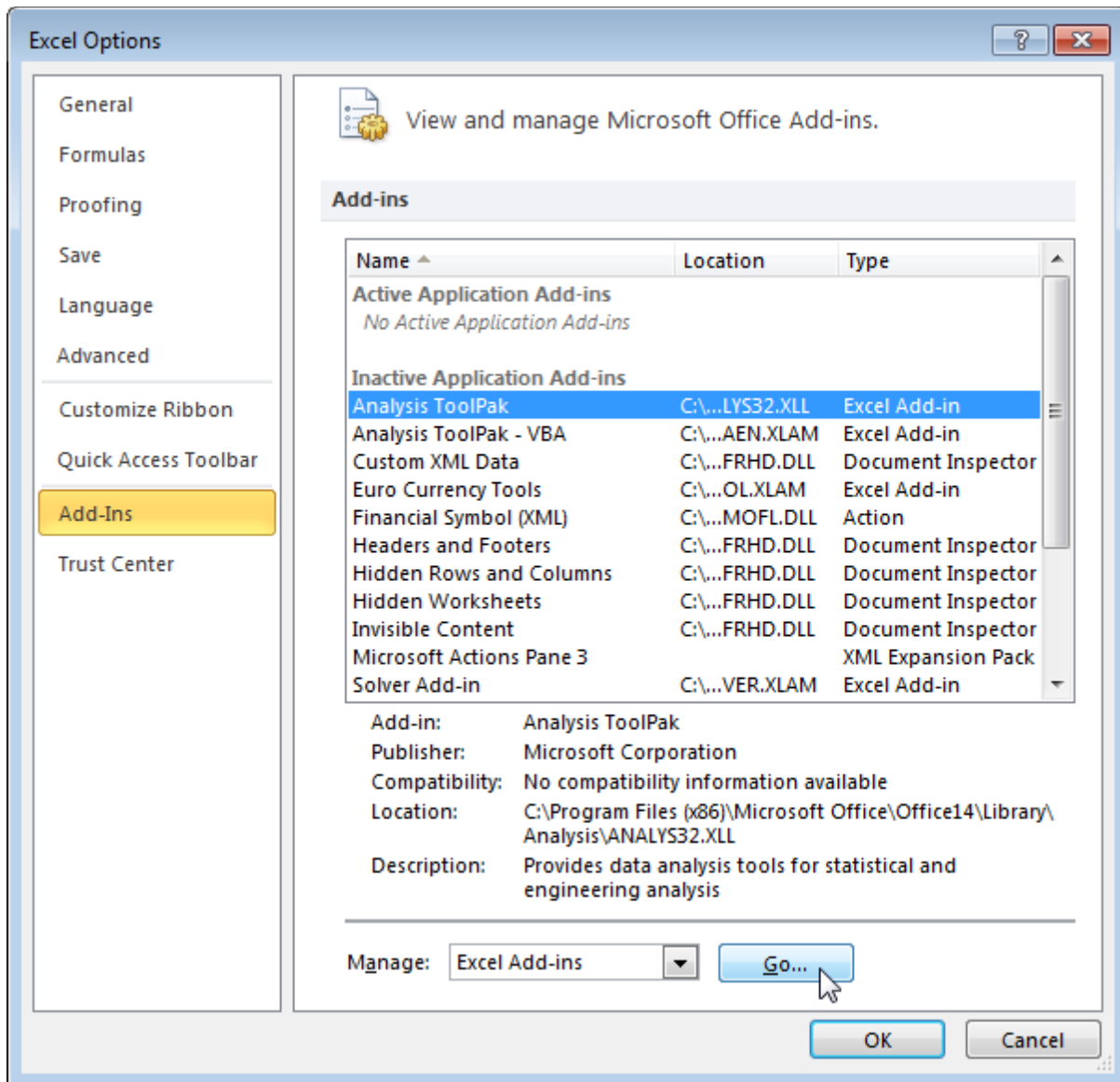
The Analysis ToolPak is an Excel add-in program that provides data analysis tools for financial, statistical and engineering data analysis.

To load the Analysis ToolPak add-in, execute the following steps.

1. Click on Excel Options.

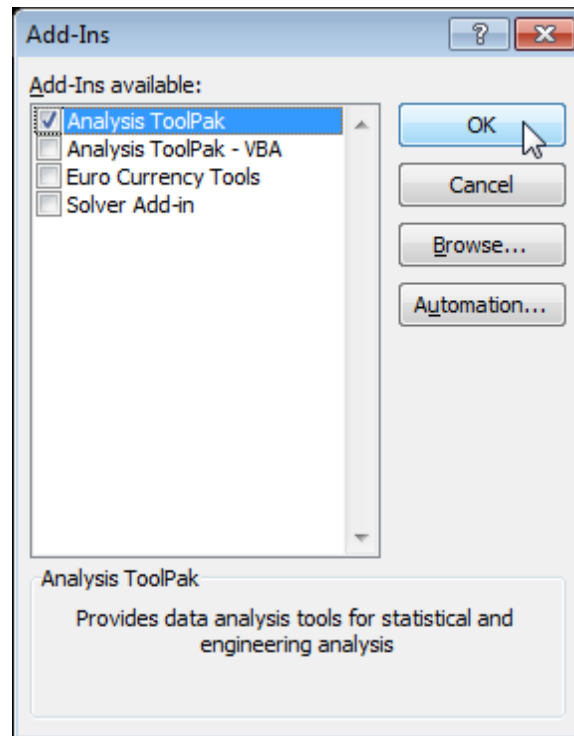


2. Under Add-ins, select Analysis ToolPak and click on the Go button.

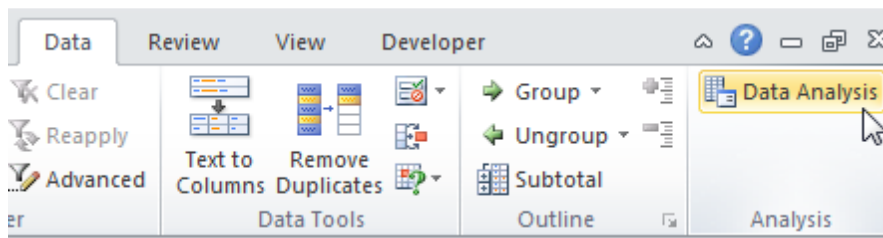


3. Check Analysis ToolPak and click on OK.

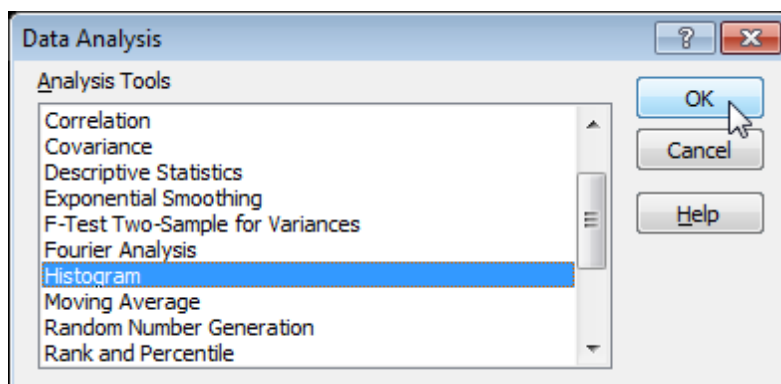




4. On the Data tab, you can now click on Data Analysis.



The following dialog box below appears.



## Examples on Data analysis

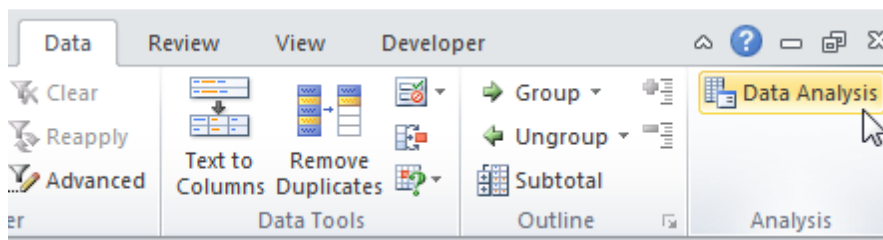
### Descriptive Statistics

You can use the Analysis Toolpak add-in to generate descriptive statistics. For example, you may have the scores of 14 participants for a test.

| M26 |        |   |
|-----|--------|---|
|     | A      | B |
| 1   | Scores |   |
| 2   | 82     |   |
| 3   | 93     |   |
| 4   | 91     |   |
| 5   | 69     |   |
| 6   | 96     |   |
| 7   | 61     |   |
| 8   | 88     |   |
| 9   | 58     |   |
| 10  | 59     |   |
| 11  | 100    |   |
| 12  | 93     |   |
| 13  | 71     |   |
| 14  | 78     |   |
| 15  | 98     |   |
| 16  |        |   |
| 17  |        |   |

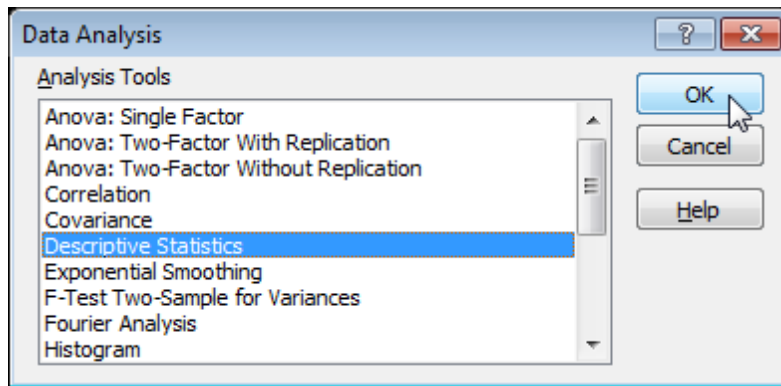
To generate descriptive statistics for these scores, execute the following steps.

1. On the Data tab, click Data Analysis.

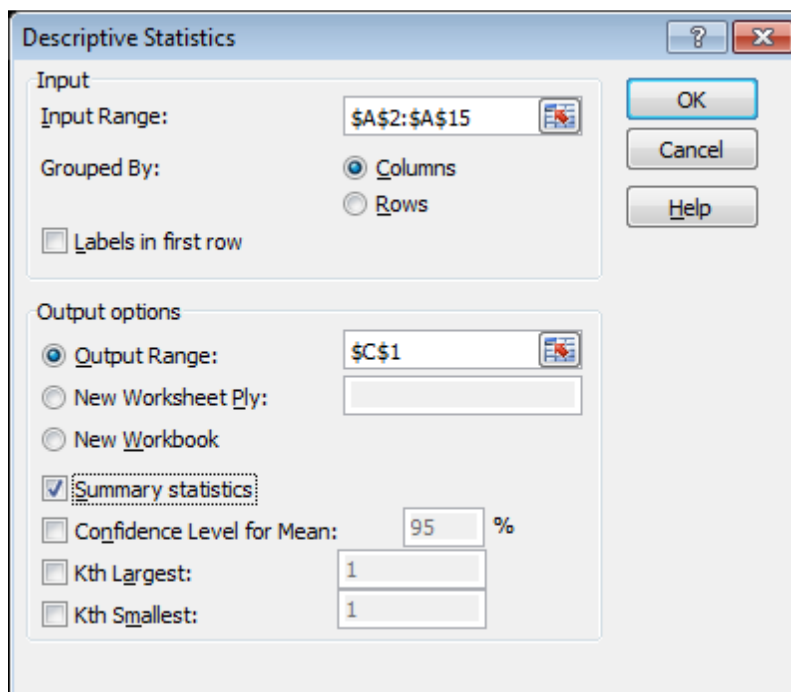


Note: can't find the Data Analysis button? Click [here](#) to load the Analysis ToolPak add-in.

2. Select Descriptive Statistics and click OK.



3. Select the range A2:A15 as the Input Range.
4. Select cell C1 as the Output Range.
5. Make sure Summary statistics is checked.



