

# Chapter 9

## Settlement of Shallow Foundations

**Omitted parts:**

Section 9.8 , 9.9, 9.15 ,9.16

# CAUSES OF SETTLEMENT

Settlement of a structure resting on soil may be caused by two distinct kinds of action within the foundation soils:-

## I. Settlement Due to Shear Stress (Distortion Settlement)

In the case the applied load caused **shearing stresses** to develop within the soil mass which are greater than the **shear strength** of the material, then the soil fails by sliding downward and laterally, and the structure settle and may tip of vertical alignment. This is what we referred to as **BEARING CAPACITY**.

## II. Settlement Due to Compressive Stress (Volumetric Settlement)

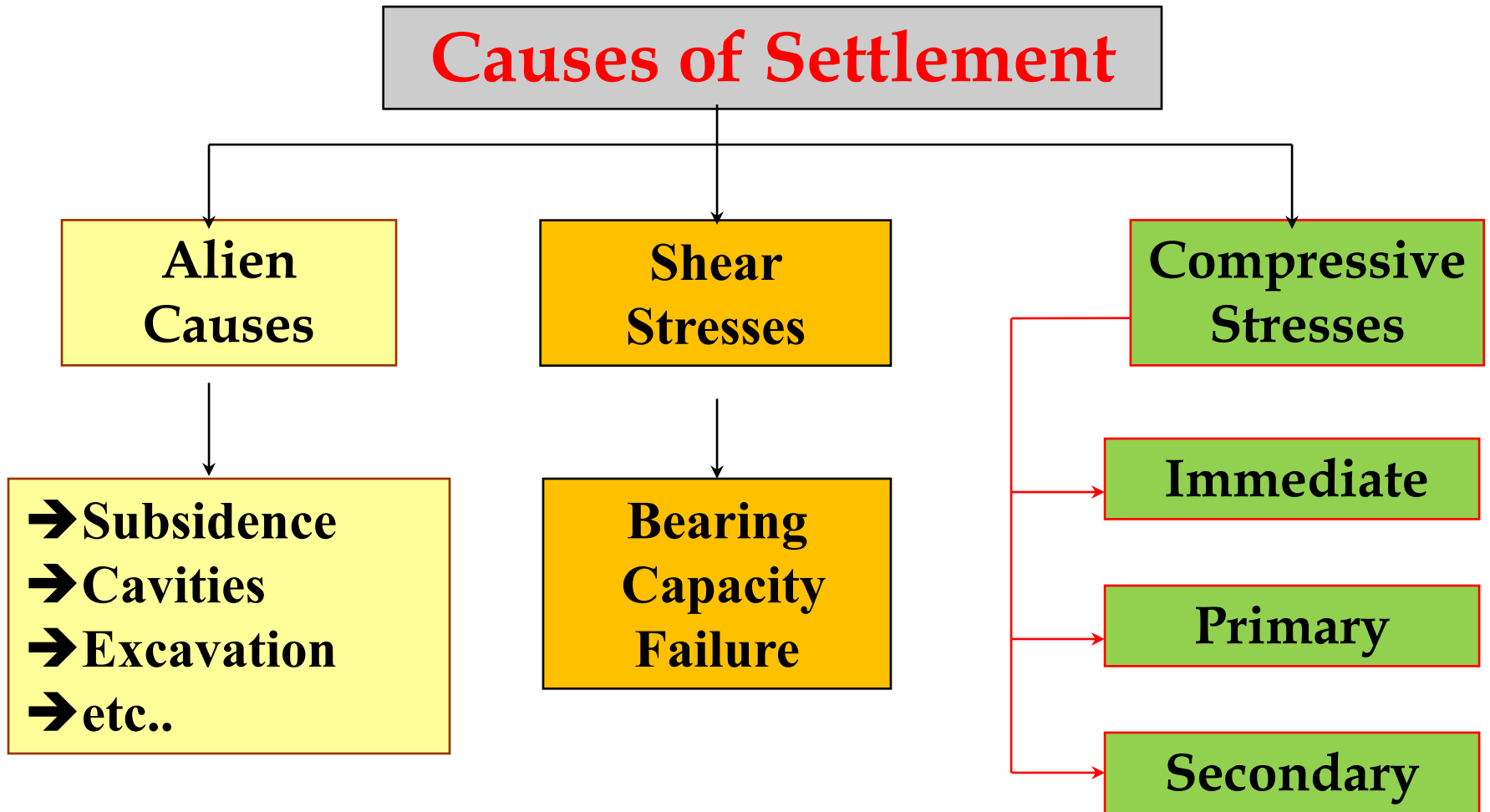
As a result of the applied load a compressive stress is transmitted to the soil leading to compressive strain. Due to the compressive strain the structure settles. This is important only if the settlement is **excessive** otherwise it is not dangerous.

# ALLOWABLE BEARING CAPACITY

The allowable bearing capacity is the smaller of the following two conditions:

$$q_{\text{all}} = \text{smallest of} \begin{cases} \frac{q_u}{FS} \text{ (to control shear failure)} \\ q_{\text{all, settlement}} \text{ (to control settlement)} \end{cases}$$

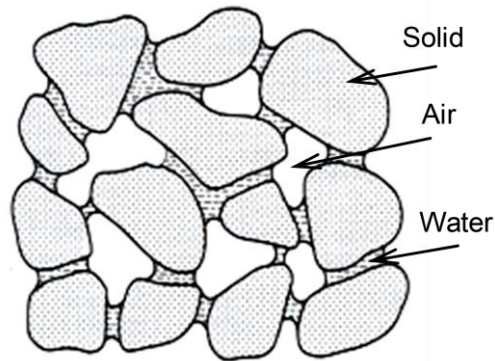
# CAUSES OF SETTLEMENT



# Mechanisms of Compression

Compression of soil is due to a number of mechanisms:

- **Deformation** of soil particles or grains
- **Relocations** of soil particles
- **Expulsion** of water or air from the void spaces



# Components of Settlement

Settlement of a soil layer under applied load is the sum of two broad components or categories:

1. Elastic settlement (or immediate) settlements
2. Consolidation settlement

## 1. Elastic settlement (or immediate) settlements

Elastic or immediate settlement takes place **instantly** at the moment of the application of load due to the distortion (but no bearing failure) and bending of soil particles (mainly clay). It is not generally elastic although theory of elasticity is applied for its evaluation. It is predominant in **coarse-grained soils**.

# Consolidation settlement

2. Consolidation settlement is the sum of two parts or types:

## A. Primary consolidation settlement

In this the compression of clay is due to expulsion of water from pores. The process is referred to as **primary consolidation** and the associated settlement is termed **primary consolidation settlement**. Commonly they are referred to simply as **consolidation or consolidation settlement (CE 481)**

## B. Secondary consolidation settlement

The compression of clay soil due to **plastic readjustment** of soil grains and progressive breaking of clayey particles and their inter-particles bonds is known as **secondary consolidation or secondary compression**, and the associated settlement is called **secondary consolidation settlement or secondary compression**.

# Components of Settlement

The total settlement of a foundation can be expressed as:

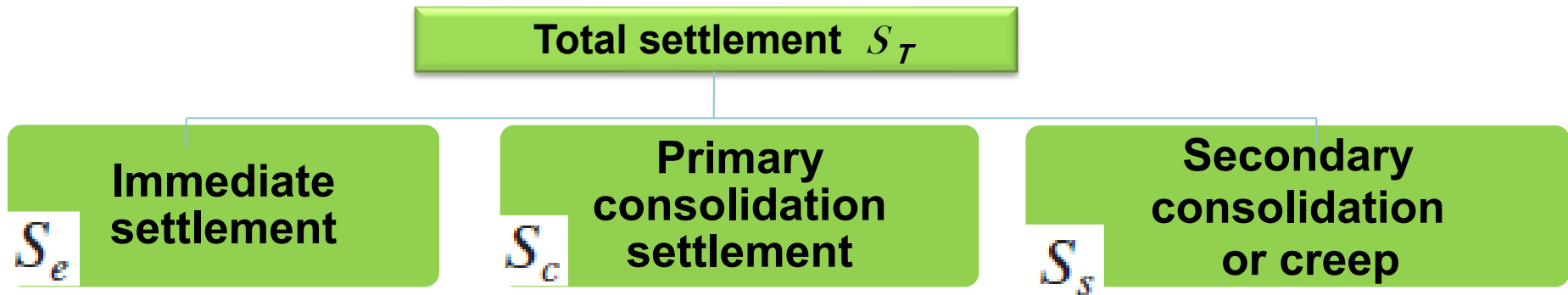
$$S_T = S_e + S_c + S_s$$

$S_T$  = Total settlement

$S_e$  = Elastic or immediate settlement

$S_c$  = Primary consolidation settlement

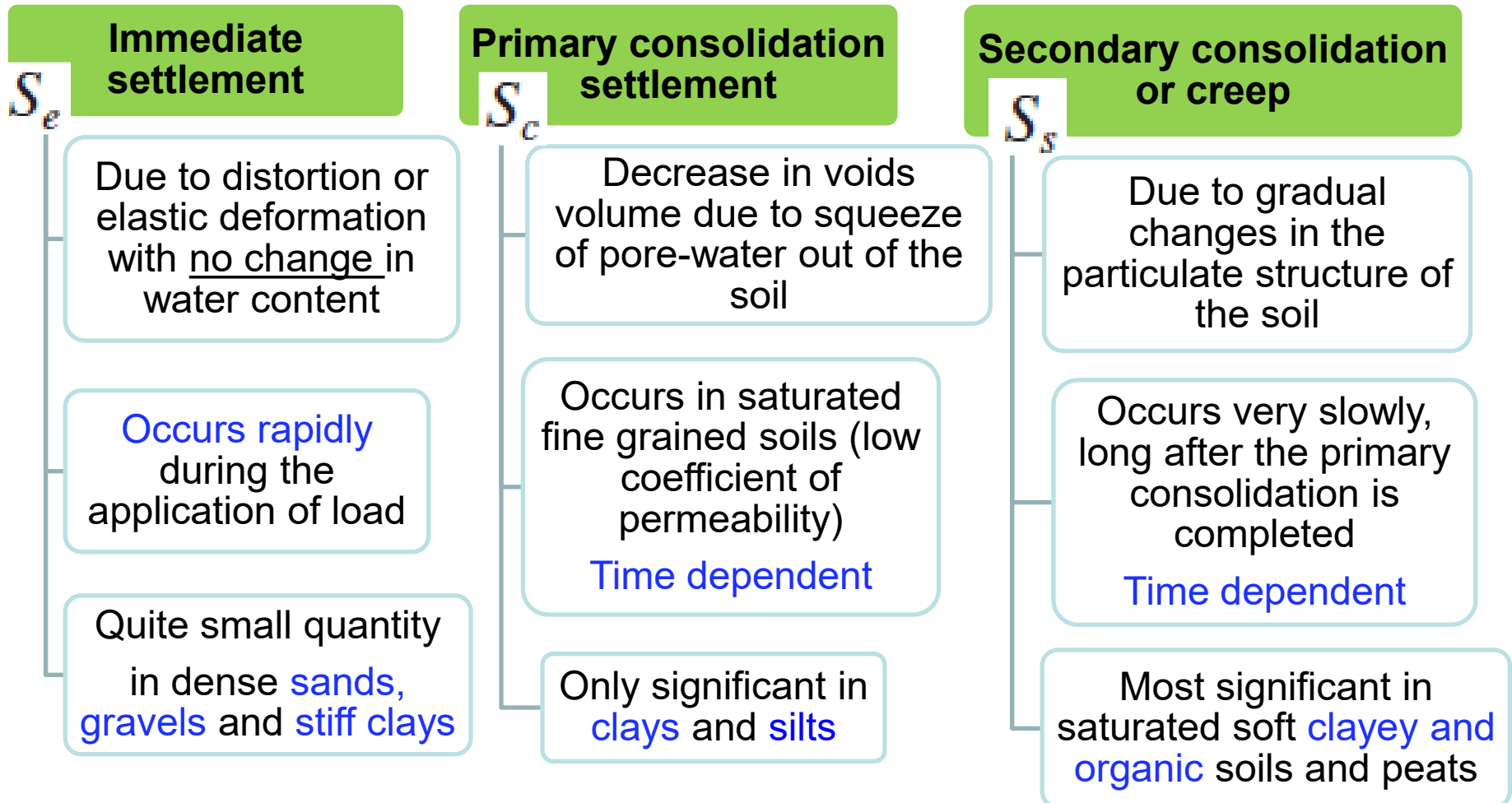
$S_s$  = Secondary consolidation settlement



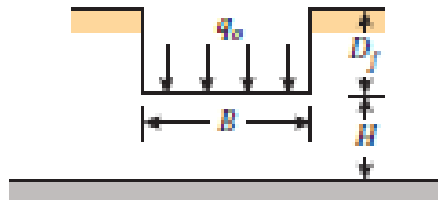
- It should be mentioned that  $S_c$  and  $S_s$  **overlap** each other and impossible to detect which certainly when one type ends and the other begins. However, for simplicity they are treated separately and secondary consolidation is usually assumed to begin at the end of primary consolidation.

