



## Applied Mathematics for Biomedical Technology

**King Saud University**

**College of Applied Medical Sciences**

**Biomedical Technology Department**

**Second Midterm Course Instructor: Dr.**

**Widad Babiker**

**Course No. 222, first Semester 1440-1441**

**Date Time: Thursday 22/3/1441 h**

**الموافق 19/11/2019 م**

**Time: 90 Minutes**

Student's Name	
Student's ID	

Question No.	$Q_1$	$Q_2$	$Q_3$	$Q_4$	Total
Maximum Marks					
Marks Obtained					

**Q. No. 1**

i. Simplify:

a.  $\frac{1}{4} \log 1 + \frac{3}{4} \log 16 + \frac{1}{2} \log 9 - 2 \log 2$

b.  $\sqrt{e^{2 \ln x}}, \quad x > 0$

ii. Find the solution of  $3^x + 1 = -2$  if it exists

iii. Change to exponential form.  $\log x = y + 4$

iv. State the range of possible values of an angle  $\beta$  such that  $\cos \beta > 0$  and  $\tan \beta < 0$ .

**Q. No. 2. Prove the given identities: (All details are required)**

**i.** 
$$\frac{\tan x - \sin x}{\sin^3 x} = \frac{\sec x}{1 + \cos x}$$

**ii.** 
$$\frac{\cos 2x + \cos x + 1}{\sin 2x + \sin x} = \cot x$$

**iii.** Find  $\sin(2\theta)$  and  $\cos(2\theta)$  given that  $\cos \theta = -\frac{24}{25}$ ,  $\theta$  in quadrant III.

**Q. No. 3.**

i. Derive (prove) the sines law of an oblique triangle ABC. **(All details are required)**

ii. The current through a diode,  $I$ , is given by  $I = I_s(e^{40V} - 1)$  where  $I$  is the reverse saturation current and  $V$  is the voltage across the diode.

(a) Express  $V$  as the subject of the equation.

(b) Evaluate  $V$  when  $I = 3 \times 10^{-2}$ ,  $I_s = 1.5 \times 10^{-4}$ .

**Q. No. 4.**

i. Graph  $f(x) = 2^{x+1} - 3$ . State the domain, range, and asymptote. **(All details are needed)**

ii. The voltage gain, measured in decibels (dB), of an amplifier is given by:

gain =  $20 \log \left( \frac{V_0}{V_i} \right)$  Where  $V_i$  is the input voltage and  $V_0$  is the output voltage. The

output voltage from an amplifier is 250 mV. If the amplifier has a gain of 17 dB calculates the input voltage. **(All details are needed)**