6. Click OK.

Result:

| L28 |        | fx |                    |              |   |
|-----|--------|----|--------------------|--------------|---|
|     | A      | B  | C                  | D            | E |
| 1   | Scores |    | Column1            |              |   |
| 2   | 82     |    |                    |              |   |
| 3   | 93     |    | Mean               | 81.21428571  |   |
| 4   | 91     |    | Standard Error     | 4.045318243  |   |
| 5   | 69     |    | Median             | 85           |   |
| 6   | 96     |    | Mode               | 93           |   |
| 7   | 61     |    | Standard Deviation | 15.13619489  |   |
| 8   | 88     |    | Sample Variance    | 229.1043956  |   |
| 9   | 58     |    | Kurtosis           | -1.426053506 |   |
| 10  | 59     |    | Skewness           | -0.402108004 |   |
| 11  | 100    |    | Range              | 42           |   |
| 12  | 93     |    | Minimum            | 58           |   |
| 13  | 71     |    | Maximum            | 100          |   |
| 14  | 78     |    | Sum                | 1137         |   |
| 15  | 98     |    | Count              | 14           |   |
| 16  |        |    |                    |              |   |
| 17  |        |    |                    |              |   |

## Statistical tests using excel

### 1- Analysis of variance (ANOVA)

#### - One Way ANOVA

$\alpha = 0.05$ .

#### Hypotheses testing:

$H_0: \mu_1 = \mu_2 = \dots = \mu_k$

$H_1$ : at least one of the means is different.

#### Test statistic:

$$F = \frac{MSA}{MSE}$$

#### Critical region:

Reject  $H_0$  if  $F > F_{1-\alpha, (v_1, v_2)}$

Or

$p - value \leq \alpha$

#### Decision:

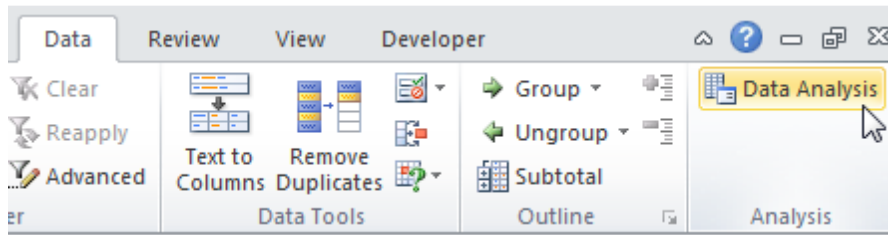
This example teaches you how to perform a single factor ANOVA (analysis of variance) in Excel. A single factor or one-way ANOVA is used to test the null hypothesis that the means of several populations are all equal.

Below you can find the salaries of people who have a degree in economics, medicine or history.

|    | A         | B        | C       | D |
|----|-----------|----------|---------|---|
| 1  | economics | medicine | history |   |
| 2  | 42        | 69       | 35      |   |
| 3  | 53        | 54       | 40      |   |
| 4  | 49        | 58       | 53      |   |
| 5  | 53        | 64       | 42      |   |
| 6  | 43        | 64       | 50      |   |
| 7  | 44        | 55       | 39      |   |
| 8  | 45        | 56       | 55      |   |
| 9  | 52        |          | 39      |   |
| 10 | 54        |          | 40      |   |
| 11 |           |          |         |   |
| 12 |           |          |         |   |

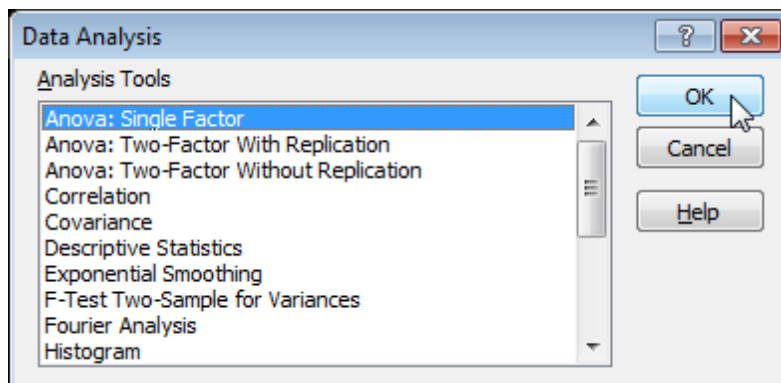
To perform a single factor ANOVA, execute the following steps.

1. On the Data tab, click Data Analysis.




Note: can't find the Data Analysis button? Click [here](#) to load the Analysis ToolPak add-in.


2. Select Anova: Single Factor and click OK.



3. Click in the Input Range box and select the range A2:C10.
4. Click in the Output Range box and select cell E1.

**Anova: Single Factor**

Input  
 Input Range:    
 Grouped By: ☒ Columns ☐ Rows  
☐ Labels in first row  
 Alpha:

Output options  
☒ Output Range:    
☐ New Worksheet Ply:   
☐ New Workbook

OK Cancel Help

5. Click OK.

Result:

| E                    | F       | G   | H        | I        | J        | K        |
|----------------------|---------|-----|----------|----------|----------|----------|
| Anova: Single Factor |         |     |          |          |          |          |
|                      |         |     |          |          |          |          |
| SUMMARY              |         |     |          |          |          |          |
| Groups               | Count   | Sum | Average  | Variance |          |          |
| Column 1             | 9       | 435 | 48.33333 | 23.5     |          |          |
| Column 2             | 7       | 420 | 60       | 32.33333 |          |          |
| Column 3             | 9       | 393 | 43.66667 | 50.5     |          |          |
|                      |         |     |          |          |          |          |
|                      |         |     |          |          |          |          |
| ANOVA                |         |     |          |          |          |          |
| Source of Variation  | SS      | df  | MS       | F        | P-value  | F crit   |
| Between Groups       | 1085.84 | 2   | 542.92   | 15.19623 | 7.16E-05 | 3.443357 |
| Within Groups        | 786     | 22  | 35.72727 |          |          |          |
|                      |         |     |          |          |          |          |
| Total                | 1871.84 | 24  |          |          |          |          |

$$\alpha = 0.05.$$

**Hypotheses testing:**

$$H_0: \mu_1 = \mu_2 = \mu_3$$

$H_1$ : at least one of the means is different.

**Test statistic:**

$$F = \frac{MSA}{MSE} = 15.19623$$

**Critical region:**

$$F_{1-\alpha, (v_1, v_2)} = F_{crit} = 3.443357$$

$$p - value = 0.00007163$$

Reject  $H_0$  if  $F > 3.443$

Or

$$p - value \leq 0.05$$

**Decision:**

Therefore, we reject the null hypothesis. The means of the three populations are not all equal. At least one of the means is different. However, the ANOVA does not tell you where the difference lies. You need a t-Test to test each pair of means.



## - Two-Factor Analysis of Variance

$\alpha = 0.05$ .

The three hypotheses to be tested are as follows:

### **Hypotheses testing:**

1.  $H_0: a_1 = a_2 = \dots = a_a = 0$

$H_1$ : At least one of the  $a_i$  is not equal to zero.

2.  $H_0: \beta_1 = \beta_2 = \dots = \beta_b = 0$

$H_1$ : At least one of the  $\beta_j$  is not equal to zero.

3.  $H_0: (a\beta)_{11} = (a\beta)_{12} = \dots = (a\beta)_{ab} = 0$

$H_1$ : At least one of the  $(a\beta)_{ij}$  is not equal to zero.

### **Critical region:**

$p - value \leq \alpha$

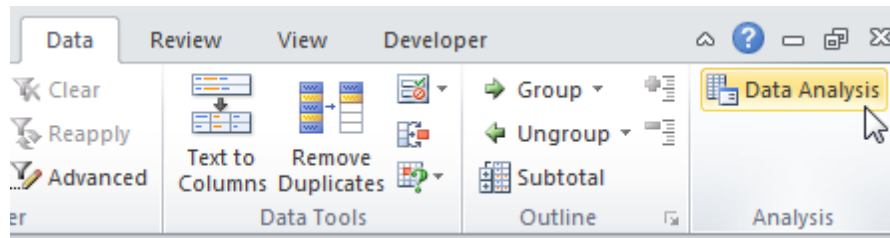
### **Decision:**

## - ANOVA two ways with Replication

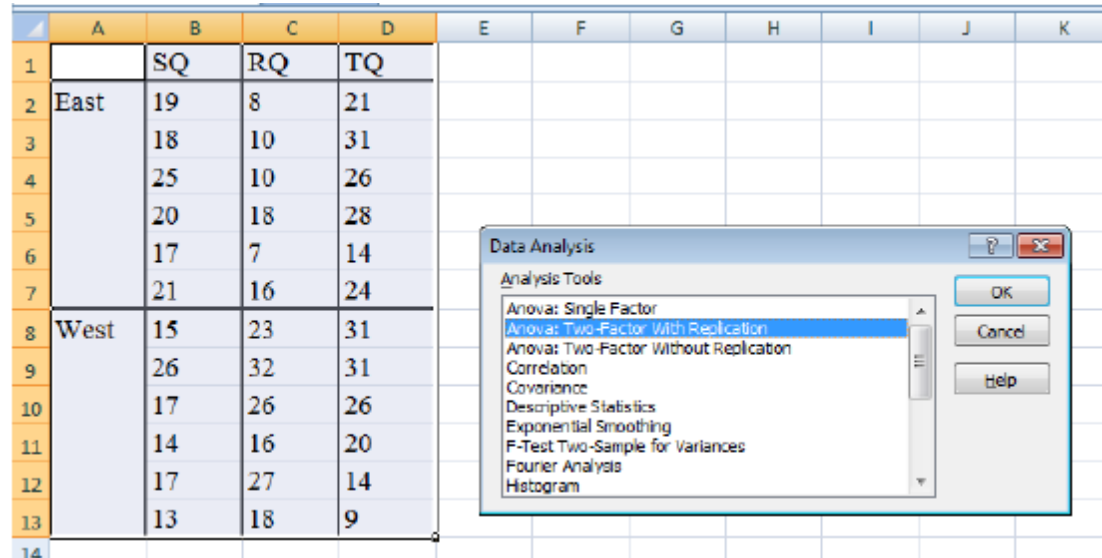
In the following example, the cost of three swimming programs in two regions in the East and the West

|      | SQ | RQ | TQ |
|------|----|----|----|
| East | 19 | 8  | 21 |
|      | 18 | 10 | 31 |
|      | 25 | 10 | 26 |
|      | 20 | 18 | 28 |
|      | 17 | 7  | 14 |
|      | 21 | 16 | 24 |
| West | 15 | 23 | 31 |
|      | 28 | 32 | 31 |
|      | 17 | 26 | 26 |
|      | 14 | 16 | 20 |
|      | 17 | 27 | 14 |
|      | 13 | 18 | 9  |