# Components of settlement

The **total soil settlement**  $S_T$  may contain one or more of these types:



# Elastic Settlement of Shallow Foundation on Saturated Clay ( $\mu_s = 0.5$ )



$$S_e = A_1 A_2 \frac{q_o B}{E_s}$$

$$A_1 = f(H/B, L/B)$$

$$A_2 = f(D_f/B)$$

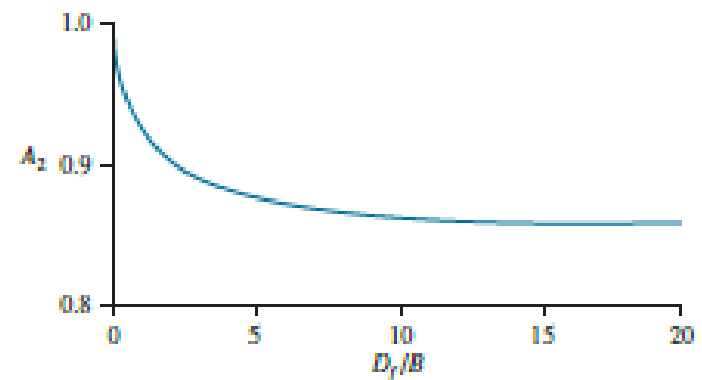
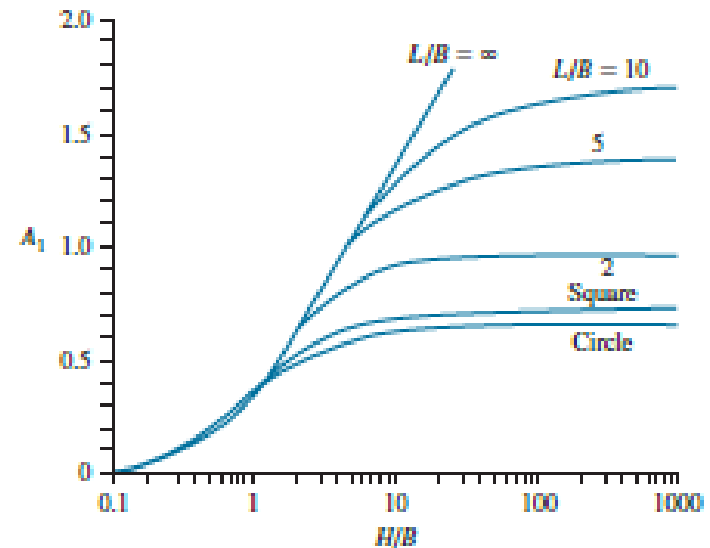
$L$  = length of the foundation

$B$  = width of the foundation

$D_f$  = depth of the foundation

$H$  = depth of the bottom of the foundation to a rigid layer

$q_o$  = net load per unit area of the foundation



# Elastic Settlement of Shallow Foundation on Saturated Clay ( $\mu_s = 0.5$ )

$$E_s = \beta c_u$$

where  $c_u$  = undrained shear strength.

**TABLE 9.1** Range of  $\beta$  for Saturated Clay [Eq. (9.2)]<sup>a</sup>

Plasticity index	$\beta$				
	OCR = 1	OCR = 2	OCR = 3	OCR = 4	OCR = 5
<30	1500–600	1380–500	1200–580	950–380	730–300
30 to 50	600–300	550–270	580–220	380–180	300–150
>50	300–150	270–120	220–100	180–90	150–75

<sup>a</sup>Based on Duncan and Buchignani (1976)

# EXAMPLE 9.1

## EXAMPLE 9.1

Consider a shallow foundation  $2 \text{ m} \times 1 \text{ m}$  in plan in a saturated clay layer. A rigid rock layer is located  $8 \text{ m}$  below the bottom of the foundation. Given:

Foundation:  $D_f = 1 \text{ m}$ ,  $q_o = 120 \text{ kN/m}^2$

Clay:  $c_u = 150 \text{ kN/m}^2$ ,  $\text{OCR} = 2$ , and plasticity index,  $\text{PI} = 35$

Estimate the elastic settlement of the foundation.

### SOLUTION

From Eq. (9.1),

$$S_e = A_1 A_2 \frac{q_o B}{E_s}$$

Given:

$$\frac{L}{B} = \frac{2}{1} = 2$$

$$\frac{D_f}{B} = \frac{1}{1} = 1$$

$$\frac{H}{B} = \frac{8}{1} = 8$$

$$E_s = \beta c_u$$

For  $\text{OCR} = 2$  and  $\text{PI} = 35$ , the value of  $\beta \approx 480$  (Table 9.1). Hence,

$$E_s = (480)(150) = 72,000 \text{ kN/m}^2$$

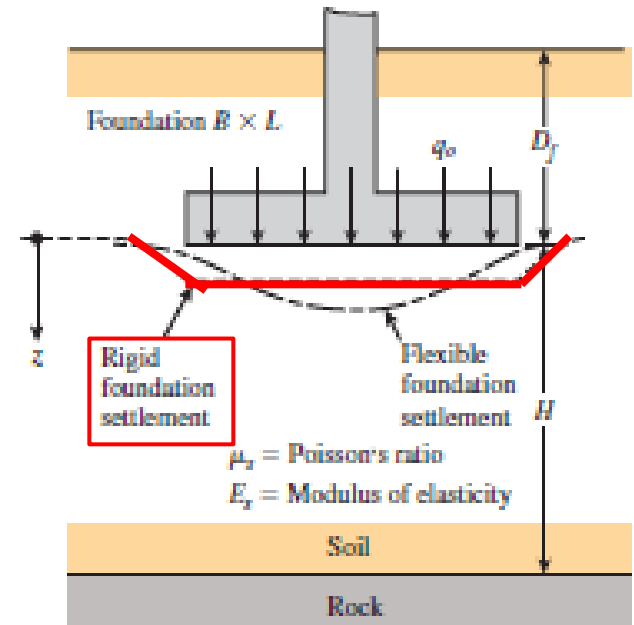
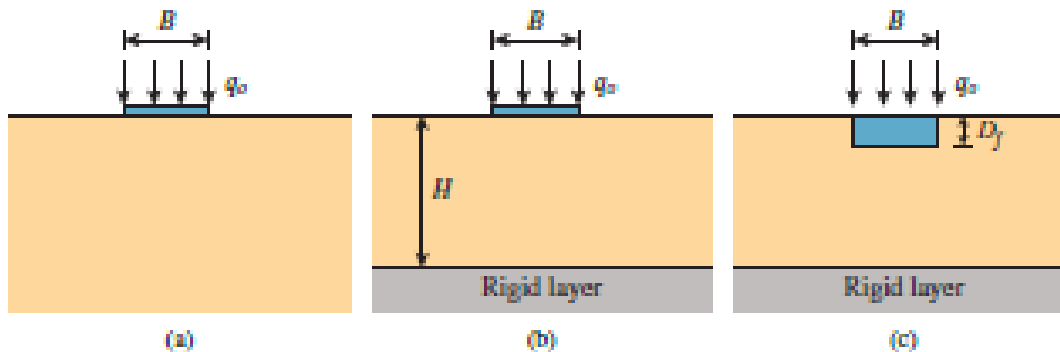
Also, from Figure 9.1,  $A_1 = 0.9$  and  $A_2 = 0.92$ . Hence,

$$S_e = A_1 A_2 \frac{q_o B}{E_s} = (0.9)(0.92) \frac{(120)(1)}{72,000} = 0.00138 \text{ m} = \mathbf{1.38 \text{ mm}}$$

# Elastic Settlement in Granular Soil

## Settlement Based on the Theory of Elasticity

1. Flexible surface foundation ( $D_f = 0$ ) resting on an elastic half-space, as shown in Figure (a)
2. The presence of a rigid layer at a finite depth  $H$  as shown in Figure (b)
3. Embedment depth  $D_f$  as shown in Figure (c).



# Elastic Settlement in Granular Soil

## 1. Surface Foundations on Elastic Half-Space

$$S_e = \frac{q_o B}{E_s} (1 - \mu_s^2) I$$

where

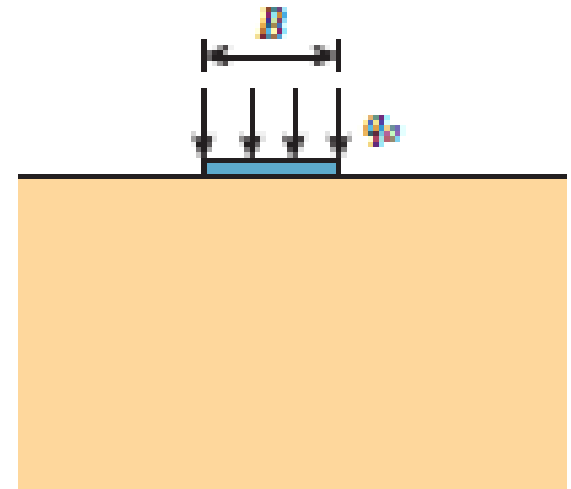
$I$  = the influence factor that depends on the location of the point of interest on the foundation.

$q_o$  = the net pressure applied by the foundation to the underlying soil

$B$  = the width of the foundation

$E_s$  = the modulus of elasticity of the soil

$\mu_s$  = Poisson's ratio of the soil.



# Elastic Settlement in Granular Soil

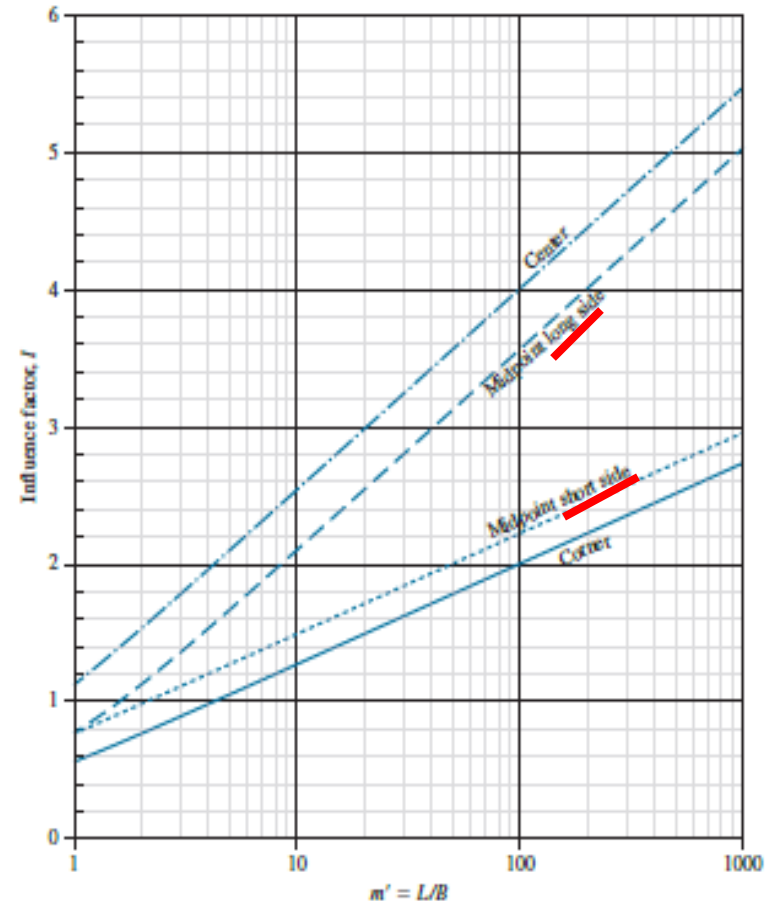
## 1. Surface Foundations on Elastic Half-Space

Schleicher (1926) expressed the influence factor for the corner of a flexible foundation as

$$I_{\text{corner}} = \frac{1}{\pi} \left[ m' \ln \left( \frac{1 + \sqrt{m'^2 + 1}}{m'} \right) + \ln(m' + \sqrt{m'^2 + 1}) \right]$$

where  $m' = L/B$

The influence factors for the other locations on the foundation can be determined by dividing the foundation into four rectangles and using the principle of superposition



# Elastic Settlement in Granular Soil

## 1. Surface Foundations on Elastic Half-Space

### Giroud (1968) and Poulos and Davis (1974)

Corner:	$I = 0.7283 \log m' + 0.5469$
Center:	$I = 1.4566 \log m' + 1.0939$
Midpoint short side:	$I = 0.7318 \log m' + 0.7617$
Midpoint long side:	$I = 1.4357 \log m' + 0.6894$

The settlements under the center and the perimeter of a uniformly loaded *flexible circular foundation* of diameter  $B$  are given by:

$$\text{Center:} \quad S_c = \frac{q_o B}{E_s} (1 - \mu_s^2) \quad I = 1.0$$

$$\text{Perimeter:} \quad S_c = \frac{q_o B}{E_s} (1 - \mu_s^2) \frac{2}{\pi} \quad I = 2/\pi$$

# Elastic Settlement in Granular Soil

## 1. Surface Foundations on Elastic Half-Space

- ❑ Flexible foundations apply uniform pressure and settle non-uniformly.
- ❑ Rigid foundations apply non-uniform pressure and settle uniformly.
- ❑ Some influence factors for estimating the average values of the settlements of flexible and rigid foundations, are given in Table 9.2.
- ❑ Bowles (1987) suggested that the settlement of the **rigid** foundation can be estimated as **93%** of the settlement computed for a **flexible foundation under the center**.
- ❑ The average values of  $I$  reported by Giroud (1968) and Poulos and Davis (1974) suggest that the average value of the settlement of a **flexible** foundation can be computed using **84–88%** of the  $I$ -value for the **center**.

TABLE 9.2 Influence Factors to Compute Average Settlement of Flexible and Rigid Foundation

$m' = L/B$	Flexible	Rigid
Circle	0.85	0.79
1	0.95	0.82
1.5	1.20	1.07
2	1.30	1.21
3	1.52	1.42
5	1.82	1.60
10	2.24	2.00
100	2.96	3.40

# Elastic Settlement in Granular Soil

## 2. Effects of a Rigid Layer on the Settlements of Surface Foundations

When the soil is underlain by a rigid layer, the settlement has to be reduced

The influence factor for the corner of a uniformly loaded flexible rectangular surface foundation is:

$$I_r = F_1 + \left( \frac{1 - 2\mu_s}{1 - \mu_s} \right) F_2$$

where

$$F_1 = \frac{1}{\pi} (A_0 + A_1)$$

$$F_2 = \frac{\pi'}{2\pi} \tan^{-1} A_2$$

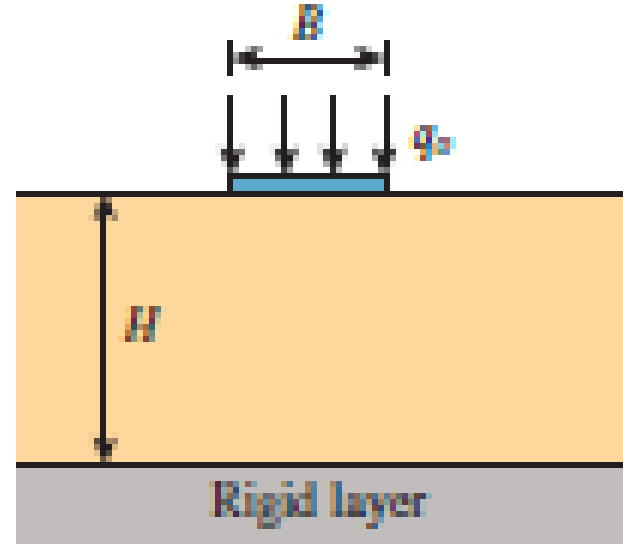
$A_0$ ,  $A_1$ , and  $A_2$  are given by

$$A_0 = m' \ln \frac{(1 + \sqrt{m'^2 + 1}) \sqrt{m'^2 + n'^2}}{m' (1 + \sqrt{m'^2 + n'^2 + 1})}$$

$$A_1 = \ln \frac{(m' + \sqrt{m'^2 + 1}) \sqrt{1 + n'^2}}{m' + \sqrt{m'^2 + n'^2 + 1}}$$

$$A_2 = \frac{m'}{n' + \sqrt{m'^2 + n'^2 + 1}}$$

$$n' = H/B.$$



# Elastic Settlement in Granular Soil

## 2. Effects of a Rigid Layer on the Settlements of Surface Foundations

$$F_1 = \frac{1}{\pi}(A_0 + A_1)$$

$$F_2 = \frac{n'}{2\pi} \tan^{-1} A_2$$

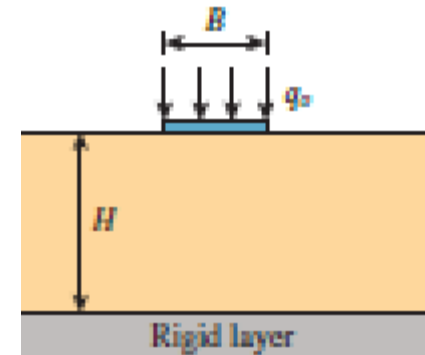


TABLE 9.3 Variation of  $F_1$  with  $m'$  and  $n'$

$n'$	$m'$									
	1.0	1.2	1.4	1.6	1.8	2.0	2.5	3.0	3.5	4.0
0.25	0.014	0.013	0.012	0.011	0.011	0.011	0.010	0.010	0.010	0.010
0.50	0.049	0.046	0.044	0.042	0.041	0.040	0.038	0.038	0.037	0.037
0.75	0.095	0.090	0.087	0.084	0.082	0.080	0.077	0.076	0.074	0.074
1.00	0.142	0.138	0.134	0.130	0.127	0.125	0.121	0.118	0.116	0.115
1.25	0.186	0.183	0.179	0.176	0.173	0.170	0.165	0.161	0.158	0.157
1.50	0.224	0.224	0.222	0.219	0.216	0.213	0.207	0.203	0.199	0.197
1.75	0.257	0.259	0.259	0.258	0.255	0.253	0.247	0.242	0.238	0.235
2.00	0.285	0.290	0.292	0.292	0.291	0.289	0.284	0.279	0.275	0.271
2.25	0.309	0.317	0.321	0.323	0.323	0.322	0.317	0.313	0.308	0.305
2.50	0.330	0.341	0.347	0.350	0.351	0.351	0.348	0.344	0.340	0.336
2.75	0.348	0.361	0.369	0.374	0.377	0.378	0.377	0.373	0.369	0.365
3.00	0.363	0.379	0.389	0.396	0.400	0.402	0.402	0.400	0.396	0.392
3.25	0.376	0.394	0.406	0.415	0.420	0.423	0.426	0.424	0.421	0.418
3.50	0.388	0.408	0.422	0.431	0.438	0.442	0.447	0.447	0.444	0.441
3.75	0.399	0.420	0.436	0.447	0.454	0.460	0.467	0.458	0.466	0.464
4.00	0.408	0.431	0.448	0.460	0.469	0.476	0.484	0.487	0.486	0.484
4.25	0.417	0.440	0.458	0.472	0.481	0.484	0.495	0.514	0.515	0.515
4.50	0.424	0.450	0.469	0.484	0.495	0.503	0.516	0.521	0.522	0.522
4.75	0.431	0.458	0.478	0.494	0.506	0.515	0.530	0.536	0.539	0.539
5.00	0.437	0.465	0.487	0.503	0.516	0.526	0.543	0.551	0.554	0.554

TABLE 9.4 Variation of  $F_2$  with  $m'$  and  $n'$

$n'$	$m'$									
	1.0	1.2	1.4	1.6	1.8	2.0	2.5	3.0	3.5	4.0
0.25	0.049	0.050	0.051	0.051	0.051	0.052	0.052	0.052	0.052	0.052
0.50	0.074	0.077	0.080	0.081	0.083	0.084	0.086	0.086	0.0878	0.087
0.75	0.083	0.089	0.093	0.097	0.099	0.101	0.104	0.106	0.107	0.108
1.00	0.083	0.091	0.098	0.102	0.106	0.109	0.114	0.117	0.119	0.120
1.25	0.080	0.089	0.096	0.102	0.107	0.111	0.118	0.122	0.125	0.127
1.50	0.075	0.084	0.093	0.099	0.105	0.110	0.118	0.124	0.128	0.130
1.75	0.069	0.079	0.088	0.095	0.101	0.107	0.117	0.123	0.128	0.131
2.00	0.064	0.074	0.083	0.090	0.097	0.102	0.114	0.121	0.127	0.131
2.25	0.059	0.069	0.077	0.085	0.092	0.098	0.110	0.119	0.125	0.130
2.50	0.055	0.064	0.073	0.080	0.087	0.093	0.106	0.115	0.122	0.127
2.75	0.051	0.060	0.068	0.076	0.082	0.089	0.102	0.111	0.119	0.125
3.00	0.048	0.056	0.064	0.071	0.078	0.084	0.097	0.108	0.116	0.122
3.25	0.045	0.053	0.060	0.067	0.074	0.080	0.093	0.104	0.112	0.119
3.50	0.042	0.050	0.057	0.064	0.070	0.076	0.089	0.100	0.109	0.116
3.75	0.040	0.047	0.054	0.060	0.067	0.073	0.086	0.096	0.105	0.113
4.00	0.037	0.044	0.051	0.057	0.063	0.069	0.082	0.093	0.102	0.110
4.25	0.036	0.042	0.049	0.055	0.061	0.066	0.079	0.090	0.099	0.107
4.50	0.034	0.040	0.046	0.052	0.058	0.063	0.076	0.086	0.096	0.104
4.75	0.032	0.038	0.044	0.050	0.055	0.061	0.073	0.083	0.093	0.101
5.00	0.031	0.036	0.042	0.048	0.053	0.058	0.070	0.080	0.090	0.098

# Elastic Settlement in Granular Soil

## 2. Effects of a Rigid Layer on the Settlements of Surface Foundations

For  $H = \infty$ ,  $n' = \infty$ ,

$$A_0 = m' \ln \frac{1 + \sqrt{m'^2 + 1}}{m'}$$

$$A_1 = \ln(m' + \sqrt{m'^2 + 1})$$

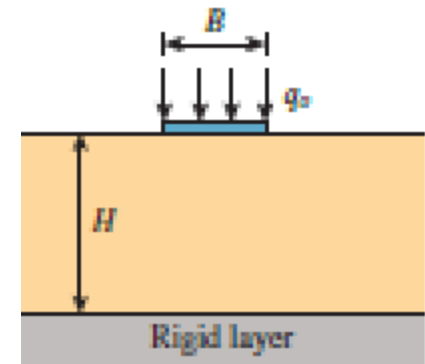
$$A_2 = 0$$

$$F_1 = \frac{1}{\pi}(A_0 + A_1)$$

$$F_2 = \frac{n'}{2\pi} \tan^{-1} A_2$$

$$F_1 = \frac{1}{\pi} \left[ m' \ln \left( \frac{1 + \sqrt{m'^2 + 1}}{m'} \right) + \ln(m' + \sqrt{m'^2 + 1}) \right]$$

$$F_2 = 0$$



# Elastic Settlement in Granular Soil

## 3. Effect of Embedment

When the foundation base is located at some depth beneath the ground level, the embedment **reduces** the settlement.

$$S_e = \frac{q_o B}{E_s} (1 - \mu_s^2) I_s I_f$$

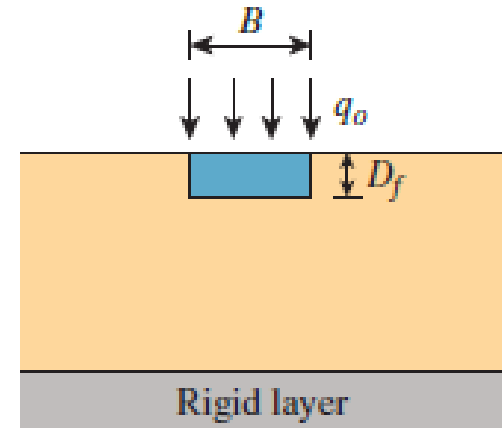
**embedment**

$$I_s = F_1 + \left( \frac{1 - 2\mu_s}{1 - \mu_s} \right) F_2$$

$I_f$  next page

$$S_e = \frac{q_o B}{E_s} (1 - \mu_s^2) M$$

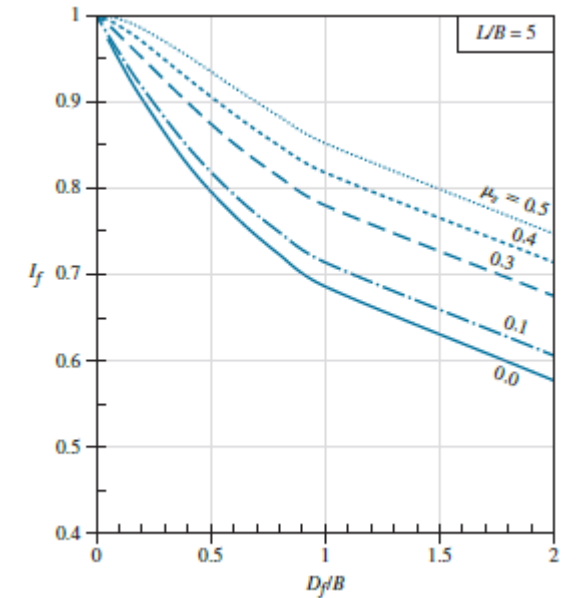
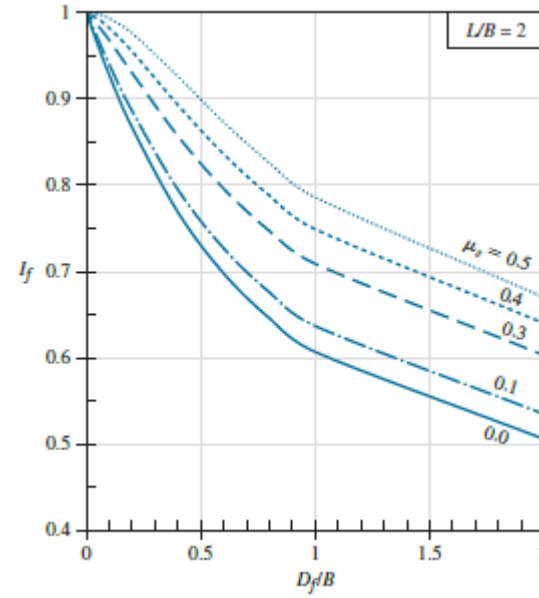
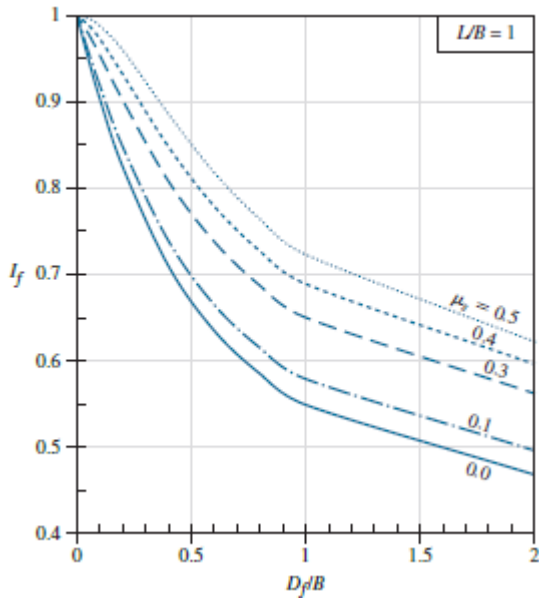
**Surface**



# Elastic Settlement in Granular Soil

## 3. Effect of Embedment

$I_f$



# Elastic Settlement in Granular Soil

## 3. Effect of Embedment

$$E_s$$

Due to the nonhomogeneous nature of soil deposits, the magnitude of  $E_s$  may vary with depth. For that reason, Bowles (1987) recommended using a weighted average of  $E_s$

$$E_s = \frac{\sum E_{s(z)} \Delta z}{\bar{z}}$$

where

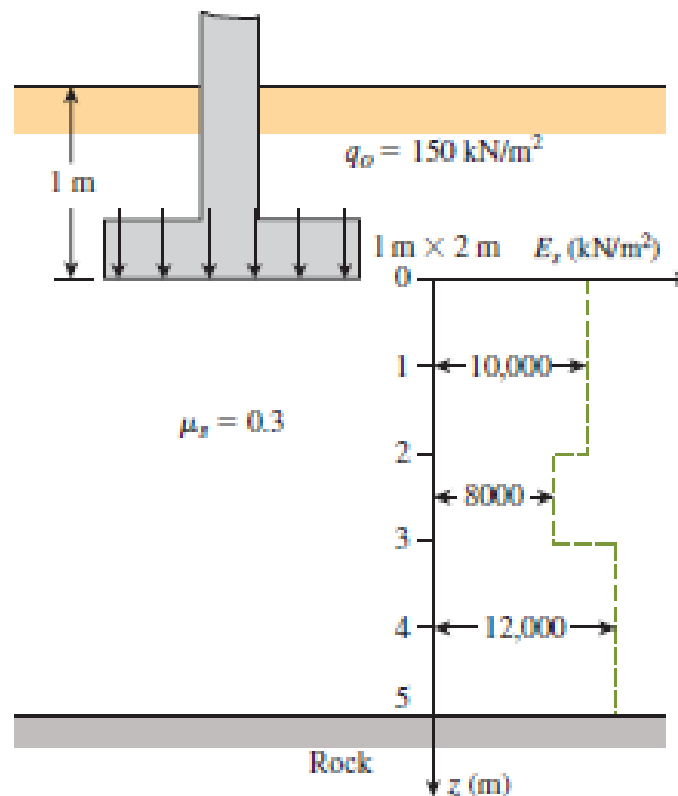
$E_{s(z)}$  = soil modulus of elasticity within a depth  $\Delta z$

$\bar{z}$  =  $H$  or  $5B$ , whichever is smaller

# EXAMPLE 9.2

## EXAMPLE 9.2

A flexible shallow foundation  $1\text{ m} \times 2\text{ m}$  is shown in Figure Calculate the elastic settlement at the center of the foundation.