1. On the Data tab, click Data Analysis.

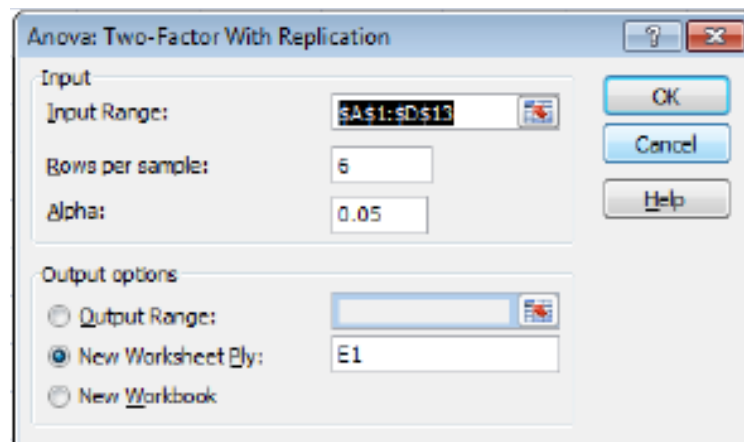


2. Select Anova: Two-Factor With Replication and click OK.



3. Click in the Input Range box and select the range A1:D13.

4. Click in the Output Range box and select cell E2.



5. Click OK.

Result:

|                                    |           |           |           |          |                |               |
|------------------------------------|-----------|-----------|-----------|----------|----------------|---------------|
| Anova: Two-Factor With Replication |           |           |           |          |                |               |
| SUMMARY                            | SQ        | RQ        | TQ        | Total    |                |               |
| <i>East</i>                        |           |           |           |          |                |               |
| Count                              | 6         | 6         | 6         | 18       |                |               |
| Sum                                | 120       | 69        | 144       | 333      |                |               |
| Average                            | 20        | 11.5      | 24        | 18.5     |                |               |
| Variance                           | 8         | 19.9      | 35.6      | 47.44118 |                |               |
| <i>West</i>                        |           |           |           |          |                |               |
| Count                              | 6         | 6         | 6         | 18       |                |               |
| Sum                                | 102       | 142       | 131       | 375      |                |               |
| Average                            | 17        | 23.66667  | 21.83333  | 20.83333 |                |               |
| Variance                           | 22        | 35.46667  | 82.96667  | 49.67647 |                |               |
| <i>Total</i>                       |           |           |           |          |                |               |
| Count                              | 12        | 12        | 12        |          |                |               |
| Sum                                | 222       | 211       | 275       |          |                |               |
| Average                            | 18.5      | 17.58333  | 22.91667  |          |                |               |
| Variance                           | 16.09091  | 65.53788  | 55.17424  |          |                |               |
| ANOVA                              |           |           |           |          |                |               |
| <i>Source of Variation</i>         | <i>SS</i> | <i>df</i> | <i>MS</i> | <i>F</i> | <i>P-value</i> | <i>F crit</i> |
| Sample                             | 49        | 1         | 49        | 1.441648 | 0.239268       | 4.170877      |
| Columns                            | 195.1667  | 2         | 97.58333  | 2.871036 | 0.072297       | 3.31583       |
| Interaction                        | 436.1667  | 2         | 218.0833  | 6.416313 | 0.004788       | 3.31583       |
| Within                             | 1019.667  | 30        | 33.98889  |          |                |               |
| Total                              | 1700      | 35        |           |          |                |               |

$$\alpha = 0.05.$$

### **1) Hypotheses testing:**

$$H_0: a_{East} = a_{West} = 0$$

$H_1$ : at least one of the means is different.

### **Test statistic:**

$$F = 1.4416$$

### **Critical region:**

$$F_{1-\alpha, (v_1, v_2)} = F_{crit} = 4.1708$$

$$p - value = 0.2392$$

Reject  $H_0$  if  $F > 4.1708$  Or  $p - value \leq 0.05$

**Decision:**

Therefore, we not reject the null hypothesis. There are no difference in the means of the cost between the two regions in the east and the west.

**2) Hypotheses testing:**

$$H_0: \beta_{SQ} = \beta_{RQ} = \beta_{TQ} = 0$$

$H_1$ : at least one of the means is different.

**Test statistic:**

$$F = 2.871$$

**Critical region:**

$$F_{1-\alpha, (v_1, v_2)} = F_{crit} = 3.3158$$

$$p - value = 0.0722$$

Reject  $H_0$  if  $F > 3.3158$  Or  $p - value \leq 0.05$

**Decision:**

Therefore, we not reject the null hypothesis. There was no significant difference between the mean cost of the three programs.

**3) Hypotheses testing:**

$$H_0: a\beta_{East, SQ} = a\beta_{East, RQ} = a\beta_{East, TQ} = a\beta_{West, SQ} = a\beta_{West, RQ} = a\beta_{West, TQ} = 0$$

$H_1$ : at least one of the means is different.

**Test statistic:**

$$F = 6.4163$$

**Critical region:**

$$F_{1-\alpha, (v_1, v_2)} = F \text{ crit} = 3.3158$$

$$p - \text{value} = 0.0047$$

Reject  $H_0$  if  $F > 3.3158$  Or  $p - \text{value} \leq 0.05$

**Decision:**

Therefore, we reject the null hypothesis. There is interaction between the two factors (region, type of program).

## **- ANOVA two ways without Replication**

In the following example, the price of three swimming programs in six areas

|   | SQ | RQ | TQ |
|---|----|----|----|
| 1 | 19 | 8  | 21 |
| 2 | 18 | 10 | 31 |
| 3 | 25 | 10 | 26 |
| 4 | 20 | 18 | 28 |
| 5 | 17 | 7  | 14 |
| 6 | 21 | 16 | 24 |

$\alpha = 0.05$ .

The two hypotheses to be tested are as follows:

### **Hypotheses testing:**

1.  $H_0: a_1 = a_2 = \dots = a_a = 0$

$H_1$ : At least one of the  $a_i$  is not equal to zero.

2.  $H_0: \beta_1 = \beta_2 = \dots = \beta_b = 0$

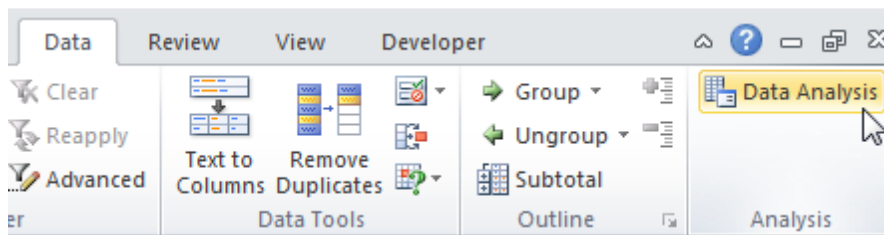
$H_1$ : At least one of the  $\beta_j$  is not equal to zero.

### **Critical region:**

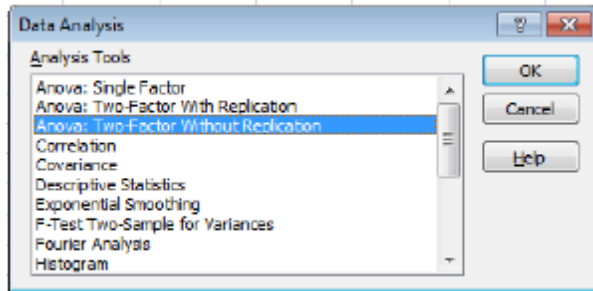
$p - \text{value} \leq \alpha$

### **Decision:**

1. On the Data tab, click Data Analysis.

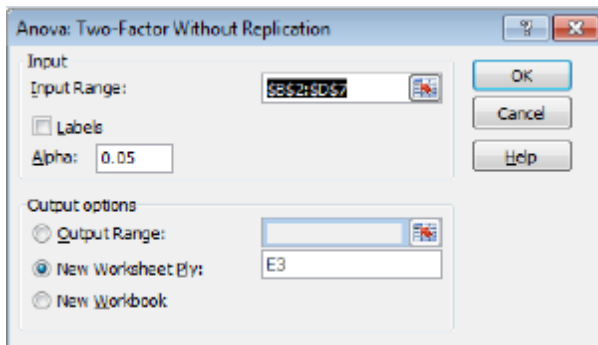


2. Select Anova: Two-Factor With Replication and click OK.



3. Click in the Input Range box and select the range B2:D7.

4. Click in the Output Range box and select cell E3.



5. Click OK.

Result:

| Anova: Two-Factor Without Replication |          |     |          |          |          |          |
|---------------------------------------|----------|-----|----------|----------|----------|----------|
| SUMMARY                               | Count    | Sum | Average  | Variance |          |          |
| Row 1                                 | 3        | 48  | 16       | 49       |          |          |
| Row 2                                 | 3        | 59  | 19.66667 | 112.3333 |          |          |
| Row 3                                 | 3        | 61  | 20.33333 | 80.33333 |          |          |
| Row 4                                 | 3        | 66  | 22       | 28       |          |          |
| Row 5                                 | 3        | 38  | 12.66667 | 26.33333 |          |          |
| Row 6                                 | 3        | 61  | 20.33333 | 16.33333 |          |          |
|                                       |          |     |          |          |          |          |
| Column 1                              | 6        | 120 | 20       | 8        |          |          |
| Column 2                              | 6        | 69  | 11.5     | 19.9     |          |          |
| Column 3                              | 6        | 144 | 24       | 35.6     |          |          |
|                                       |          |     |          |          |          |          |
|                                       |          |     |          |          |          |          |
| ANOVA                                 |          |     |          |          |          |          |
| Source of Variation                   | SS       | df  | MS       | F        | P-value  | F crit   |
| Rows                                  | 181.8333 | 5   | 36.36667 | 2.68059  | 0.086618 | 3.325835 |
| Columns                               | 489      | 2   | 244.5    | 18.02211 | 0.000483 | 4.102821 |
| Error                                 | 135.6667 | 10  | 13.56667 |          |          |          |
|                                       |          |     |          |          |          |          |
| Total                                 | 806.5    | 17  |          |          |          |          |

$$\alpha = 0.05.$$

### **1) Hypotheses testing:**

$$H_0: a_1 = a_2 = \dots = a_6 = 0$$

$H_1$ : at least one of the means is different.

### **Test statistic:**

$$F = 2.6805$$

### **Critical region:**

$$F_{1-\alpha, (v_1, v_2)} = F_{crit} = 3.3258$$

$$p - value = 0.0866$$



Reject  $H_0$  if  $F > 3.3258$  Or  $p - value \leq 0.05$

**Decision:**

Therefore, we not reject the null hypothesis. There are no difference in the means of the cost between the six areas.

**2) Hypotheses testing:**

$$H_0: \beta_{SQ} = \beta_{RQ} = \beta_{TQ} = 0$$

$H_1$ : at least one of the means is different.

**Test statistic:**

$$F = 18.022$$

**Critical region:**

$$F_{1-\alpha, (v_1, v_2)} = F_{crit} = 4.1028$$

$$p - value = 0.0004$$

Reject  $H_0$  if  $F > 4.1028$  Or  $p - value \leq 0.05$

**Decision:**

Therefore, we reject the null hypothesis. There is a significant difference between the mean prices of the three programs.

### 3- F-Test

This example teaches you how to perform an F-Test in Excel. The F-Test is used to test the null hypothesis that the variances of two populations are equal.

Below you can find the study hours of 6 female students and 5 male students.

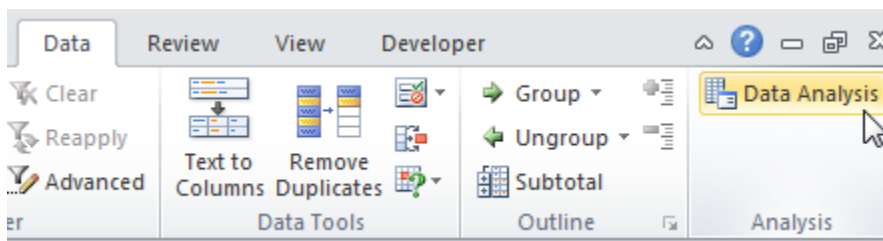
$$H_0: \sigma_1^2 = \sigma_2^2$$

$$H_1: \sigma_1^2 \neq \sigma_2^2$$

|   | A      | B    | C |
|---|--------|------|---|
| 1 | Female | Male |   |
| 2 | 26     | 23   |   |
| 3 | 25     | 30   |   |
| 4 | 43     | 18   |   |
| 5 | 34     | 25   |   |
| 6 | 18     | 28   |   |
| 7 | 52     |      |   |
| 8 |        |      |   |
| 9 |        |      |   |

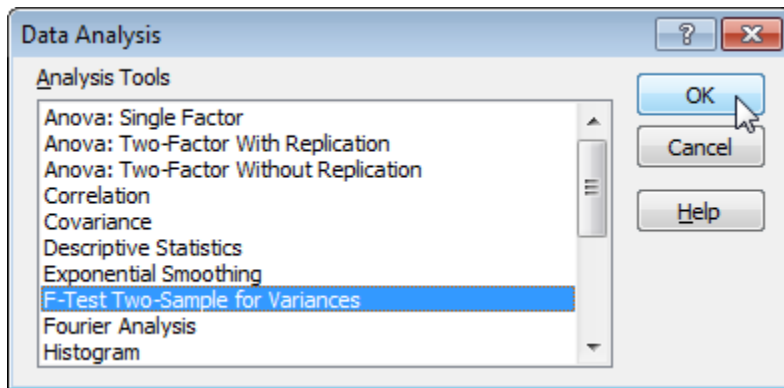
To perform an F-Test, execute the following steps.