# EXAMPLE 9.2

$$S_e = \frac{q_o B}{E_s} (1 - \mu_s^2) I_s I_f$$

## SOLUTION

We are given that  $B = 1$  m and  $L = 2$  m. Note that  $\bar{z} = 5$  m  $= 5B$ . From Eq. (9.23),

$$E_s = \frac{\sum E_{s(i)} \Delta z}{\bar{z}} = \frac{(10,000)(2) + (8000)(1) + (12,000)(2)}{5} = 10,400 \text{ kN/m}^2$$

For one of the four quarters of the foundation,  $B = 0.5$  m and  $L = 1.0$  m. Also,  $H = 6.0$  m (Note: The Steinbrenner factors in Tables 9.3 and 9.4 are for surface foundations with  $D_f = 0$ .)

**H=6.0 m**

$$m' = L/B = 2.0 \text{ and } n' = H/B = 12.0$$

From Table 9.3,  $F_1 = 0.653$ , and from Table 9.4,  $F_2 = 0.028$ .

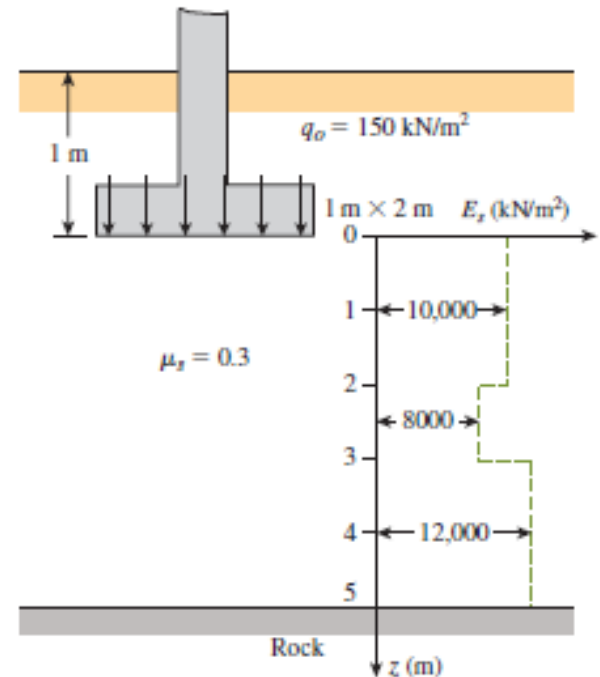
From Eq. (9.11), with  $\mu_s = 0.3$ ,

$$I_s = F_1 + \left( \frac{1 - 2\mu_s}{1 - \mu_s} \right) F_2 = 0.653 + \left( \frac{1 - 2 \times 0.3}{1 - 0.3} \right) (0.028) = 0.669$$

For  $\mu_s = 0.3$ ,  $L/B = 2$  and  $D_f/B = 1$  (using  $B = 1$  m for the entire foundation); from Figure 9.5b,  $I_f = 0.71$ .

From Eq. (9.22) and considering the four quarters,

$$S_e = \frac{q_o B}{E_s} (1 - \mu_s^2) I_s I_f = \frac{(150)(0.5)}{(10,400)} (1 - 0.3^2) (0.669 \times 4) (0.71) = 0.0124 \text{ m} = \mathbf{12.4 \text{ mm}}$$




**B = 0.5 m**  
**L = 1.0 m**

# Improved Equation for Elastic Settlement

## The improved formula takes into account

1. The rigidity of the foundation
2. The depth of embedment of the foundation
3. The increase in the modulus of elasticity of the soil with depth
4. The location of rigid layers at a limited depth

$$S_e = \frac{q_o B_e I_G I_F I_E}{E_o} (1 - \mu_s^2)$$

where

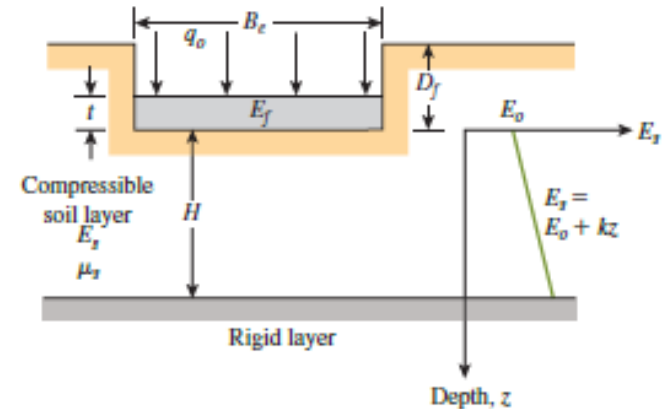
$I_G$  = influence factor for the variation of  $E_s$  with depth

$$= f\left(\beta = \frac{E_o}{kB_e}, \frac{H}{B_e}\right)$$

$I_F$  = foundation rigidity correction factor

$I_E$  = foundation embedment correction factor

$B_e$  = the equivalent diameter



$B_e$  of a rectangular foundation,

$$B_e = \sqrt{\frac{4BL}{\pi}}$$

$B$  = width of foundation

$L$  = length of foundation

For circular foundations,

$$B_e = B$$

$B$  = diameter of foundation.

# Improved Equation for Elastic Settlement

$$S_e = \frac{q_o B_e I_G I_F I_E}{E_o} (1 - \mu_s^2)$$

$I_G$  = influence factor for the variation of  $E_s$  with depth

$$= f\left(\beta = \frac{E_o}{kB_e}, \frac{H}{B_e}\right)$$

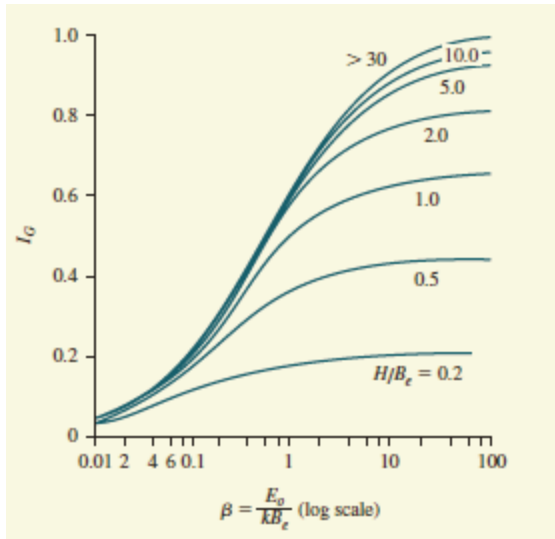
$I_F$  = foundation rigidity correction factor

$I_E$  = foundation embedment correction factor

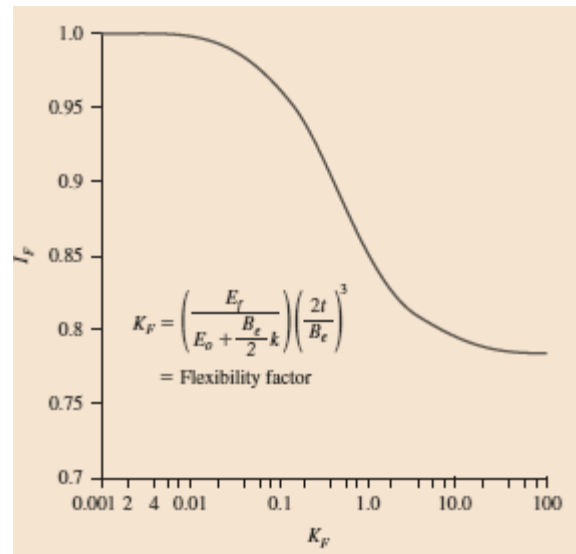
$$I_F = \frac{\pi}{4} + \frac{1}{4.6 + 10 \left( \frac{E_f}{E_o + \frac{B_e k}{2}} \right) \left( \frac{2t}{B_e} \right)^3}$$

$$I_E = 1 - \frac{1}{3.5 \exp(1.22\mu_s - 0.4) \left( \frac{B_e}{D_f} + 1.6 \right)}$$

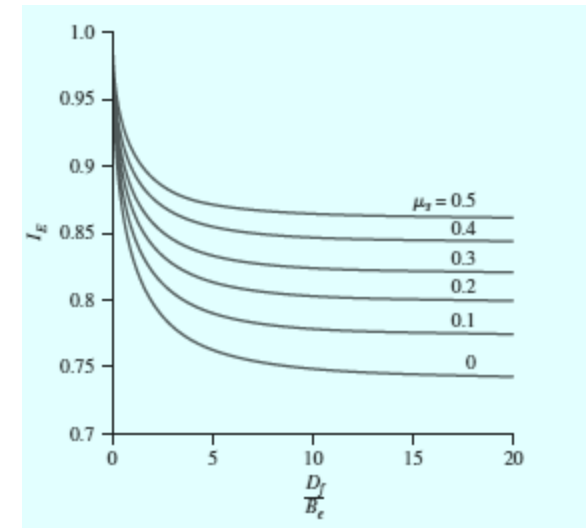
# Improved Equation for Elastic Settlement



$I_G$



$I_F$



$I_E$

# EXAMPLE 9.3

## EXAMPLE 9.3

For a shallow foundation supported by a silty sand, as shown in Figure

Length =  $L = 3$  m

Width =  $B = 1.5$  m

Depth of foundation =  $D_f = 1.5$  m

Thickness of foundation =  $t = 0.3$  m

Load per unit area =  $q_o = 240$  kN/m<sup>2</sup>

$E_f = 16 \times 10^6$  kN/m<sup>2</sup>

The silty sand soil has the following properties:

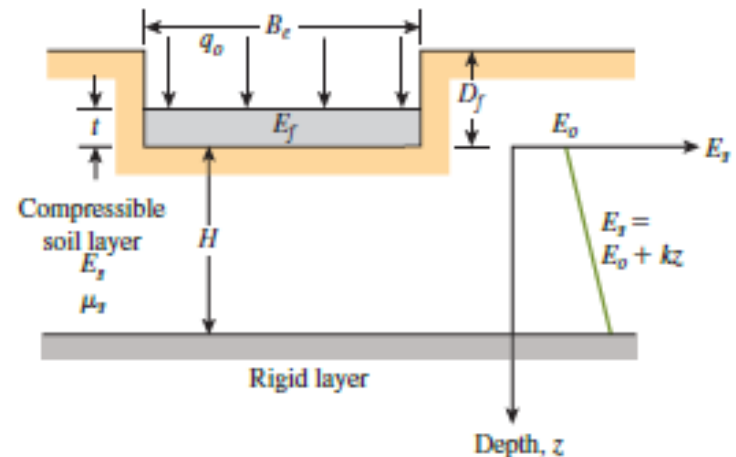
$H = 3.7$  m

$\mu_s = 0.3$

$E_o = 9700$  kN/m<sup>2</sup>

$k = 575$  kN/m<sup>2</sup>/m

Estimate the elastic settlement of the foundation.



## Example 9.3

### SOLUTION

From Eq. (9.24), the equivalent diameter is

$$B_e = \sqrt{\frac{4BL}{\pi}} = \sqrt{\frac{(4)(1.5)(3)}{\pi}} = 2.39 \text{ m}$$

so

$$\beta = \frac{E_o}{kB_e} = \frac{9700}{(575)(2.39)} = 7.06$$

and

$$\frac{H}{B_e} = \frac{3.7}{2.39} = 1.55$$

From Figure 9.8, for  $\beta = 7.06$  and  $H/B_e = 1.55$ , the value of  $I_G \approx 0.7$ . From Eq. (9.28),

$$\begin{aligned} I_r &= \frac{\pi}{4} + \frac{1}{4.6 + 10 \left( \frac{E_f}{E_o + \frac{B_e}{2} k} \right) \left( \frac{2l}{B_e} \right)^3} \\ &= \frac{\pi}{4} + \frac{1}{4.6 + 10 \left[ \frac{16 \times 10^6}{9700 + \left( \frac{2.39}{2} \right) (575)} \right] \left[ \frac{(2)(0.3)}{2.39} \right]^3} = 0.789 \end{aligned}$$

## Example 9.3

From Eq. (9.29),

$$\begin{aligned} I_E &= 1 - \frac{1}{3.5 \exp(1.22\mu_s - 0.4) \left( \frac{B_e}{D_f} + 1.6 \right)} \\ &= 1 - \frac{1}{3.5 \exp[(1.22)(0.3) - 0.4] \left( \frac{2.39}{1.5} + 1.6 \right)} = 0.907 \end{aligned}$$

From Eq. (9.27),

$$S_e = \frac{q_o B_e I_G I_F I_E}{E_o} (1 - \mu_s^2)$$

so, with  $q_o = 240 \text{ kN/m}^2$ , it follows that

$$S_e = \frac{(240)(2.39)(0.7)(0.789)(0.907)}{9700} (1 - 0.3^2) \approx 0.02696 \text{ m} \approx \mathbf{27 \text{ mm}}$$

# Settlement of Sandy Soil: Use of Strain Influence Factor

## Strain Influence Factor

- I. **Solution of Schmertmann et al. (1978)**
  
- II. **Solution of Terzaghi et al. (1996)**

# Settlement of Sandy Soil: Use of Strain Influence Factor

## I. Solution of Schmertmann et al. (1978)

$$S_e = C_1 C_2 (\bar{q} - q) \sum_0^{z_2} \frac{I_z}{E_s} \Delta z$$

$I_z$  = strain influence factor

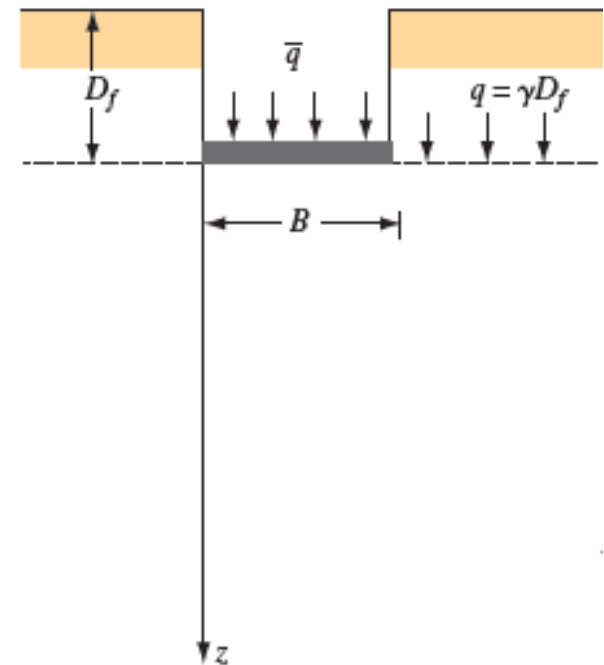
$C_1$  = a correction factor for the depth of foundation embedment  
=  $1 - 0.5 [q/(\bar{q} - q)]$

$C_2$  = a correction factor to account for creep in soil  
=  $1 + 0.2 \log (\text{time in years}/0.1)$

$\bar{q}$  = stress at the level of the foundation

$q = \gamma D_f$  = effective stress at the base of the foundation

$E_s$  = modulus of elasticity of soil



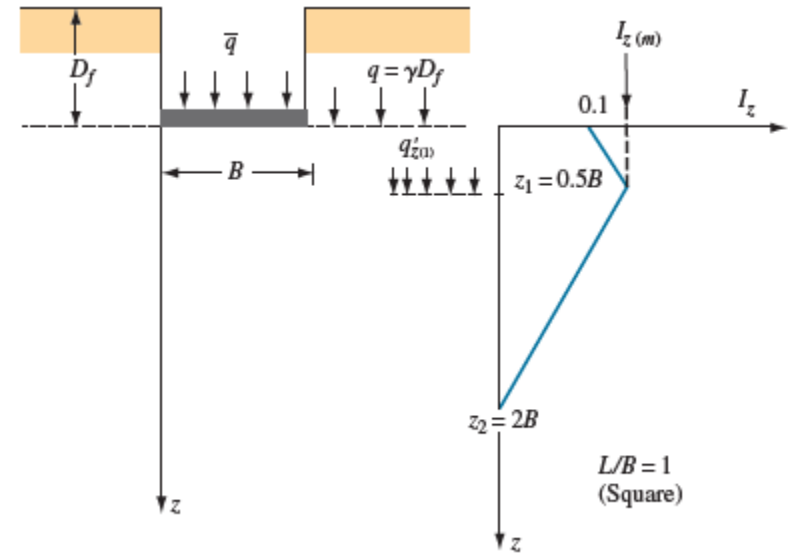
# I. Solution of Schmertmann et al. (1978)

## Square ( $L/B = 1$ ) or circular foundations

$z$	$I_z$
<b>0</b>	<b>0.1</b>
$Z_1 = 0.5 B$	$I_{z(m)}$
$Z_2 = 2 B$	<b>0</b>

$$I_{z(m)} = 0.5 + 0.1 \sqrt{\frac{\bar{q} - q}{q'_{z_1(t)}}}$$

$q'_{z_1(t)}$  = effective stress at a depth of  $z_1$  before construction of the foundation



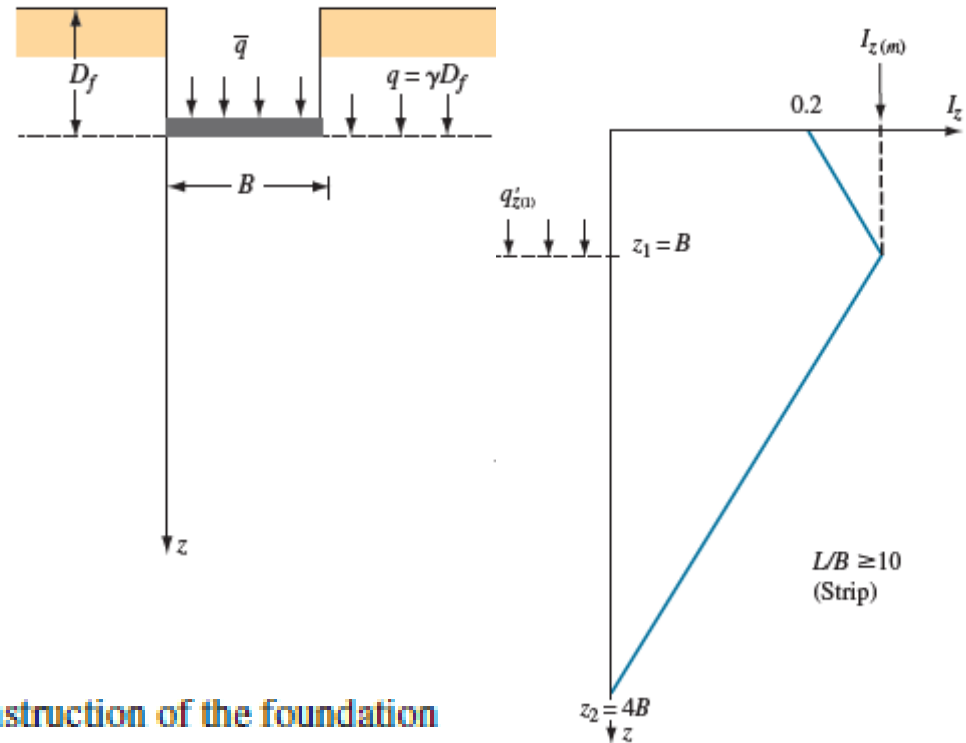
# I. Solution of Schmertmann et al. (1978)

## Foundation with $L/B \geq 10$

$z$	$I_z$
0	0.2
$Z_1 = B$	$I_{z(m)}$
$Z_2 = 4B$	0

$$I_{z(m)} = 0.5 + 0.1 \sqrt{\frac{\bar{q} - q}{q'_{z(1)}}}$$

$q'_{z(1)}$  = effective stress at a depth of  $z_1$  before construction of the foundation



# I. Solution of Schmertmann et al. (1978)

## Rectangular foundations

The following relations are suggested by Salgado (2008) for interpolation of  $I_z$  at  $z = 0$ ,  $z_1/B$ , and  $z_2/B$  for rectangular foundations.

- $I_z$  at  $z = 0$

$$I_z = 0.1 + 0.0111 \left( \frac{L}{B} - 1 \right) \leq 0.2$$

- $z_1/B$

$$\frac{z_1}{B} = 0.5 + 0.0555 \left( \frac{L}{B} - 1 \right) \leq 1$$

- $z_2/B$

$$\frac{z_2}{B} = 2 + 0.222 \left( \frac{L}{B} - 1 \right) \leq 4$$

# I. Solution of Schmertmann et al. (1978)

## $E_s$ Modulus of Elasticity of Soil

Schmertmann et al. (1978) suggested that

$$E_s = 2.5q_c \text{ (for square foundation)}$$

and

$$E_s = 3.5q_c \text{ (for } L/B \geq 10 \text{)}$$

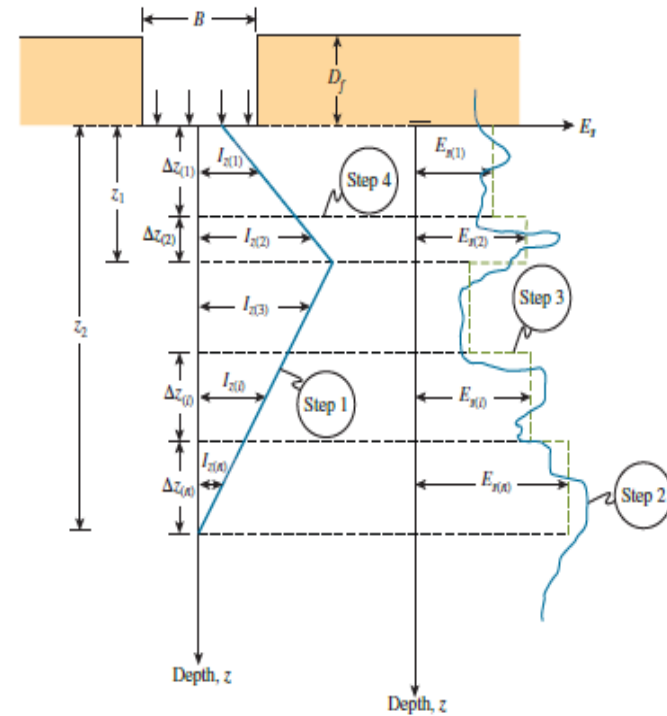
where  $q_c$  is the cone penetration resistance.

It appears reasonable to write (Terzaghi et al., 1996)

$$E_{s(\text{rectangle})} = \left( 1 + 0.4 \log \frac{L}{B} \right) E_{s(\text{square})}$$

# Procedure for calculation of $S_e$ using the strain influence factor

- Step 1.** Plot the foundation and the variation of  $I_z$  with depth to scale
- Step 2.** Using the correlation from standard penetration resistance ( $N_{60}$ ) or cone penetration resistance ( $q_c$ ), plot the actual variation of  $E_s$  with depth
- Step 3.** Approximate the actual variation of  $E_s$  into a number of layers of soil having a constant  $E_s$ , such as  $E_{s(1)}$ ,  $E_{s(2)}$ ,  $\dots$ ,  $E_{s(i)}$ ,  $\dots$ ,  $E_{s(n)}$
- Step 4.** Divide the soil layer from  $z = 0$  to  $z = z_2$  into a number of layers by drawing horizontal lines. The number of layers will depend on the break in continuity in the  $I_z$  and  $E_s$  diagrams.



# Procedure for calculation of $S_e$ using the strain influence factor

**Step 5.** Prepare a table (such as Table 9.5) to obtain  $\sum \frac{I_z}{E_s} \Delta z$ .

**Step 6.** Calculate  $C_1$  and  $C_2$ .

**Step 7.** Calculate  $S_e$

$$S_e = C_1 C_2 (\bar{q} - q) \sum_0^z \frac{I_z}{E_s} \Delta z$$

**TABLE 9.5** Calculation of  $\sum \frac{I_z}{E_s} \Delta z$

Layer no.	$\Delta z$	$E_s$	$I_z$ at the middle of the layer	$\frac{I_z}{E_s} \Delta z$
1	$\Delta z_{(1)}$	$E_{s(1)}$	$I_{z(1)}$	$\frac{I_{z(1)}}{E_{s(1)}} \Delta z_1$
2	$\Delta z_{(2)}$	$E_{s(2)}$	$I_{z(2)}$	
⋮	⋮	⋮	⋮	
$i$	$\Delta z_{(i)}$	$E_{s(i)}$	$I_{z(i)}$	$\frac{I_{z(i)}}{E_{s(i)}} \Delta z_i$
⋮	⋮	⋮	⋮	⋮
$n$	$\Delta z_{(n)}$	$E_{s(n)}$	$I_{z(n)}$	$\frac{I_{z(n)}}{E_{s(n)}} \Delta z_n$
				$\sum \frac{I_z}{E_s} \Delta z$

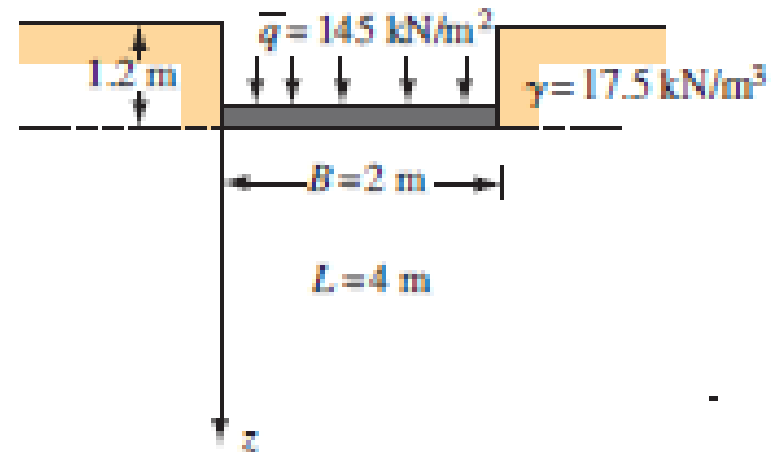
# EXAMPLE 9.4

## EXAMPLE 9.4

Consider a rectangular foundation  $2\text{ m} \times 4\text{ m}$  in plan at a depth of  $1.2\text{ m}$  in a sand deposit, as shown in Figure 9.13a. Given:  $\gamma = 17.5\text{ kN/m}^3$ ,  $\bar{q} = 145\text{ kN/m}^2$ , and the following approximated variation of  $q_c$  with  $z$ :

$z$ (m)	$q_c$ (kN/m <sup>2</sup> )
0–0.5	2250
0.5–2.5	3430
2.5–6.0	2950

Estimate the elastic settlement of the foundation using the strain influence factor method.



# EXAMPLE 9.4

Step 1. Plot the foundation and the variation of  $I_z$  with depth to scale

## Rectangular Foundation

- $I_z$  at  $z = 0$

$$I_z = 0.1 + 0.0111 \left( \frac{L}{B} - 1 \right) \leq 0.2$$

- $z_1/B$

$$\frac{z_1}{B} = 0.5 + 0.0555 \left( \frac{L}{B} - 1 \right) \leq 1$$

- $z_2/B$

$$\frac{z_2}{B} = 2 + 0.222 \left( \frac{L}{B} - 1 \right) \leq 4$$

at  $z = 0$ ,

$$I_z = 0.1 + 0.0111 \left( \frac{L}{B} - 1 \right) = 0.1 + 0.0111 \left( \frac{4}{2} - 1 \right) \approx 0.11$$

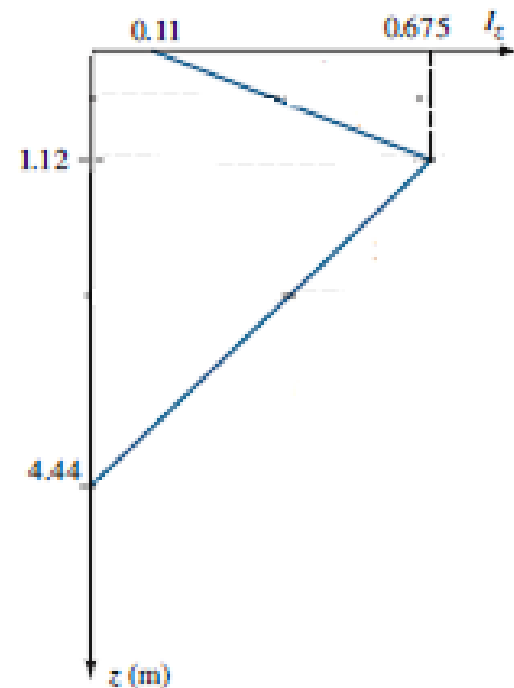
$$\frac{z_1}{B} = 0.5 + 0.0555 \left( \frac{L}{B} - 1 \right) = 0.5 + 0.0555 \left( \frac{4}{2} - 1 \right) \approx 0.56$$

$$z_1 = (0.56)(2) = 1.12 \text{ m}$$

$$\frac{z_2}{B} = 2 + 0.222 \left( \frac{L}{B} - 1 \right) = 2 + 0.222(2 - 1) = 2.22$$

$$z_2 = (2.22)(2) = 4.44 \text{ m}$$

$$I_{z(m)} = 0.5 + 0.1 \sqrt{\frac{\bar{q} - q}{q'_{z(1)}}} = 0.5 + 0.1 \left[ \frac{145 - (1.2 \times 17.5)}{(1.2 + 1.12)(17.5)} \right]^{0.5} = 0.675$$