1. On the Data tab, click Data Analysis.

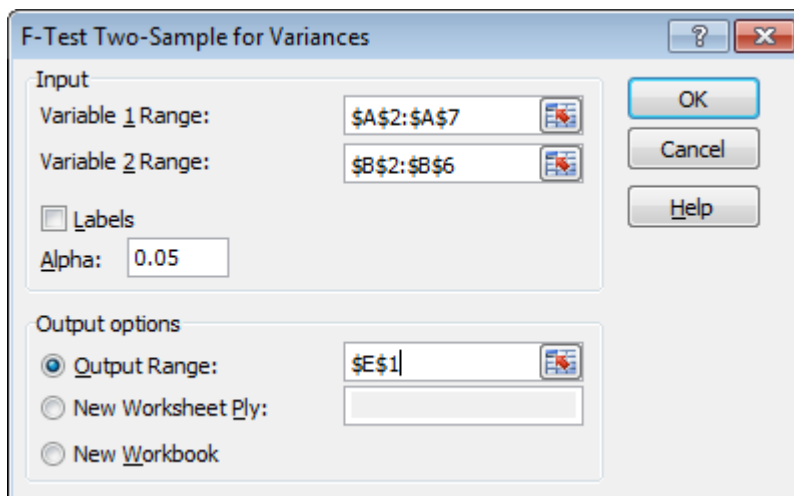


Note: can't find the Data Analysis button? Click [here](#) to load the Analysis ToolPak add-in.

2. Select F-Test Two-Sample for Variances and click OK.



3. Click in the Variable 1 Range box and select the range A2:A7.
4. Click in the Variable 2 Range box and select the range B2:B6.
5. Click in the Output Range box and select cell E1.



6. Click OK.

Result:

| E                               | F                 | G                 |
|---------------------------------|-------------------|-------------------|
| F-Test Two-Sample for Variances |                   |                   |
|                                 |                   |                   |
|                                 | <i>Variable 1</i> | <i>Variable 2</i> |
| Mean                            | 33                | 24.8              |
| Variance                        | 160               | 21.7              |
| Observations                    | 6                 | 5                 |
| df                              | 5                 | 4                 |
| F                               | 7.373271889       |                   |
| P(F<=f) one-tail                | 0.037888376       |                   |
| F Critical one-tail             | 6.256056502       |                   |

**Important:** be sure that the variance of Variable 1 is higher than the variance of Variable 2. This is the case,  $160 > 21.7$ . If not, swap your data. As a result, Excel calculates the correct F value, which is the ratio of Variance 1 to Variance 2 ( $F = 160 / 21.7 = 7.373$ ).

**Conclusion:** if  $F > F$  Critical one-tail, we reject the null hypothesis. This is the case,  $7.373 > 6.256$ . Therefore, we reject the null hypothesis. The variances of the two populations are unequal.

#### 4- t-Test

This example teaches you how to perform a t-Test in Excel. The t-Test is used to test the null hypothesis that the means of two populations are equal.

Below you can find the study hours of 6 female students and 5 male students.

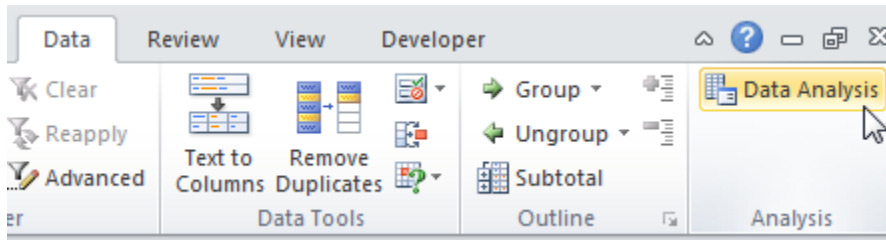
$H_0: \mu_1 - \mu_2 = 0$

$H_1: \mu_1 - \mu_2 \neq 0$

| H15      fx |        |      |   |
|-------------|--------|------|---|
|             | A      | B    | C |
| 1           | Female | Male |   |
| 2           | 26     | 23   |   |
| 3           | 25     | 30   |   |
| 4           | 43     | 18   |   |
| 5           | 34     | 25   |   |
| 6           | 18     | 28   |   |
| 7           | 52     |      |   |
| 8           |        |      |   |
| 9           |        |      |   |

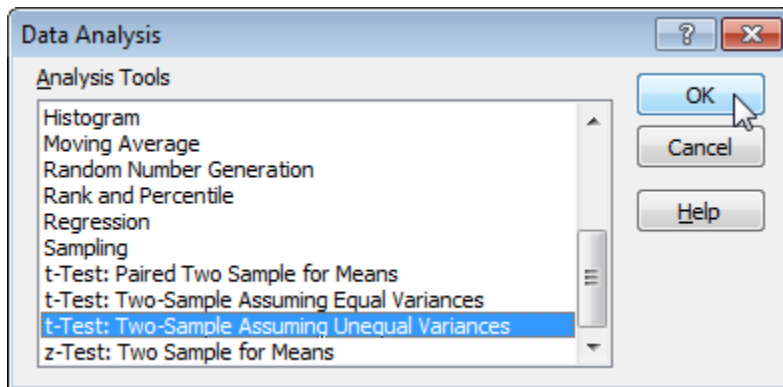
To perform a t-Test, execute the following steps.

1. First, perform an F-Test to determine if the variances of the two populations are equal. This is not the case.
2. On the Data tab, click Data Analysis.



Note: can't find the Data Analysis button? Click [here](#) to load the Analysis ToolPak add-in.

3. Select t-Test: Two-Sample Assuming Unequal Variances and click OK.

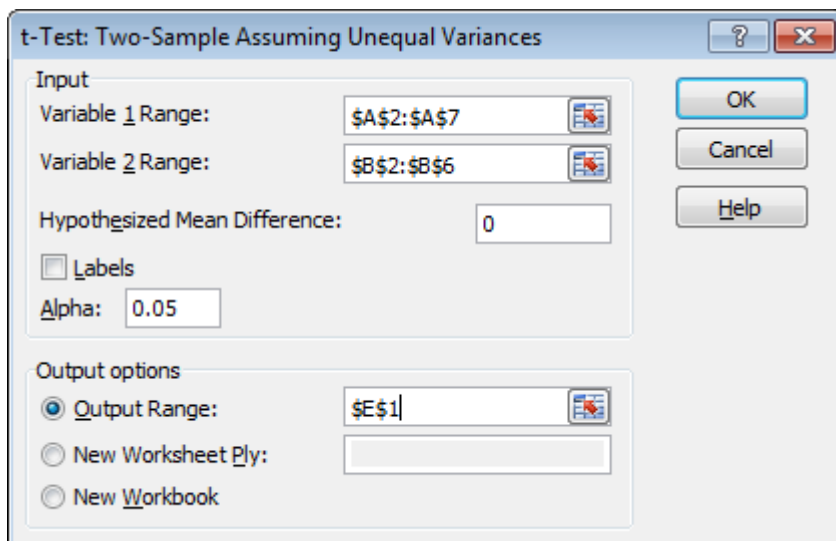


4. Click in the Variable 1 Range box and select the range A2:A7.

5. Click in the Variable 2 Range box and select the range B2:B6.

6. Click in the Hypothesized Mean Difference box and type 0 ( $H_0: \mu_1 - \mu_2 = 0$ ).

7. Click in the Output Range box and select cell E1.



8. Click OK.

Result:

| E   | F                 | G                 |
|---|-------------------|-------------------|
| t-Test: Two-Sample Assuming Unequal Variances |                   |                   |
|   |                   |                   |
|   | <i>Variable 1</i> | <i>Variable 2</i> |
| Mean  | 33                | 24.8              |
| Variance                                      | 160               | 21.7              |
| Observations                                  | 6                 | 5                 |
| Hypothesized Mean Difference                  | 0                 |                   |
| df  | 7                 |                   |
| t Stat  | 1.47260514        |                   |
| P(T<=t) one-tail                              | 0.092170202       |                   |
| t Critical one-tail                           | 1.894578605       |                   |
| P(T<=t) two-tail                              | 0.184340405       |                   |
| t Critical two-tail                           | 2.364624252       |                   |

### Conclusion:

We do a two-tail test (inequality). If  $t \text{ Stat} < -t \text{ Critical two-tail}$  or  $t \text{ Stat} > t \text{ Critical two-tail}$ , we reject the null hypothesis. This is not the case,  $-2.365 < 1.473 < 2.365$ . Therefore, we do not reject the null hypothesis. The observed difference between the sample means (33 - 24.8) is not convincing enough to say that the average number of study hours between female and male students differ significantly.

## 5- Paired Sample t Test

In paired sample hypothesis testing, a sample from the population is chosen and two measurements for each element in the sample are taken. Each set of measurements is considered a sample. Unlike the hypothesis testing studied so far, the two samples are not independent of one another. Paired samples are also called matched samples or repeated measures.

### Example:

A clinic provides a program to help their clients lose weight and asks a consumer agency to investigate the effectiveness of the program. The agency takes a sample of 15 people, weighing each person in the sample before the program begins and 3 months later to produce the table below.

|    | A                                     | B      | C     | D          |
|----|---------------------------------------|--------|-------|------------|
| 1  | Two sample t test with paired samples |        |       |            |
| 2  |                                       |        |       |            |
| 3  | Person                                | Before | After | Difference |
| 4  | 1                                     | 210    | 197   | 13         |
| 5  | 2                                     | 205    | 195   | 10         |
| 6  | 3                                     | 193    | 191   | 2          |
| 7  | 4                                     | 182    | 174   | 8          |
| 8  | 5                                     | 259    | 236   | 23         |
| 9  | 6                                     | 239    | 226   | 13         |
| 10 | 7                                     | 164    | 157   | 7          |
| 11 | 8                                     | 197    | 196   | 1          |
| 12 | 9                                     | 222    | 201   | 21         |
| 13 | 10                                    | 211    | 196   | 15         |
| 14 | 11                                    | 187    | 181   | 6          |
| 15 | 12                                    | 175    | 164   | 11         |
| 16 | 13                                    | 186    | 181   | 5          |
| 17 | 14                                    | 243    | 229   | 14         |
| 18 | 15                                    | 246    | 231   | 15         |
| 19 |                                       |        |       |            |
| 20 | mean                                  |        |       | 10.933333  |
| 21 | std dev                               |        |       | 6.3298236  |

Determine whether the program is effective?

## Solution

Let  $x$  = the difference in weight 3 months after the program starts. The null hypothesis is:

$H_0: \mu = 0$ ; i.e. any differences in weight is due to chance

We use the Excel's t-Test: Paired Two Sample for Means data analysis tool or the T Test. The output from the Excel data analysis tool is shown below:

| t-Test: Paired Two Sample for Means |          |       |
|-------------------------------------|----------|-------|
|                                     | Before   | After |
| Mean                                | 207.9333 | 197   |
| Variance                            | 815.781  | 595   |
| Observations                        | 15       | 15    |
| Pearson Correlation                 | 0.98372  |       |
| Hypothesized Mean Difference        | 0        |       |
| df                                  | 14       |       |
| t Stat                              | 6.6897   |       |
| P(T<=t) one-tail                    | 5.14E-06 |       |
| t Critical one-tail                 | 1.76131  |       |
| P(T<=t) two-tail                    | 1.03E-05 |       |
| t Critical two-tail                 | 2.144787 |       |

Note that the mean differences are the same, but the standard deviation for the paired sample case is lower, which results in a higher t-stat and a lower p-value. This is generally true.