## EXAMPLE 9.4

*Step 2.* Using the correlation from standard penetration resistance ( $N_{60}$ ) or cone penetration resistance ( $q_c$ ), plot the actual variation of  $E_s$  with depth

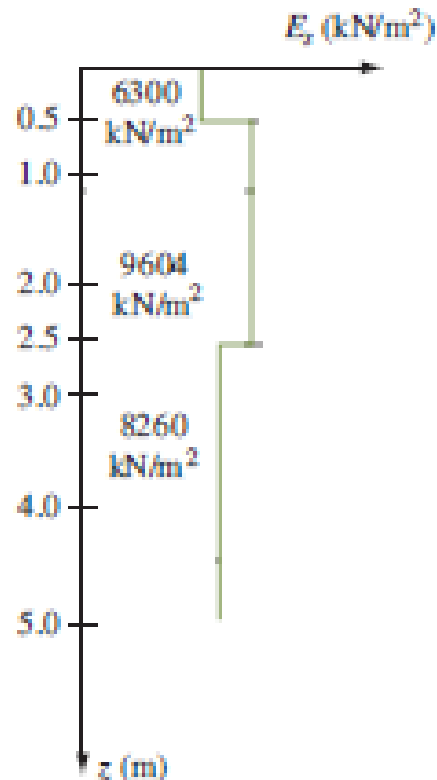
$$E_{s(\text{rectangle})} = \left(1 + 0.4 \log \frac{L}{B}\right) E_{s(\text{square})} = \left[1 + 0.4 \log \left(\frac{4}{2}\right)\right] (2.5 \times q_c) = 2.8 q_c$$

the approximated variation of  $E_s$  with  $z$  is as follows:

$z$ (m)	$q_c$ (kN/m <sup>2</sup> )	$E_s$ (kN/m <sup>2</sup> )
0–0.5	2250	6300
0.5–2.5	3430	9604
2.5–6.0	2950	8260

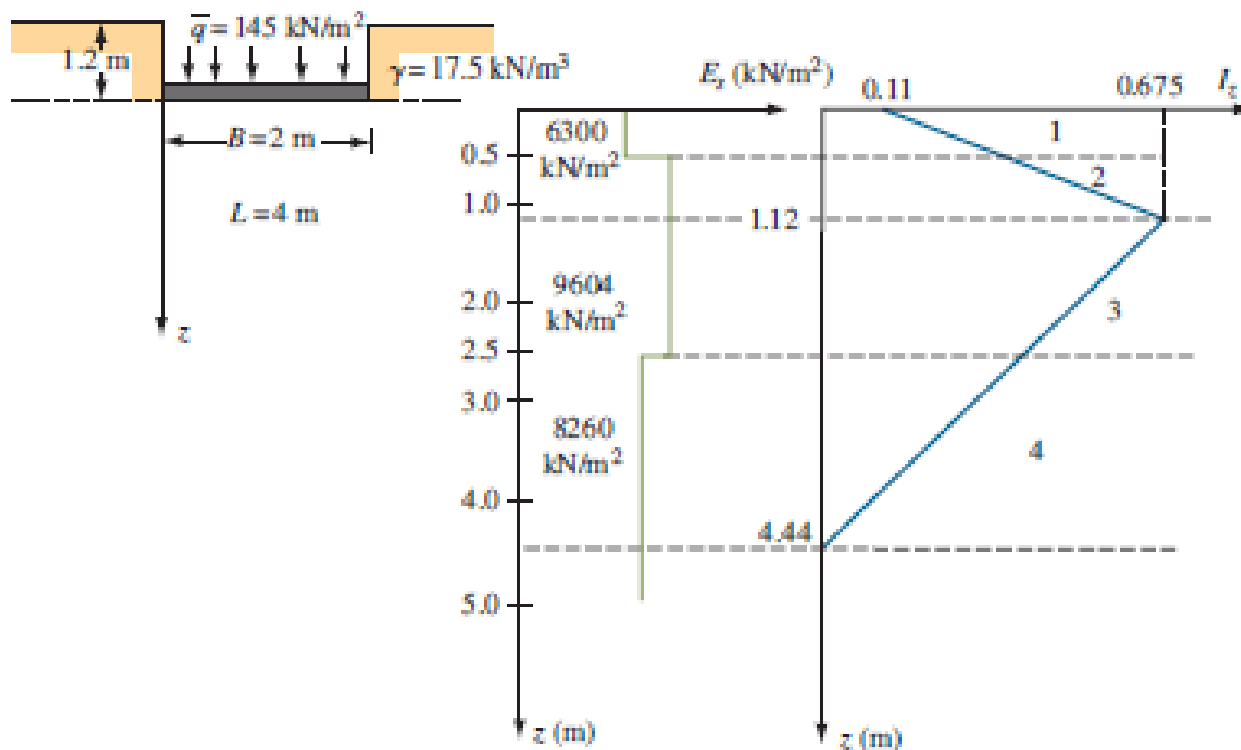
# EXAMPLE 9.4

*Step 3.* Approximate the actual variation of  $E_s$  into a number of layers of soil having a constant  $E_s$ , such as  $E_{s(1)}$ ,  $E_{s(2)}$ ,  $\dots$ ,  $E_{s(i)}$ ,  $\dots$ ,  $E_{s(n)}$



# EXAMPLE 9.4

*Step 4.* Divide the soil layer from  $z = 0$  to  $z = z_2$  into a number of layers by drawing horizontal lines. The number of layers will depend on the break in continuity in the  $I_z$  and  $E_s$  diagrams.



## EXAMPLE 9.4

*Step 5.* Prepare a table to obtain  $\sum \frac{I_z}{E_s} \Delta z$ .

Layer no.	$\Delta z$ (m)	$E_s$ (kN/m <sup>2</sup> )	$I_z$ at middle of layer	$\frac{I_z}{E_s} \Delta z$ (m <sup>3</sup> /kN)
1	0.50	6300	0.236	$1.87 \times 10^{-5}$
2	0.62	9604	0.519	$3.35 \times 10^{-5}$
3	1.38	9604	0.535	$7.68 \times 10^{-5}$
4	1.94	8260	0.197	$4.62 \times 10^{-5}$
				$\Sigma 17.52 \times 10^{-5}$

## EXAMPLE 9.4

*Step 6.* Calculate  $C_1$  and  $C_2$ .

*Step 7.* Calculate  $S_e$

$$S_e = C_1 C_2 (\bar{q} - q) \sum \frac{I_z}{E_s} \Delta z$$

$$C_1 = 1 - 0.5 \left( \frac{q}{\bar{q} - q} \right) = 1 - 0.5 \left( \frac{21}{145 - 21} \right) = 0.915$$

Assume the time for creep is 10 years. So,

$$C_2 = 1 + 0.2 \log \left( \frac{10}{0.1} \right) = 1.4$$

Hence,

$$S_e = (0.915)(1.4)(145 - 21)(17.52 \times 10^{-5}) = 2783 \times 10^{-5} \text{ m} = 27.83 \text{ mm}$$

## II. Solution of Terzaghi et al. (1996)

$$S_e = C_d(\bar{q} - q) \sum_0^{z_2} \frac{I_z}{E_s} \Delta z + \underbrace{0.02 \left[ \frac{0.1}{\sum (q_c \Delta z)} \right] z_2 \log \left( \frac{t \text{ days}}{1 \text{ day}} \right)}_{\text{Postconstruction settlement}}$$

$q_c$  is in  $\text{MN/m}^2$ .

$C_d$  is the depth factor

## II. Solution of Terzaghi et al. (1996)

Terzaghi et al. (1996) proposed a slightly different form of the strain influence factor diagram

At  $z = 0$ ,  $I_z = 0.2$  (for all  $L/B$  values)

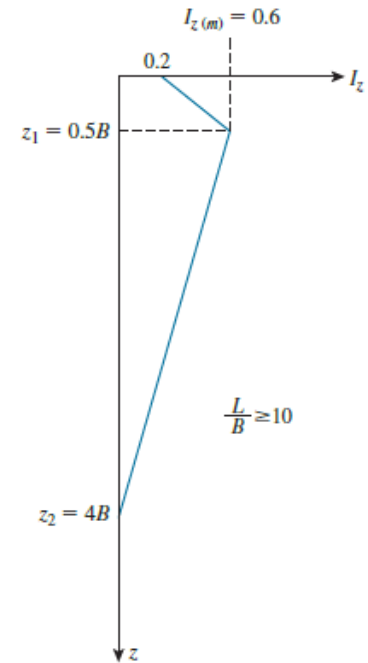
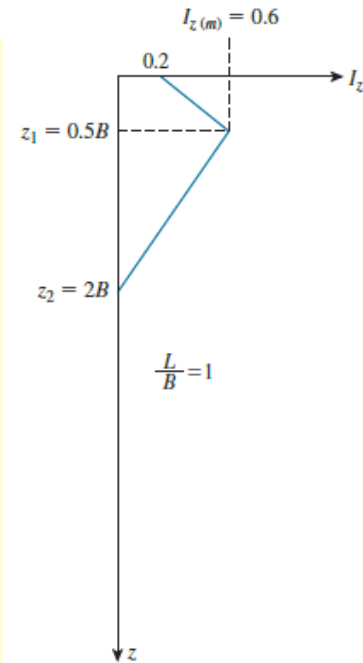
At  $z = z_1 = 0.5B$ ,  $I_z = 0.6$  (for all  $L/B$  values)

At  $z = z_2 = 2B$ ,  $I_z = 0$  (for  $L/B = 1$ )

At  $z = z_2 = 4B$ ,  $I_z = 0$  (for  $L/B \geq 10$ )

For  $L/B$  between 1 and 10 (or  $> 10$ ),

$$\frac{z_2}{B} = 2 \left[ 1 + \log \left( \frac{L}{B} \right) \right]$$



## II. Solution of Terzaghi et al. (1996)

$$E_s = 3.5q_c \text{ (for square and circular foundations)}$$

$$E_{s(\text{rectangular})} = \left[ 1 + 0.4 \log\left(\frac{L}{B}\right) \right] E_{s(\text{square})} \leq 1.4E_{s(\text{square})}$$

$C_d$  is the depth factor



**TABLE 9.6** Variation of  $C_d$  with  $D_f/B^*$

$D_f/B$	$C_d$
0.1	1
0.2	0.96
0.3	0.92
0.5	0.86
0.7	0.82
1.0	0.77
2.0	0.68
3.0	0.65

\*Based on data from Terzaghi et al. (1996)

# Example 9.5

## EXAMPLE 9.5

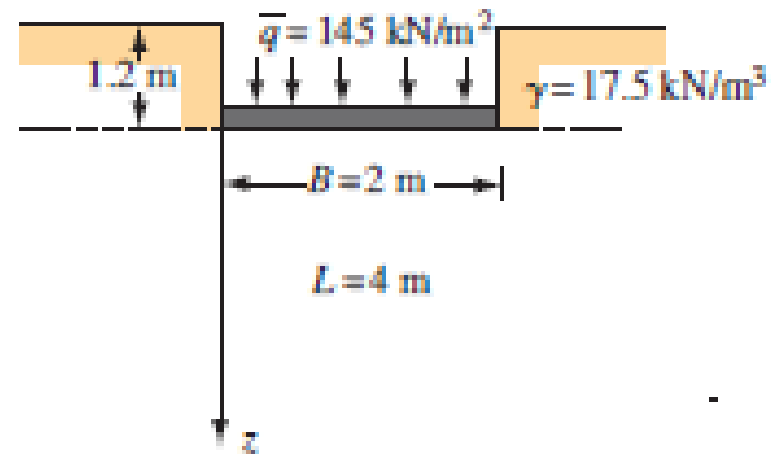
Solve Example 9.4 using the method of Terzaghi et al. (1996).

## EXAMPLE 9.4

Consider a rectangular foundation  $2\text{ m} \times 4\text{ m}$  in plan at a depth of  $1.2\text{ m}$  in a sand deposit, as shown in Figure 9.13a. Given:  $\gamma = 17.5\text{ kN/m}^3$ ,  $\bar{q} = 145\text{ kN/m}^2$ , and the following approximated variation of  $q_c$  with  $z$ :

$z$ (m)	$q_c$ (kN/m <sup>2</sup> )
0–0.5	2250
0.5–2.5	3430
2.5–6.0	2950

Estimate the elastic settlement of the foundation using the strain influence factor method.



# Example 9.5

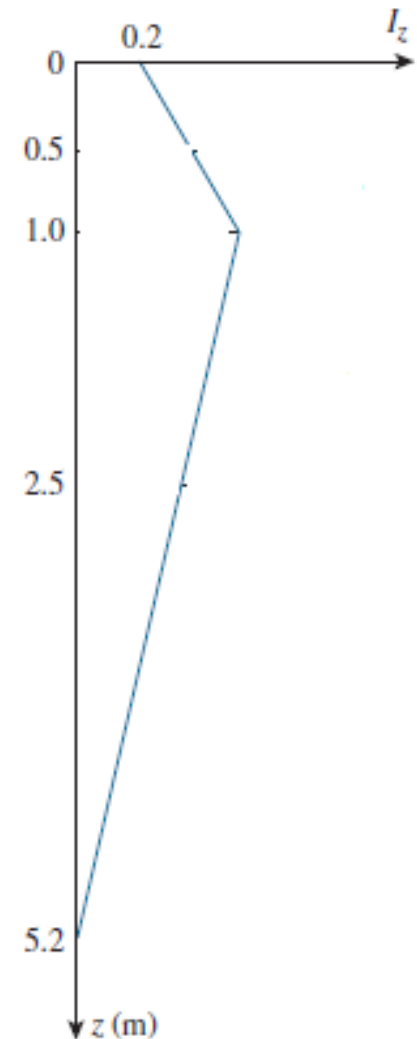
Given:  $L/B = 4/2 = 2$ .