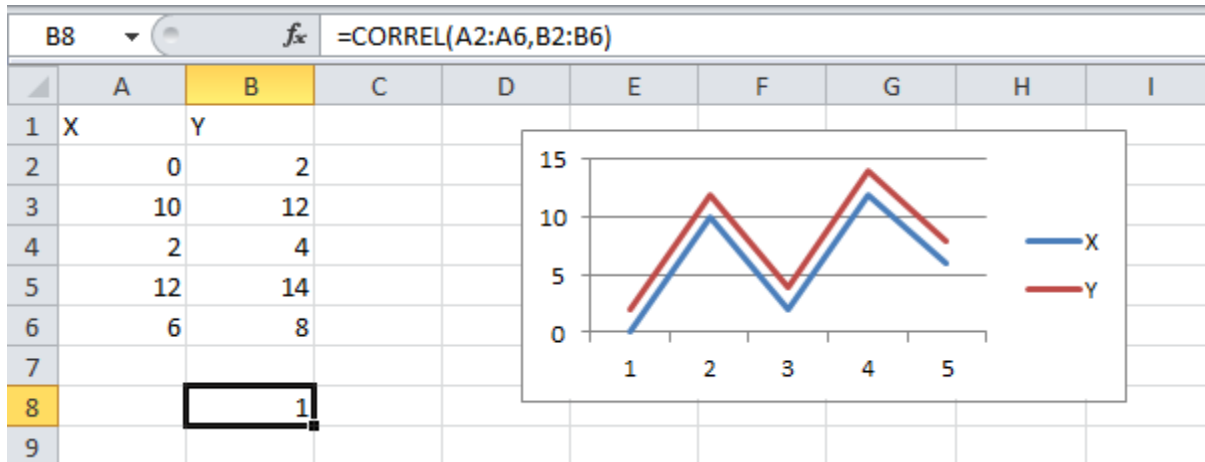
**Observation:** Since the two sample paired data case is equivalent to the one sample case.



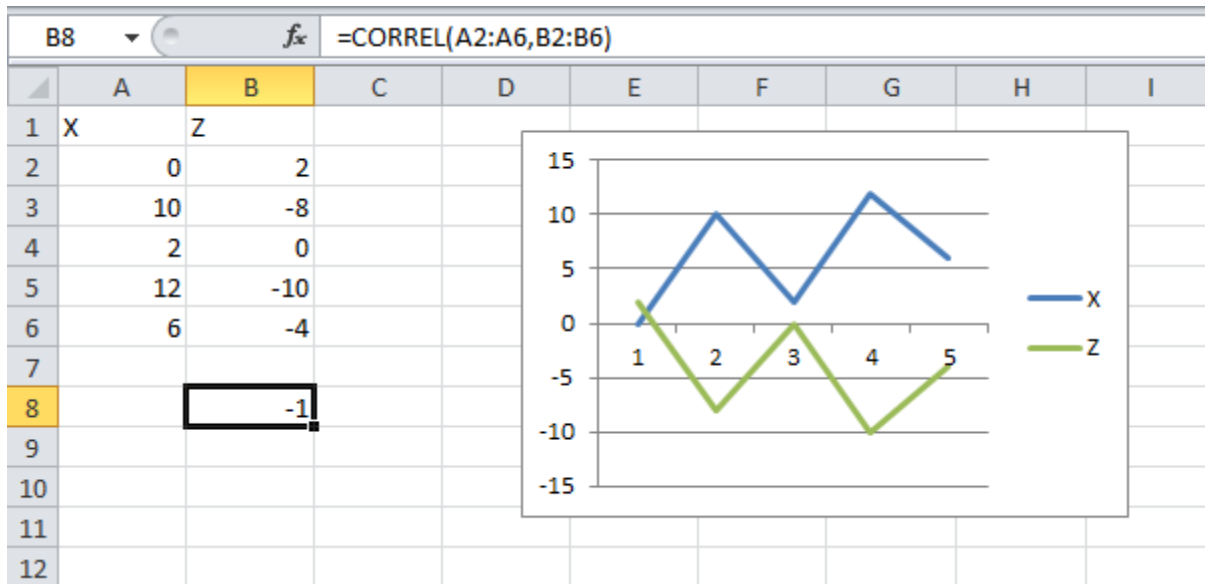
## 6- Correlation

The correlation coefficient (a value between -1 and +1) tells you how strongly two variables are related to each other. We can use the CORREL function or the Analysis Toolpak add-in in Excel to find the correlation coefficient between two variables.

- A correlation coefficient of +1 indicates a perfect positive correlation. As variable X increases, variable Y increases. As variable X decreases, variable Y decreases.



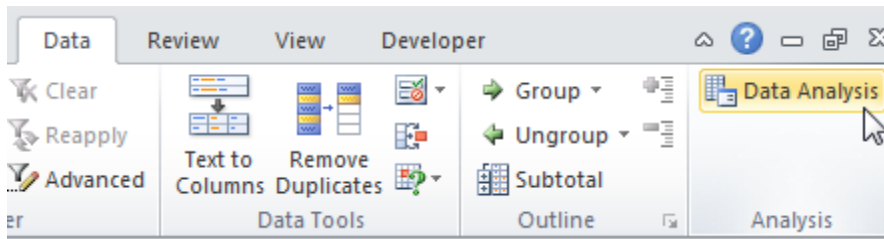
- A correlation coefficient of -1 indicates a perfect negative correlation. As variable X increases, variable Z decreases. As variable X decreases, variable Z increases.



- A correlation coefficient near 0 indicates no correlation.

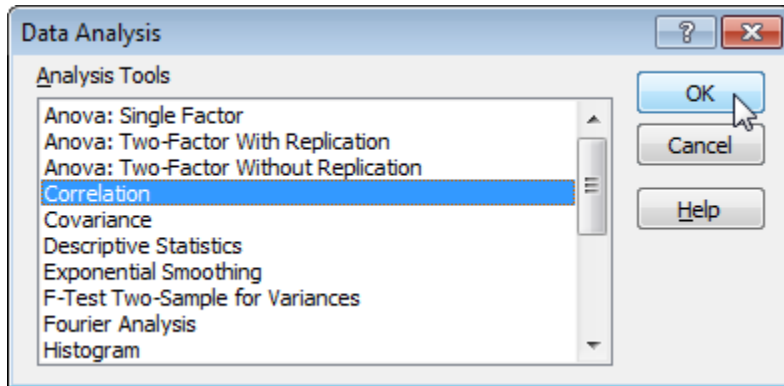
To use the Analysis Toolpak add-in in Excel to quickly generate correlation coefficients between multiple variables, execute the following steps.

1. On the Data tab, click Data Analysis.

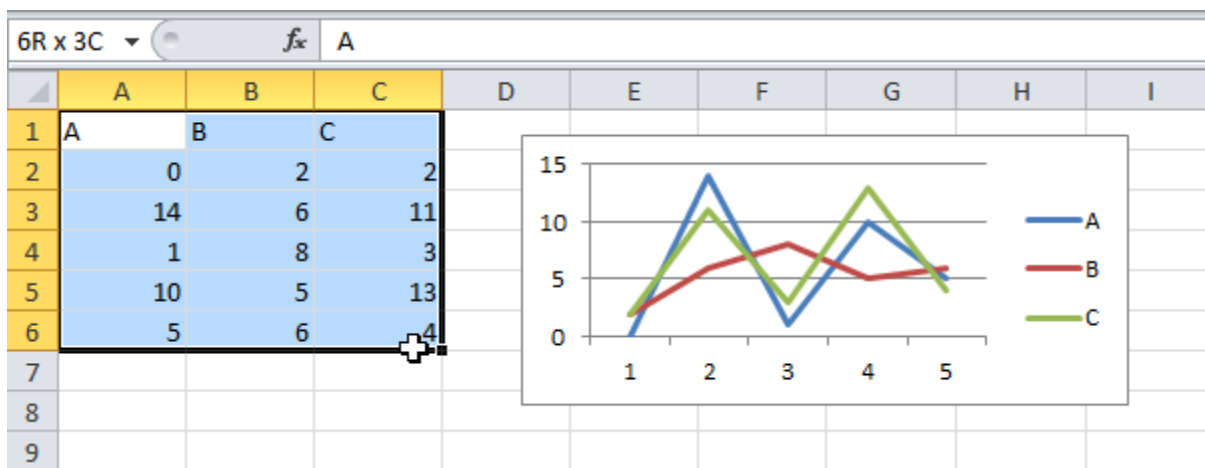


Note: can't find the Data Analysis button? Click [here](#) to load the Analysis ToolPak add-in.

2. Select Correlation and click OK.



3. For example, select the range A1:C6 as the Input Range.



4. Check Labels in first row.

5. Select cell A9 as the Output Range.

6. Click OK.

**Correlation**

Input

Input Range:

Grouped By: ☒ Columns ☐ Rows

☒ Labels in first row

Output options

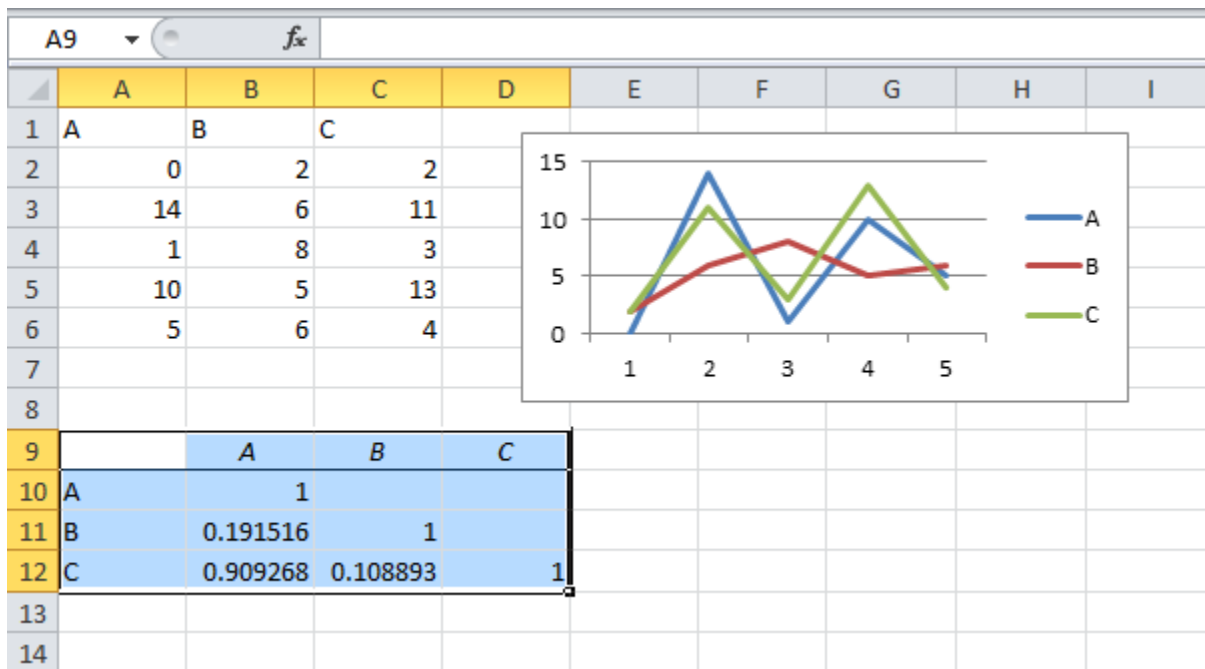
☒ Output Range:

☐ New Worksheet Ply:

☐ New Workbook

OK Cancel Help

Result.



**Conclusion:** variables A and C are positively correlated (0.91). Variables A and B are not correlated (0.19). Variables B and C are also not correlated (0.11) . You can verify these conclusions by looking at the graph.

## 7-Regression

This example teaches you how to perform a regression analysis in Excel and how to interpret the Summary Output.

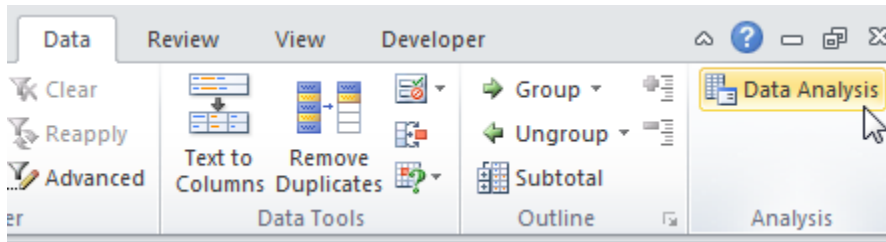
In this study a random sample of service call records for a computer repair operation were examined and the length of each call (in minutes) and the number of components repaired or replaced were recorded. The data is given below.

| Minutes | Units |
|---------|-------|
| 23      | 1     |
| 29      | 2     |
| 49      | 3     |
| 64      | 4     |
| 74      | 4     |
| 87      | 5     |
| 96      | 6     |
| 97      | 6     |
| 109     | 7     |
| 119     | 8     |
| 149     | 9     |
| 145     | 9     |
| 154     | 10    |
| 166     | 10    |

Below you can find our data. The big question is:

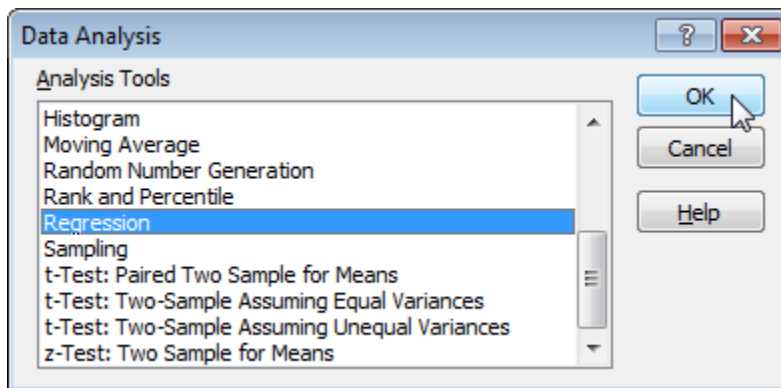
is there a relation between Minutes (Output) and Units (Input). In other words: can we predict Minutes if we know the unites?

1. On the Data tab, click Data Analysis.



Note: can't find the Data Analysis button? Click [here](#) to load the Analysis ToolPak add-in.

2. Select Regression and click OK.



3. Select the Y Range (A2:A15). This is the predictor variable (also called dependent variable).

4. Select the X Range(B2:B15). These are the explanatory variables (also called independent variables). These columns must be adjacent to each other.


5. Check Labels.


6. Select an Output Range.

8. Click OK.

**Regression** ? X

**Input**


Input Y Range:  

Input X Range:  

☒ Labels ☐ Constant is Zero

☐ Confidence Level:  %

**Output options**

☒ Output Range:  

☐ New Worksheet Ply:

☐ New Workbook

**Residuals**

☐ Residuals ☐ Residual Plots

☐ Standardized Residuals ☐ Line Fit Plots

**Normal Probability**

☐ Normal Probability Plots

OK Cancel Help

Excel produces the following Summary Output (rounded to 3 decimal places).

|         |       |  |                       |                |           |           |           |                |             |             |        |
|---------|-------|--|-----------------------|----------------|-----------|-----------|-----------|----------------|-------------|-------------|--------|
| Minutes | Units |  |                       |                |           |           |           |                |             |             |        |
| 23      | 1     |  | SUMMARY OUTPUT        |                |           |           |           |                |             |             |        |
| 29      | 2     |  |                       |                |           |           |           |                |             |             |        |
| 49      | 3     |  | Regression Statistics |                |           |           |           |                |             |             |        |
| 64      | 4     |  | Multiple R            | 0.994          |           |           |           |                |             |             |        |
| 74      | 4     |  | R Square              | 0.987          |           |           |           |                |             |             |        |
| 87      | 5     |  | Adjusted R            | 0.986          |           |           |           |                |             |             |        |
| 96      | 6     |  | Standard Error        | 5.392          |           |           |           |                |             |             |        |
| 97      | 6     |  | Observations          | 14.000         |           |           |           |                |             |             |        |
| 109     | 7     |  |                       |                |           |           |           |                |             |             |        |
| 119     | 8     |  | ANOVA                 |                |           |           |           |                |             |             |        |
| 149     | 9     |  |                       | df             | SS        | MS        | F         | Significance F |             |             |        |
| 145     | 9     |  | Regression            | 1.000          | 27419.509 | 27419.509 | 943.201   | 0.000          |             |             |        |
| 154     | 10    |  | Residual              | 12.000         | 348.848   | 29.071    |           |                |             |             |        |
| 166     | 10    |  | Total                 | 13.000         | 27768.357 |           |           |                |             |             |        |
|         |       |  |                       |                |           |           |           |                |             |             |        |
|         |       |  |                       |                |           |           |           |                |             |             |        |
|         |       |  | Coefficients          | Standard Error | t Stat    | P-value   | Lower 95% | Upper 95%      | Lower 95.0% | Upper 95.0% |        |
|         |       |  | Intercept             | 4.162          | 3.355     | 1.240     | 0.239     | -3.148         | 11.472      | -3.148      | 11.472 |
|         |       |  | Units                 | 15.509         | 0.505     | 30.712    | 0.000     | 14.409         | 16.609      | 14.409      | 16.609 |

## Results

The regression line is:  $y = \text{Minutes} = 4.162 + 15.509 * \text{Units}$ . In other words, for increasing the units by one, the Time Minutes increases by 15.509, while there is 4.162 minutes does not depend on the unites.

## Part 3

### Some Statistical Charts in Excel

Excel provides fairly extensive capabilities for creating graphs, what Excel calls **charts**. You can access Excel's charting capabilities by selecting **Insert > Charts**. We will describe how to create bar and line charts here. Elsewhere on the website we describe how to create [scatter charts](#). Other types of charts are created in a similar manner. Once a chart is created three new ribbons are accessible, namely **Design**, **Layout** and **Format**. These are used to refine the chart created.

#### 1- Bar charts

To create a bar chart, execute the following steps:

1. Enter the data that you are charting into a worksheet.
2. Highlight the data range and select **Insert > Charts|Column**. A list of bar chart types is displayed. As usual you can place the mouse pointer over the picture of any chart type to get a brief description of that chart type. E.g. the first type is a 2-dimensional side-by-side bar chart while second choice is a 2-dimensional stacked bar chart.
3. Use the **Design**, **Layout** and **Format** ribbons to refine the chart. At any time, you can click on the chart to get access to these ribbons.

We now demonstrate how to create a bar chart via the following example.

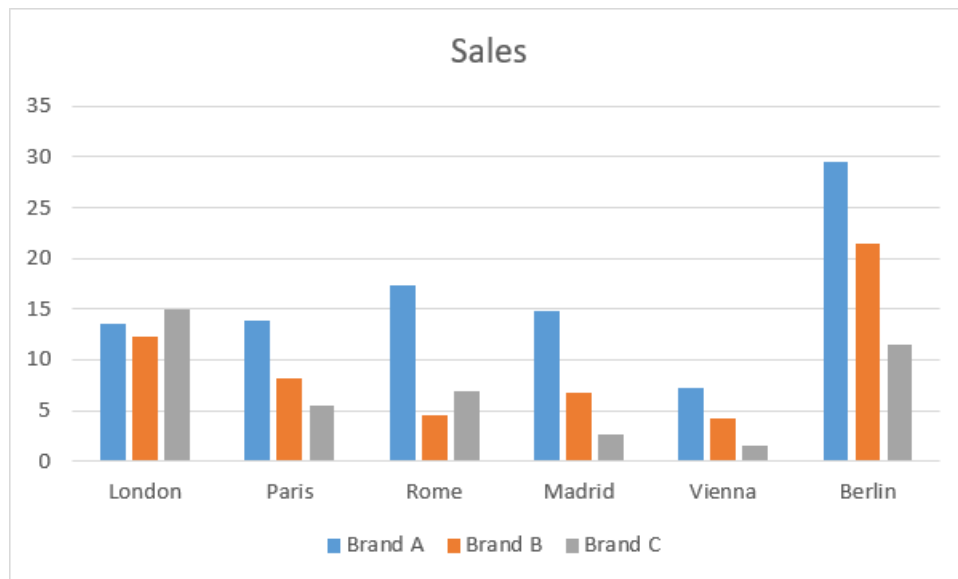


## Example

The following data represents the sales in millions of Euros in for a certain product has three brands A, B and C

| City   | Brand A | Brand B | Brand C |
|--------|---------|---------|---------|
| London | 13.5    | 12.3    | 15      |
| Paris  | 13.8    | 8.1     | 5.5     |
| Rome   | 17.3    | 4.5     | 6.9     |
| Madrid | 14.8    | 6.8     | 2.7     |
| Vienna | 7.2     | 4.2     | 1.6     |
| Berlin | 29.5    | 21.4    | 11.5    |

The first step is to enter the data into the worksheet. We next highlight the range the data including the row and column headings, and select **Insert > Charts|Column**.

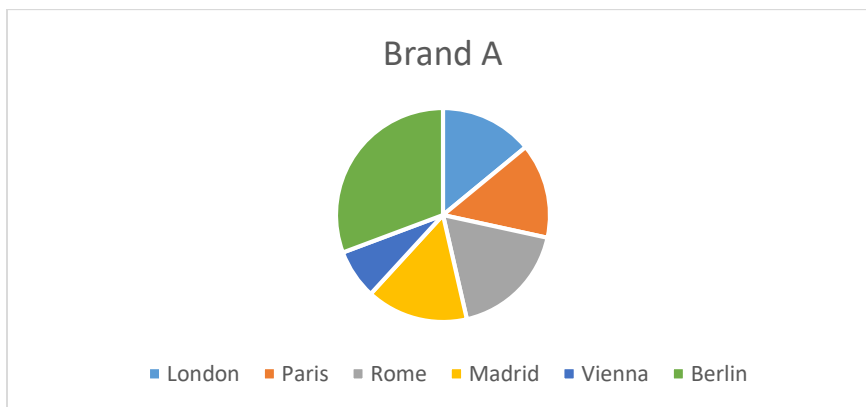


The resulting chart, although initially the chart does not contain a chart title or axes titles. To add a chart title click on the chart, select **Layout > Labels|Chart Title** and then choose **Above Chart** and enter the title sales. The title of the horizontal axis can be added in a similar manner by selecting **Layout > Labels|Axis Titles > Primary Horizontal Axis Title > Title Below Axis** and entering the word City. Finally, the

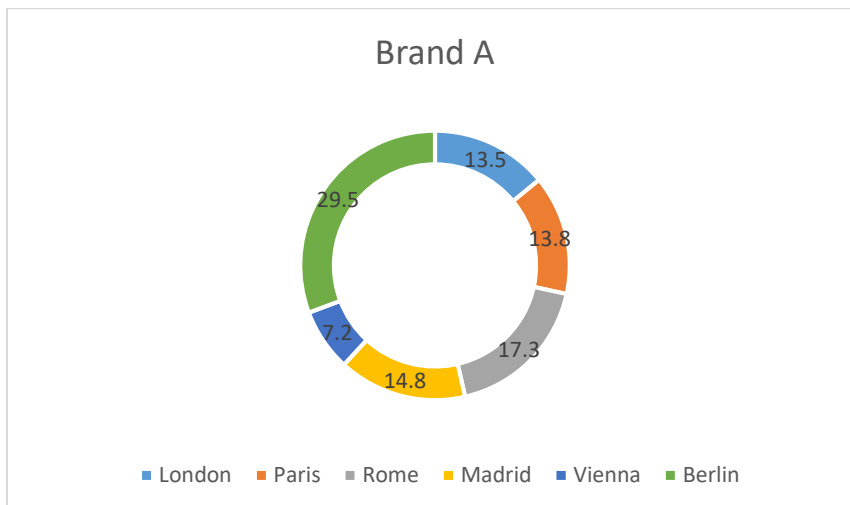
title of the vertical axis is added by selecting Layout > Labels|Axis Titles > Primary Vertical Axis Title > Rotated Title.