Figure shows the plot of  $I_z$  with depth below the foundation. Note that

$$\frac{z_2}{B} = 2 \left[ 1 + \log \left( \frac{L}{B} \right) \right] = 2[1 + \log(2)] = 2.6$$

or

$$z_2 = (2.6)(B) = (2.6)(2) = 5.2 \text{ m}$$

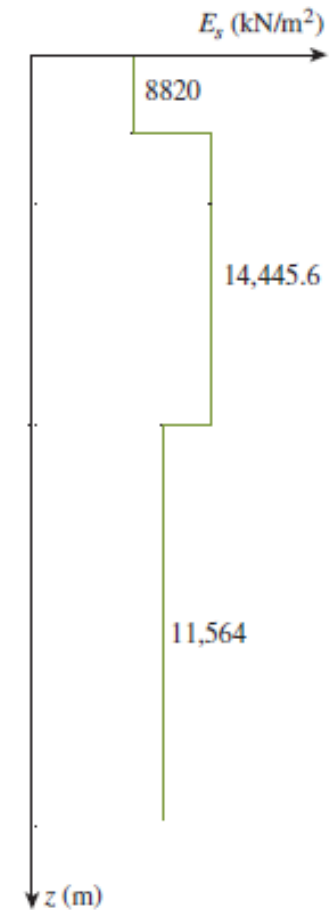


# Example 9.5

$$E_s = \left[ 1 + 0.4 \log\left(\frac{L}{B}\right) \right] (3.5q_c) = \left[ 1 + 0.4 \log\left(\frac{4}{2}\right) \right] (3.5q_c) = 3.92q_c$$

The following table can be prepared and shows the variation of  $E_s$  with depth

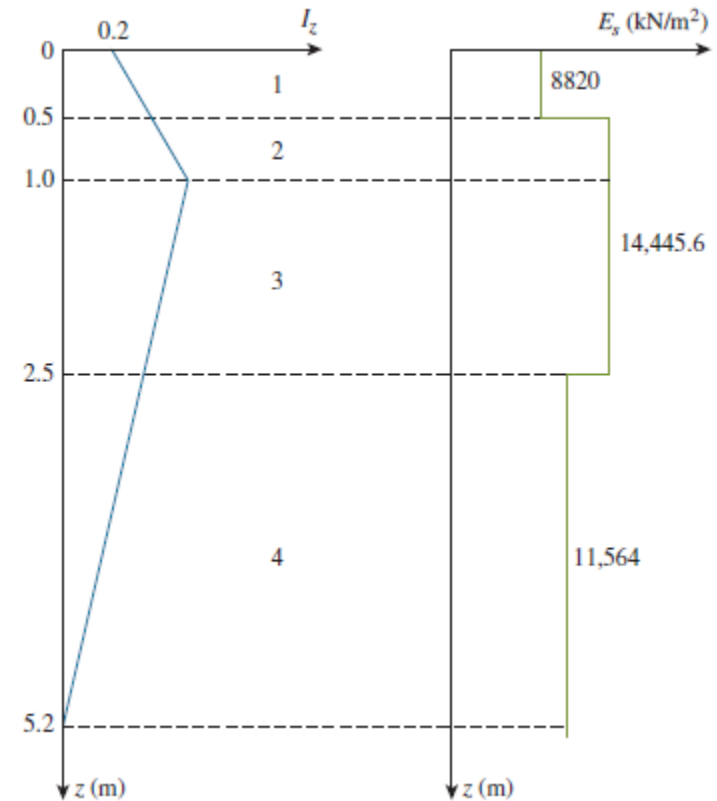
$z$ (m)	$q_c$ (kN/m <sup>2</sup> )	$E_s$ (kN/m <sup>2</sup> )
0–0.5	2250	8820
0.5–2.5	3430	14,445.6
2.5–6	2950	11,564



# Example 9.5

The following table is used to calculate  $\sum_0^z \frac{I_z}{E_s} \Delta z$ .

Layer no.	$\Delta z$ (m)	$E_s$ (kN/m <sup>2</sup> )	$I_z$ at the middle of the layer	$\frac{I_z}{E_s} \Delta z$ (m <sup>2</sup> /kN)
1	0.5	8820	0.3	$1.7 \times 10^{-5}$
2	0.5	14,445.6	0.5	$1.73 \times 10^{-5}$
3	1.5	14,445.6	0.493	$5.12 \times 10^{-5}$
4	2.7	11,564	0.193	$4.5 \times 10^{-5}$
				$\Sigma 13.06 \times 10^{-5} \text{ m}^2/\text{kN}$



## Example 9.5

$D_f/B = 1.2/2 = 0.6$ . From Table 9.6,  $C_d \approx 0.85$ .

$$C_d(\bar{q} - q) \sum_0^{z_2} \frac{I_z}{E_s} \Delta z = (0.85)(145 - 21)(13.06 \times 10^{-5}) = 1376.5 \times 10^{-5} \text{ m}$$

Postconstruction creep is

$$0.02 \left[ \frac{0.1}{\sum (q_c \Delta z)} \right] z_2 \log \left( \frac{t \text{ days}}{1 \text{ day}} \right)$$

$$\begin{aligned} \frac{\sum (q_c \Delta z)}{z_2} &= \frac{(2250 \times 0.5) + (3430 \times 2) + (2950 \times 2.7)}{5.2} \\ &= 3067.3 \text{ kN/m}^2 \approx 3.07 \text{ MN/m}^2 \end{aligned}$$

$$\begin{aligned} S_e &= 1376.5 \times 10^{-5} + 0.02 \left[ \frac{0.1}{3.07} \right] (5.2) \log \left( \frac{10 \times 365 \text{ days}}{1 \text{ day}} \right) \\ &= 2583.3 \times 10^{-5} \text{ m} \\ &\approx \mathbf{25.83 \text{ mm}} \end{aligned}$$

# Examples 9.4 & 9.5

Example	Method	$S_e$ (mm)
Example 9.4	Schmertmann et al. (1978)	27.83
Example 9.5	Terzaghi et al. (1996)	25.83

## Notes:

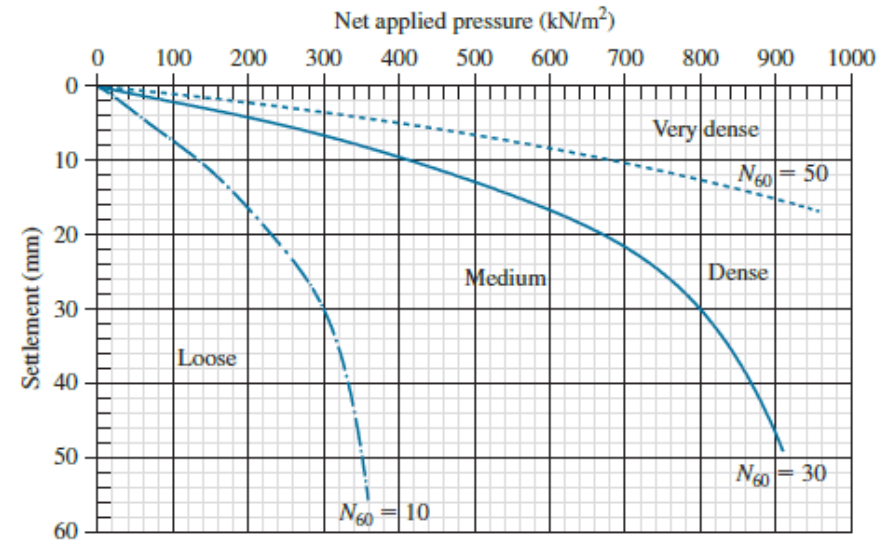
- The magnitude of  $S_e$  in Example 9.5 is about 93% of that found in Example 9.4.
- In Example 9.4, the elastic settlement was about 19.88 mm, and settlement due to creep was about 7.95 mm.
- In Example 9.5, elastic settlement is about 13.77 mm, and the settlement due to creep is about 12.07 mm.
- The magnitude of creep settlement is about 50% more in Example 9.5.
- The magnitude of elastic settlement in Example 9.4 is about 30% more compared to that in Example 9.5. This is because of the assumption of the  $E_s - q_c$  relationship.

# Settlement of Foundation on Sand Based on Standard Penetration Resistance

## I. Terzaghi and Peck's Method

$$S_{e, \text{foundation}} = S_{e, \text{plate}} \left( \frac{2B}{B + 0.3} \right)^2 \left( 1 - \frac{1}{4} \frac{D_f}{B} \right)$$

where  $B$  is in meters



Settlement of 300 mm × 300 mm plate

- Leonards (1986) suggested replacing  $\frac{1}{4}$  by  $\frac{1}{3}$ , based on additional load test data.
- The values of  $S_{e, \text{plate}}$  can be obtained from Figure
- These load tests were carried out on thick deposits of normally consolidated drained sand.
- This method was originally proposed for square foundations but can be applied to rectangular and strip foundations with caution.
- The deeper influence zone and increase in the stresses within the underlying soil mass in the case of rectangular or strip foundations are compensated by the increase in the soil stiffness.

# EXAMPLE 9.6

## EXAMPLE 9.6

A 2.5 m square foundation placed at a depth of 1.5 m within a sandy soil applies a net pressure of 120 kN/m<sup>2</sup> to the underlying ground. The sand has  $\gamma = 18.5$  kN/m<sup>3</sup> and  $N_{60} = 25$ . What would be the settlement?

### SOLUTION

For net applied pressure = 120 kN/m<sup>2</sup> and  $N_{60} = 25$ ; from Figure ,  $S_{e, \text{plate}} = 4$  mm.

$$\begin{aligned} S_{e, \text{foundation}} &= S_{e, \text{plate}} \left( \frac{2B}{B + 0.3} \right)^2 \left( 1 - \frac{1}{3} \frac{D_f}{B} \right) \\ &= (4) \left( \frac{2 \times 2.5}{2.5 + 0.3} \right)^2 \left( 1 - \frac{1}{3} \times \frac{1.5}{2.5} \right) = 10.2 \text{ mm} \end{aligned}$$

# Settlement of Foundation on Sand Based on Standard Penetration Resistance

## II. Meyerhof's Method

Meyerhof (1956) proposed a correlation for the *net bearing pressure* for foundations with the standard penetration resistance,  $N_{60}$ . The net pressure has been defined as

$$q_{\text{net}} = \bar{q} - \gamma D_f$$

where  $\bar{q}$  is the stress at the level of the foundation.

### For 25 mm of estimated maximum settlement

$$q_{\text{net}}(\text{kN/m}^2) = \frac{N_{60}}{0.08} \quad (\text{for } B \leq 1.22 \text{ m})$$

$$q_{\text{net}}(\text{kN/m}^2) = \frac{N_{60}}{0.125} \left( \frac{B + 0.3}{B} \right)^2 \quad (\text{for } B > 1.22 \text{ m})$$

Meyerhof (1965) suggested that the net allowable bearing pressure should be increased by about 50%.

# Settlement of Foundation on Sand Based on Standard Penetration Resistance

## II. Meyerhof's Method

Bowles (1977) proposed modified form of the bearing equations

$$q_{\text{net}}(\text{kN/m}^2) = \frac{N_{60}}{0.05} F_d \left( \frac{S_e}{25} \right) \quad (\text{for } B \leq 1.22 \text{ m})$$

$$q_{\text{net}}(\text{kN/m}^2) = \frac{N_{60}}{0.08} \left( \frac{B + 0.3}{B} \right)^2 F_d \left( \frac{S_e}{25} \right) \quad (\text{for } B > 1.22 \text{ m})$$

$$F_d = \text{depth factor} = 1 + 0.33(D_f/B)$$

$B$  = foundation width, in meters

$S_e$  = settlement, in mm

# Settlement of Foundation on Sand Based on Standard Penetration Resistance

## II. Meyerhof's Method

$$S_e(\text{mm}) = \frac{1.25q_{\text{net}}(\text{kN/m}^2)}{N_{60}F_d} \quad (\text{for } B \leq 1.22 \text{ m})$$

$$S_e(\text{mm}) = \frac{2q_{\text{net}}(\text{kN/m}^2)}{N_{60}F_d} \left( \frac{B}{B + 0.3} \right)^2 \quad (\text{for } B > 1.22 \text{ m})$$

The  $N_{60}$  is the standard penetration resistance between the bottom of the foundation and  $2B$  below the bottom.

# Settlement of Foundation on Sand Based on Standard Penetration Resistance

## III. Burland and Burbidge's Method

### 1. Variation of Standard Penetration Number with Depth:

Obtain the field penetration numbers  $N_{60}$  with depth at the location of the foundation

The following adjustments of  $N_{60}$  may be necessary:

For gravel or sandy gravel

$$N_{60(a)} = 1.25 N_{60}$$

For fine sand or silty sand below the groundwater table and  $N_{60} > 15$ ,

$$N_{60(a)} = 15 + 0.5(N_{60} - 15)$$

where  $N_{60(a)}$  = adjusted  $N_{60}$  value.

# Settlement of Foundation on Sand Based on Standard Penetration Resistance

## III. Burland and Burbidge's Method

### 2. Determination of Depth of Stress Influence ( $z'$ ):

In determining the depth of stress influence, the following three cases may arise:

**Case I.** If  $N_{60}$  [or  $N_{60(a)}$ ] is approximately constant with depth, calculate  $z'$  from

$$\frac{z'}{B_R} = 1.4 \left( \frac{B}{B_R} \right)^{0.75}$$

where

$B_R$  = reference width = 0.3 m (if  $B$  is in m)

$B$  = width of the actual foundation

**Case II.** If  $N_{60}$  [or  $N_{60(a)}$ ] is increasing with depth, use the above Equation.

**Case III.** If  $N_{60}$  [or  $N_{60(a)}$ ] is decreasing with depth,  $z' = 2B$  or to the bottom of soft soil layer measured from the bottom of the foundation (whichever is smaller).

# Settlement of Foundation on Sand Based on Standard Penetration Resistance

## III. Burland and Burbidge's Method

### 3. Calculation of Elastic Settlement $S_e$

The elastic settlement of the foundation,  $S_e$ , can be calculated from

$$\frac{S_e}{B_R} = \alpha_1 \alpha_2 \alpha_3 \left[ \frac{1.25 \left( \frac{L}{B} \right)}{0.25 + \left( \frac{L}{B} \right)} \right]^2 \left( \frac{B}{B_R} \right)^{0.7} \left( \frac{q'}{p_a} \right)$$

where

$\alpha_1$  = a constant

$\alpha_2$  = compressibility index

$\alpha_3$  = correction for the depth of influence

$p_a$  = atmospheric pressure = 100 kN/m<sup>2</sup>

$L$  = length of the foundation

TABLE 9.7 Summary of  $q'$ ,  $\alpha_1$ ,  $\alpha_2$ , and  $\alpha_3$

Soil type	$q'$	$\alpha_1$	$\alpha_2$	$\alpha_3$
Normally consolidated sand	$q_{net}$	0.14	$\frac{1.71}{[\bar{N}_{60} \text{ or } \bar{N}_{60(a)}]^{1.4}}$	
Overconsolidated sand ( $q_{net} \leq \sigma'_c$ )	$q_{net}$	0.047	$\frac{0.57}{[\bar{N}_{60} \text{ or } \bar{N}_{60(a)}]^{1.4}}$	$\alpha_3 = \frac{H}{z'} \left( 2 - \frac{H}{z'} \right)$ (if $H \leq z'$ ) or $\alpha_3 = 1$ (if $H > z'$ )
where $\sigma'_c$ = preconsolidation pressure				
Overconsolidated sand ( $q_{net} > \sigma'_c$ )	$q_{net} - 0.67\sigma'_c$	0.14	$\frac{0.57}{[\bar{N}_{60} \text{ or } \bar{N}_{60(a)}]^{1.4}}$	where $H$ = depth of compressible layer

Table 9.7 summarizes the values of  $q'$ ,  $\alpha_1$ ,  $\alpha_2$ , and  $\alpha_3$  to be used in Equation for various types of soils. Note that, in this table,  $[\bar{N}_{60} \text{ or } \bar{N}_{60(a)}]$  = average value of  $N_{60}$  or  $N_{60(a)}$  in the depth of stress influence.