## 2-Pie charts

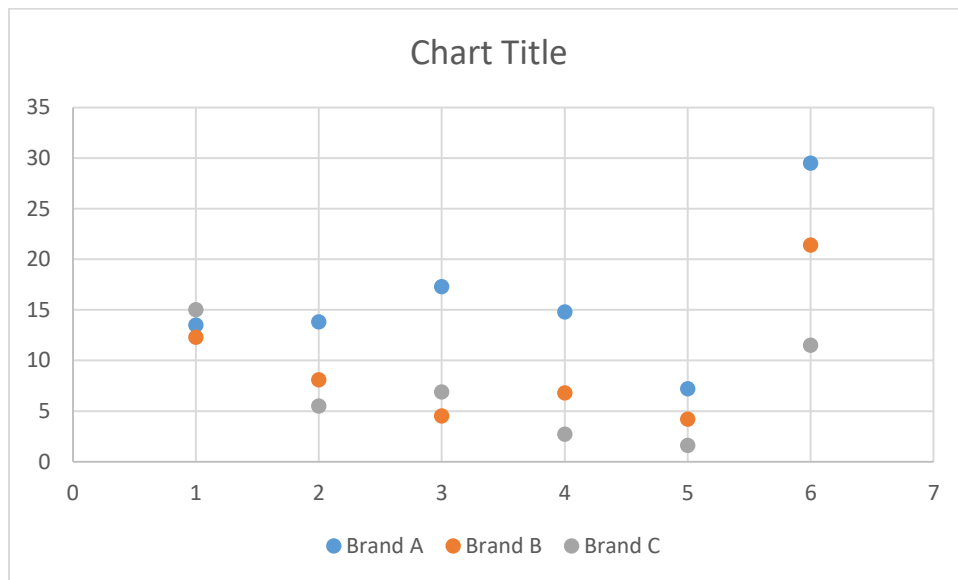
For the previous example draw the pie chart for brand A



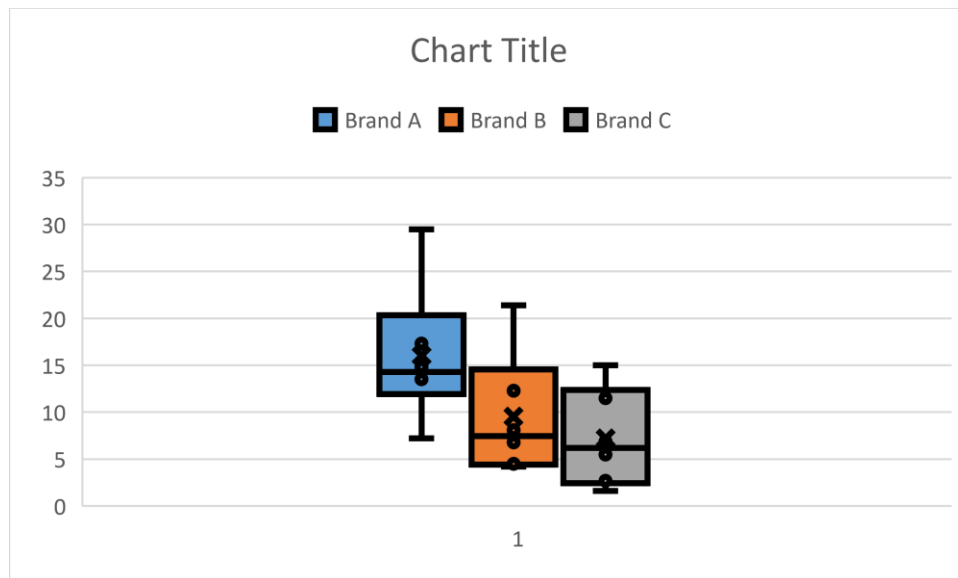
Also,



### 3-scatter plot



### 4-Boxplot



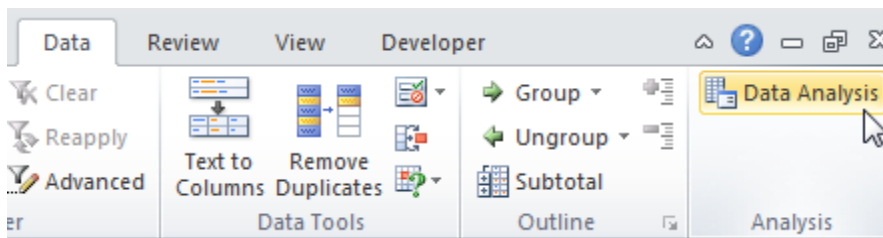
## 4-Histogram

We explain how to create the Histogram in Excel through the following example given in the file Histogram.xls. This example teaches you how to create a histogram in Excel.

1. First, enter the bin numbers (upper levels) in the range C3:C7.

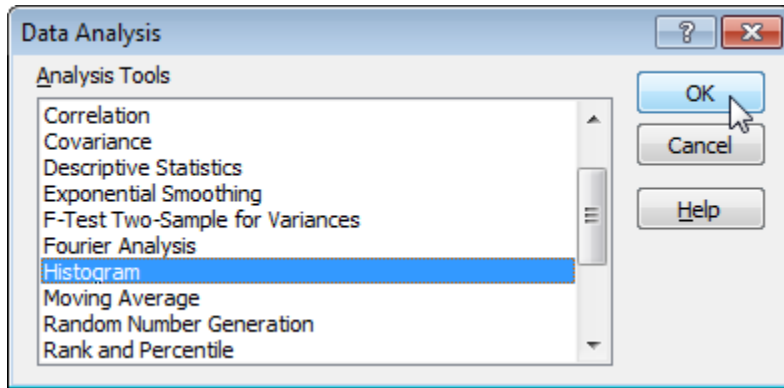
|    | A                  | B | C  | D |
|----|--------------------|---|----|---|
| 1  | Number of students |   |    |   |
| 2  | 22                 |   |    |   |
| 3  | 29                 |   | 20 |   |
| 4  | 40                 |   | 25 |   |
| 5  | 30                 |   | 30 |   |
| 6  | 48                 |   | 35 |   |
| 7  | 24                 |   | 40 |   |
| 8  | 21                 |   |    |   |
| 9  | 19                 |   |    |   |
| 10 | 24                 |   |    |   |
| 11 | 22                 |   |    |   |
| 12 | 25                 |   |    |   |
| 13 | 52                 |   |    |   |
| 14 | 35                 |   |    |   |
| 15 | 40                 |   |    |   |
| 16 | 31                 |   |    |   |
| 17 | 37                 |   |    |   |
| 18 | 21                 |   |    |   |
| 19 | 23                 |   |    |   |
| 20 |                    |   |    |   |
| 21 |                    |   |    |   |

2. On the Data tab, click Data Analysis.



Note: can't find the Data Analysis button? Click [here](#) to load the Analysis ToolPak add-in.

3. Select Histogram and click OK.

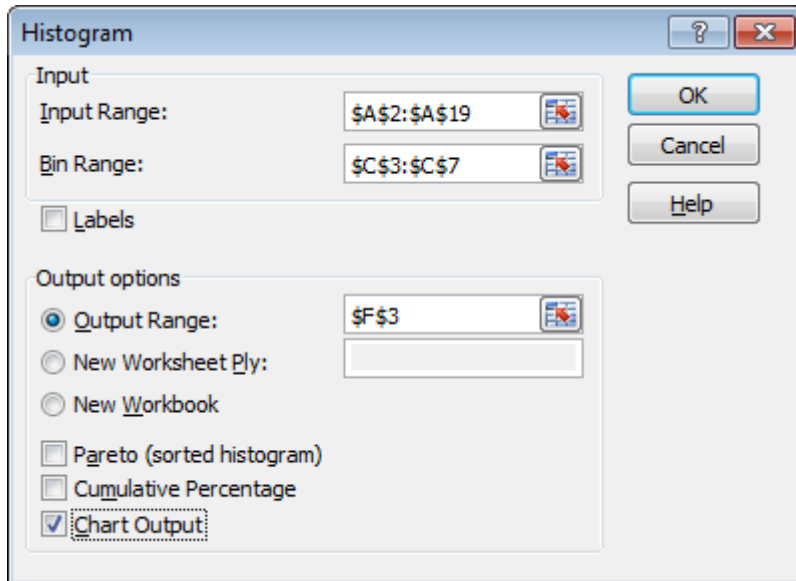


4. Select the range A2:A19.

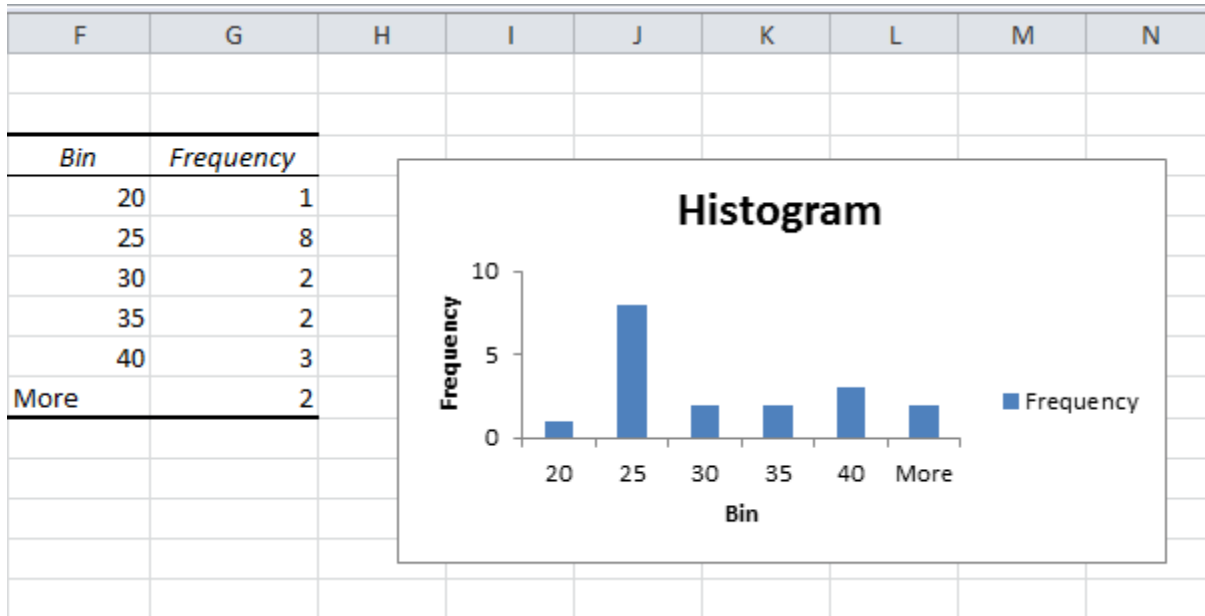
5. Click in the Bin Range box and select the range C3:C7.

6. Click the Output Range option button, click in the Output Range box and select cell F3.

7. Check Chart Output.



8. Click OK.

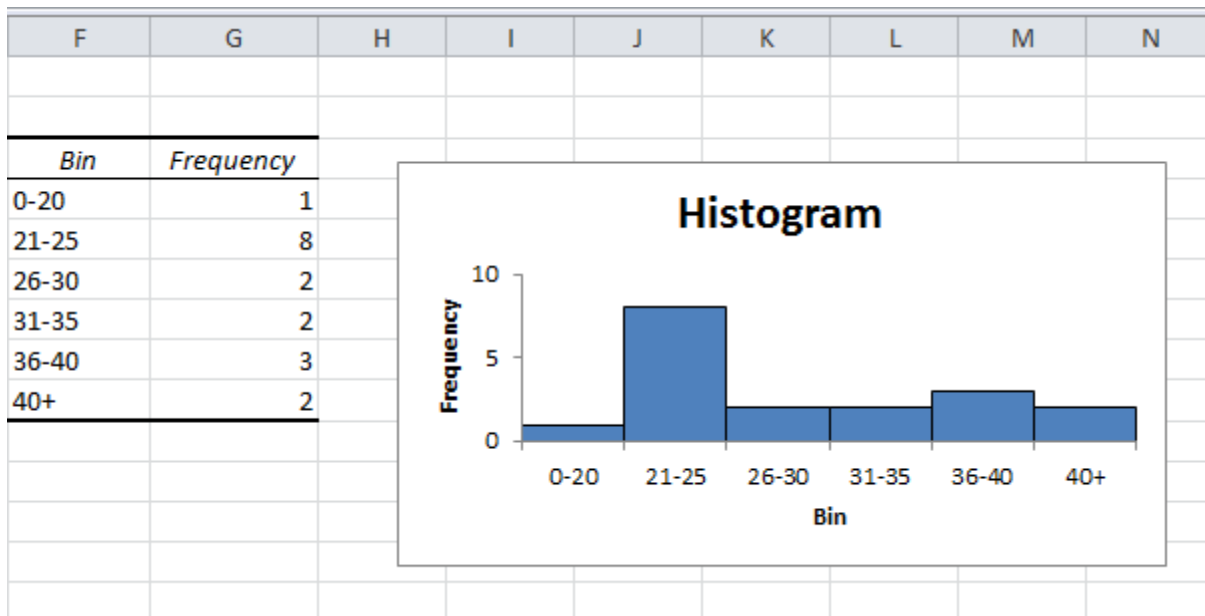


9. Click the legend on the right side and press Delete.

10. Properly label your bins.

11. To remove the space between the bars, right click a bar, select Format Data Series and change the Gap Width to 0%. Select Border Color to add a border.

Result:



## **Working With Matrices In Excel**

To work with matrices in excel, especially with the multiplications and inverse, you have to follow the following steps

- 1- Select suitable (m x n) block anywhere else in your spreadsheet to receive the expected results on them.
- 2- Press the “F2” key. • Press the “=” sign
- 3- Type the matrix function with its arguments.
- 4- Hold down the keys “Ctrl” and “Shift” at the same time and press the “Enter” key while holding down the other two.

### **Example:**

Find the inverse of

$$A = \begin{pmatrix} 2 & -2 & 1 \\ 3 & 1 & -1 \\ 1 & -3 & 2 \end{pmatrix}$$

$A^{-1}$  should now appear in the block of cells you had selected (see screen shot on the right below).

|   | A                | B  | C  | D |
|---|------------------|----|----|---|
| 1 | 2                | -2 | 1  |   |
| 2 | 3                | 1  | -1 |   |
| 3 | 1                | -3 | 2  |   |
| 4 |                  |    |    |   |
| 5 | =MINVERSE(A1:C3) |    |    |   |
| 6 |                  |    |    |   |
| 7 |                  |    |    |   |

|   | A    | B   | C   | D |
|---|------|-----|-----|---|
| 1 | 2    | -2  | 1   |   |
| 2 | 3    | 1   | -1  |   |
| 3 | 1    | -3  | 2   |   |
| 4 |      |     |     |   |
| 5 | -0.5 | 0.5 | 0.5 |   |
| 6 | -3.5 | 1.5 | 2.5 |   |
| 7 | -5   | 2   | 4   |   |

If something weird appears (like only one number appearing), you may have pressed the **Enter** key without holding down the **Ctrl** and **Shift** keys. If this is the case re-select the cells you had chosen for your  $A^{-1}$  and press the **Delete** key, then repeat the above steps.

If  $A^{-1}$  does not exist, e.g. the matrix  $B = \begin{pmatrix} 2 & -4 \\ -3 & 6 \end{pmatrix}$  has no inverse since  $\det(B) = 0$ , you may get something that looks like this:

|   | A     | B     |   |
|---|-------|-------|---|
| 1 | 2     | -4    |   |
| 2 | -3    | 6     |   |
| 3 |       |       |   |
| 4 | #NUM! | #NUM! | ⚠ |
| 5 | #NUM! | #NUM! |   |
| 6 |       |       |   |



## Example

### Example:

Find the A.C, such that

$$A = \begin{pmatrix} 2 & -2 & 1 \\ 3 & 1 & -1 \\ 1 & -3 & 2 \end{pmatrix}, \quad C = \begin{pmatrix} 1 & 1 \\ 2 & 1 \\ 2 & 3 \end{pmatrix}$$

## Solution

As an illustration, let  $A$  be as given above and  $C = \begin{pmatrix} 1 & 1 \\ 2 & 1 \\ 2 & 3 \end{pmatrix}$ . Since  $A$  is a  $3 \times 3$  matrix and  $C$  is a  $3 \times 2$  matrix, the product  $AC$  is a  $3 \times 2$  matrix. Performing the above steps will give the following screen shots:

|   | A                   | B  | C  | D | E | F |
|---|---------------------|----|----|---|---|---|
| 1 | 2                   | -2 | 1  |   | 1 | 1 |
| 2 | 3                   | 1  | -1 |   | 2 | 1 |
| 3 | 1                   | -3 | 2  |   | 2 | 3 |
| 4 |                     |    |    |   |   |   |
| 5 | =MMULT(A1:C3,E1:F3) |    |    |   |   |   |
| 6 |                     |    |    |   |   |   |
| 7 |                     |    |    |   |   |   |

|   | A  | B  | C  | D | E | F |
|---|----|----|----|---|---|---|
| 1 | 2  | -2 | 1  |   | 1 | 1 |
| 2 | 3  | 1  | -1 |   | 2 | 1 |
| 3 | 1  | -3 | 2  |   | 2 | 3 |
| 4 |    |    |    |   |   |   |
| 5 | 0  | 3  |    |   |   |   |
| 6 | 3  | 1  |    |   |   |   |
| 7 | -1 | 4  |    |   |   |   |

We are now ready to find the solution to our system of equations.

## Solving the system of Equations

Enter the right-hand-side column vector  $\mathbf{b} = \begin{pmatrix} 3 \\ 7 \\ 0 \end{pmatrix}$  into a  $3 \times 1$  block of cells in your spreadsheet. Also enter the matrix  $A$  into a  $3 \times 3$  block of cells in your spreadsheet.

Since we will get the solution from the matrix product  $A^{-1}\mathbf{b}$ , we first determine the order of the resultant matrix. In this case, we are multiplying a  $3 \times 3$  matrix by a  $3 \times 1$  vector, we will get a  $3 \times 1$  vector.

Select a  $3 \times 1$  block of empty cells. Type the following: **F2 = MMULT(MINVERSE(** and select the cells containing matrix  $A$ . Close bracket **)**. Type a comma and select the cells containing the vector  $\mathbf{b}$  and close bracket **)**. You should have something that looks like this:

|   | A | B                             | C  | D | E |
|---|---|-------------------------------|----|---|---|
| 1 | 2 | -2                            | 1  |   | 3 |
| 2 | 3 | 1                             | -1 |   | 7 |
| 3 | 1 | -3                            | 2  |   | 0 |
| 4 |   |                               |    |   |   |
| 5 |   | =MMULT(MINVERSE(A1:C3),E1:E3) |    |   |   |
| 6 |   |                               |    |   |   |
| 7 |   |                               |    |   |   |

Hold down the **Ctrl** and **Shift** keys and press the **Enter** key while still holding the other two keys. The values of  $x, y$  and  $z$  should now appear (see screen shot below).

|   | A | B  | C  | D | E |
|---|---|----|----|---|---|
| 1 | 2 | -2 | 1  |   | 3 |
| 2 | 3 | 1  | -1 |   | 7 |
| 3 | 1 | -3 | 2  |   | 0 |
| 4 |   |    |    |   |   |
| 5 |   | 2  |    |   |   |
| 6 |   | 0  |    |   |   |
| 7 |   | -1 |    |   |   |

Note that we did not have to calculate  $A^{-1}$  separately. We simply asked Excel to calculate it for us and then multiply the inverse by  $\mathbf{b}$ . Most Excel functions can be nested in this way.

# Matrix determinant

## Example 1 - 2x2 Matrix

The spreadsheet on the right shows a simple 2x2 matrix. The determinant of this matrix can be calculated using the Excel Mdeterm function as follows:

`=MDETERM( A1:B2 )`

This gives the result **-9**.

|   | A | B |
|---|---|---|
| 1 | 5 | 2 |
| 2 | 7 | 1 |

## Example 2 - 3x3 Matrix

The determinant of the simple 3x3 matrix on the right can be calculated using the following Excel Mdeterm function:

`=MDETERM( A1:C3 )`

This gives the result **40**.

|   | A | B | C |
|---|---|---|---|
| 1 | 6 | 4 | 2 |
| 2 | 3 | 5 | 3 |
| 3 | 2 | 3 | 4 |

## Generation Random samples

- Generation from uniform distribution between 0 and 1

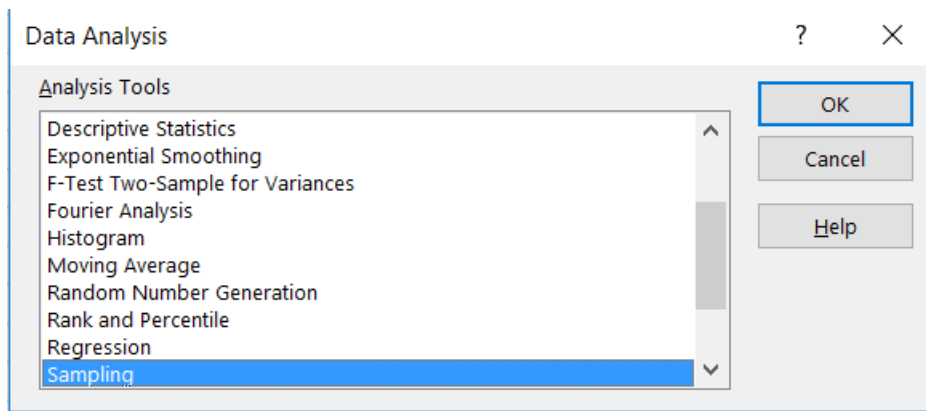
To generate a random sample between 0 and 1 follow the steps below

- 1- Highlight number the cells (in column A, for example) equal the sample size.
- 2- Type "=RAND()" without the quotes into the Formula bar, and then press "Ctrl-Enter" to assign random numbers to your selection.


- Random between two numbers

=RANDBETWEEN(a,b)


- Random sample



Sampling ? X

Input  
 Input Range:    
☒ Labels


Sampling Method  
☐ Periodic  
 Period:   
☒ Random  
 Number of Samples:

Output options  
☒ Output Range:    
☐ New Worksheet Ply:   
☐ New Workbook

OK  
 Cancel  
 Help


- Random number generation from distributions

Random Number Generation ? X

Number of Variables:   
 Number of Random Numbers:   
 Distribution:  

Parameters  
 Mean =   
 Standard deviation =

Random Seed:


Output options  
☒ Output Range:    
☐ New Worksheet Ply:   
☐ New Workbook

OK  
 Cancel  
 Help

- Rank and percentile

Rank and Percentile ? X


Input

Input Range:  

Grouped By: ☒ Columns ☐ Rows

☒ Labels in first row

Output options

☒ Output Range:  

☐ New Worksheet Ply:

☐ New Workbook

OK Cancel Help

| x |  | Point | x | Rank | Percent |
|---|--|-------|---|------|---------|
| 5 |  | 9     | 9 | 1    | 100.00% |
| 7 |  | 6     | 8 | 2    | 92.30%  |
| 4 |  | 2     | 7 | 3    | 84.60%  |
| 5 |  | 14    | 6 | 4    | 76.90%  |
| 5 |  | 1     | 5 | 5    | 53.80%  |
| 8 |  | 4     | 5 | 5    | 53.80%  |
| 2 |  | 5     | 5 | 5    | 53.80%  |
| 2 |  | 3     | 4 | 8    | 30.70%  |
| 9 |  | 10    | 4 | 8    | 30.70%  |
| 4 |  | 11    | 4 | 8    | 30.70%  |
| 4 |  | 13    | 3 | 11   | 23.00%  |
| 2 |  | 7     | 2 | 12   | 0.00%   |
| 3 |  | 8     | 2 | 12   | 0.00%   |
| 6 |  | 12    | 2 | 12   | 0.00%   |