# EXAMPLE 9.7

## EXAMPLE 9.7

A shallow foundation measuring  $1.75 \text{ m} \times 1.75 \text{ m}$  is to be constructed over a layer of sand. Given  $D_f = 1 \text{ m}$ ;  $N_{60}$  is generally increasing with depth;  $\bar{N}_{60}$  in the depth of stress influence = 10,  $q_{\text{net}} = 120 \text{ kN/m}^2$ . The sand is normally consolidated. Estimate the elastic settlement of the foundation. Use the Burland and Burbidge method.

### SOLUTION

$$\frac{z'}{B_R} = 1.4 \left( \frac{B}{B_R} \right)^{0.75}$$

Depth of stress influence,

$$z' = 1.4 \left( \frac{B}{B_R} \right)^{0.75} B_R = (1.4)(0.3) \left( \frac{1.75}{0.3} \right)^{0.75} \approx 1.58 \text{ m}$$

$$\frac{S_e}{B_R} = \alpha_1 \alpha_2 \alpha_3 \left[ \frac{1.25 \left( \frac{L}{B} \right)}{0.25 + \left( \frac{L}{B} \right)} \right]^2 \left( \frac{B}{B_R} \right)^{0.7} \left( \frac{q'}{p_a} \right)$$

For normally consolidated sand (Table 9.7),

$$\alpha_1 = 0.14$$

$$\alpha_2 = \frac{1.71}{(\bar{N}_{60})^{1.4}} = \frac{1.71}{(10)^{1.4}} = 0.068$$

$$\alpha_3 = 1$$

$$q' = q_{\text{net}} = 120 \text{ kN/m}^2$$

So,

$$\frac{S_e}{0.3} = (0.14)(0.068)(1) \left[ \frac{(1.25) \left( \frac{1.75}{1.75} \right)}{0.25 + \left( \frac{1.75}{1.75} \right)} \right]^2 \left( \frac{1.75}{0.3} \right)^{0.7} \left( \frac{120}{100} \right)$$

$$S_e \approx 0.0118 \text{ m} = 11.8 \text{ mm}$$

# EXAMPLE 9.8

## EXAMPLE 9.8

Solve Example 9.6 using Meyerhof's method.

### SOLUTION

A shallow foundation measuring 1.75 m × 1.75 m is to be constructed over a layer of sand. Given  $D_f = 1$  m;  $N_{60}$  is generally increasing with depth;  $\bar{N}_{60}$  in the depth of stress influence = 10,  $q_{\text{net}} = 120$  kN/m<sup>2</sup>. The sand is normally consolidated. Estimate the elastic settlement of the foundation.

$$S_e = \frac{2q_{\text{net}}}{(N_{60})(F_d)} \left( \frac{B}{B + 0.3} \right)^2$$

$$F_d = 1 + 0.33(D_f/B) = 1 + 0.33(1/1.75) = 1.19$$

$$S_e = \frac{(2)(120)}{(10)(1.19)} \left( \frac{1.75}{1.75 + 0.3} \right)^2 = 14.7 \text{ mm}$$

# Settlement Estimation Using the $L1 - L2$ Method

Akbas and Kulhawy (2009) evaluated 167 load–displacement relationships obtained from field tests.

$$\frac{Q}{Q_{L2}} = \frac{\left(\frac{S_e}{B}\right)}{0.69\left(\frac{S_e}{B}\right) + 1.68}$$

$S_e/B$  is in percent.

Akbas and Kulhawy (2009) recommended that

- For  $B > 1$  m [from Eq. (6.42) with  $c' = 0$ ]

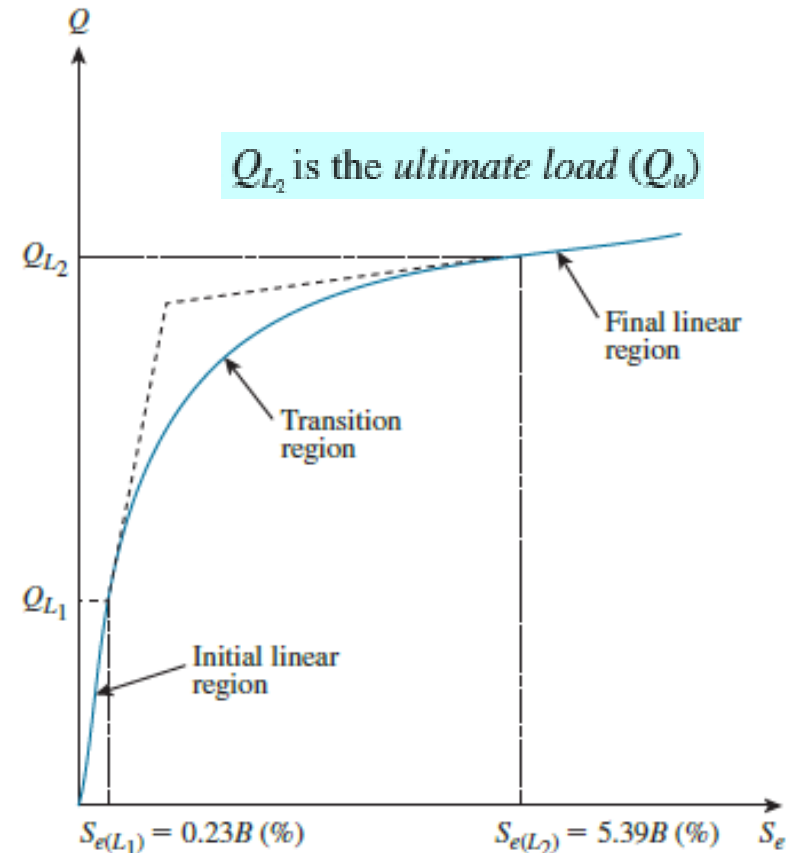
$$Q_{L2} = Q_u = \left[ \frac{1}{2} \gamma B N_\gamma F_{\gamma s} F_{\gamma d} F_{\gamma c} + q N_q F_{qs} F_{qd} F_{qc} \right] A$$

where

$A$  = area of the foundation

- For  $B \leq 1$  m,

$$Q_{L2} = \left[ \frac{1}{2} \gamma N_\gamma F_{\gamma s} F_{\gamma d} F_{\gamma c} + q N_q F_{qs} F_{qd} F_{qc} \right] A$$



# EXAMPLE 9.11

## EXAMPLE 9.11

For a square foundation supported by a sand layer, the following are given:

Foundation:  $B = 1.5 \text{ m}$ ;  $D_f = 1 \text{ m}$

Sand:  $\gamma = 16.5 \text{ kN/m}^3$ ;  $\phi' = 35^\circ$ ;  $G_s = 280 \text{ kN/m}^2$

Load on foundation:  $Q = 800 \text{ kN}$

Estimate:

- $S_{e(L_1)}$
- $S_{e(L_2)}$
- Settlement  $S_e$  with application of load  $Q = 800 \text{ kN}$

**SOLUTION**

**Part a**

$$S_{e(L_1)} = 0.23B (\%) = \frac{(0.23)(1.5 \times 1000)}{100} = 3.45 \text{ mm}$$

**Part b**

$$S_{e(L_2)} = 5.39B (\%) = \frac{(5.39)(1.5 \times 1000)}{100} = 80.85 \text{ mm}$$

# EXAMPLE 9.11

Part c

$B$  is greater than 1 m.

$$Q_{L_2} = \left[ \frac{1}{2} \gamma B N_\gamma F_{\gamma s} F_{\gamma d} F_{\gamma c} + q N_q F_{qs} F_{qd} F_{qc} \right] A$$

$$\gamma = 16.5 \text{ kN/m}^3; B = 1.5 \text{ m}; q = \gamma D_f = (16.5)(1) = 16.5 \text{ kN/m}^2$$

From Table 6.2, for  $\phi' = 35^\circ$ ,  $N_\gamma = 48.03$  and  $N_q = 33.3$ . From Table 6.3,

$$F_{qs} = 1 + \left( \frac{B}{L} \right) \tan \phi' = 1 + \left( \frac{1.5}{1.5} \right) \tan 35 = 1.7$$

$$F_{\gamma s} = 1 - 0.4 \left( \frac{B}{L} \right) = 1 - (0.4) \left( \frac{1.5}{1.5} \right) = 0.6$$

$$F_{qd} = 1 + 2 \tan \phi' (1 - \sin \phi')^2 \left( \frac{D_f}{B} \right) = 1 + 2 \tan 35 (1 - \sin 35)^2 \left( \frac{1}{1.5} \right) \approx 1.17$$

$$F_{\gamma d} = 1$$

In order to calculate  $F_{qc}$  and  $F_{\gamma c}$ , refer to Eq. (6.43) (with  $c' = 0$ ):

$$I_r = \frac{G_s}{q \tan \phi'} = \frac{280}{(16.5)(\tan 35)} = 24.23$$

$$\begin{aligned} I_{r(ct)} &= \frac{1}{2} \left\{ \exp \left[ \left( 3.3 - 0.45 \frac{B}{L} \right) \cot \left( 45 - \frac{\phi'}{2} \right) \right] \right\} \\ &= \frac{1}{2} \left\{ \exp \left[ \left( 3.3 - 0.45 \frac{1.5}{1.5} \right) \cot \left( 45 - \frac{35}{2} \right) \right] \right\} = 119.3 \end{aligned}$$

# EXAMPLE 9.11

So,  $I_r < I_{r(cr)}$ .

$$\begin{aligned} F_{\gamma c} = F_{qc} &= \exp \left\{ \left[ -4.4 + 0.6 \left( \frac{B}{L} \right) \right] \tan \phi' + \frac{(3.07 \sin \phi') (\log 2I_r)}{1 + \sin \phi'} \right\} \\ &= \exp \left\{ \left[ -4.4 + 0.6 \left( \frac{1.5}{1.5} \right) \right] \tan 35 + \frac{(3.07 \sin 35) (\log 2 \times 24.23)}{1 + \sin 35} \right\} \\ &= 0.461 \end{aligned}$$

Thus,

$$Q_{L_2} = \left[ \begin{aligned} &\left( \frac{1}{2} \right) (16.5)(1.5)(48.03)(0.6)(1)(0.461) \\ &+ (16.5)(33.3)(1.7)(1.7)(0.461) \end{aligned} \right] (1.5 \times 1.5) = 1467.4 \text{ kN}$$

Substituting the values of  $Q$  and  $Q_{L_2}$  in Eq. (9.76),

$$\frac{800}{1467.4} = \frac{\left( \frac{S_e}{B} \right)}{0.69 \left( \frac{S_e}{B} \right) + 1.68}, \quad \frac{S_e}{B} = 1.467\%$$

$$S_e = (1.467) \left( \frac{1.5 \times 1000}{100} \right) \approx 22.0 \text{ mm}$$

# Effect of the Rise of Water Table on Elastic Settlement

Terzaghi (1943) suggested that the submergence of soil mass reduces the soil stiffness by about half, which in turn doubles the settlement. In most cases of foundation design, it is considered that, if the ground water table is located  $1.5B$  to  $2B$  below the bottom of the foundation, it will not have any effect on the settlement.

The total elastic settlement ( $S'_e$ ) due to the rise of the ground water table can be given as:

$$S'_e = S_e C_w$$

where

$S_e$  = elastic settlement before the rise of ground water table

$C_w$  = water correction factor

# Effect of the Rise of Water Table on Elastic Settlement

- Peck, Hansen, and Thornburn (1974):

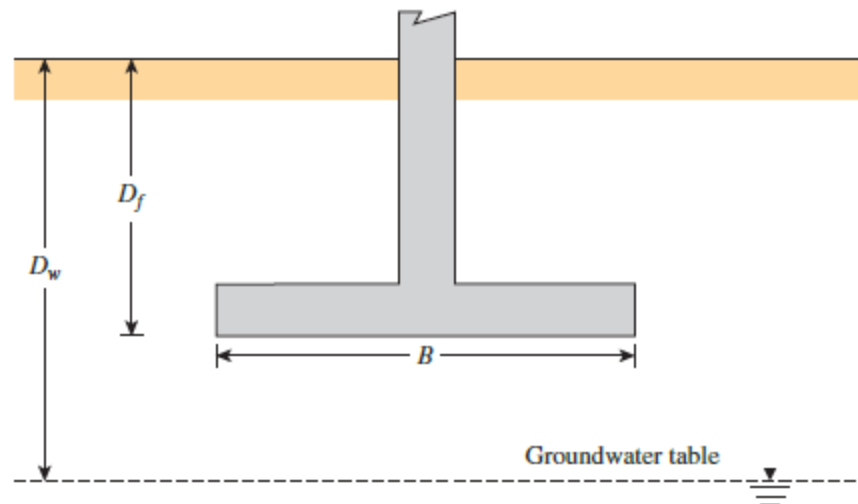
$$C_w = \frac{1}{0.5 + 0.5 \left( \frac{D_w}{D_f + B} \right)} \cong 1$$

- Teng (1982):

$$C_w = \frac{1}{0.5 + 0.5 \left( \frac{D_w - D_f}{B} \right)} \leq 2 \quad \left( \begin{array}{l} \text{for water table below the} \\ \text{base of the foundation} \end{array} \right)$$

- Bowles (1977):

$$C_w = 2 - \left( \frac{D_w}{D_f + B} \right)$$



# Effect of the Rise of Water Table on Elastic Settlement

## Method of Shahriar et al. (2014)

- **When the water table is present in the vicinity of the foundation, the unit weight of the soil has to be reduced for calculation of bearing capacity.**
- **Any future rise in the water table can reduce the ultimate bearing capacity. A future water table rise in the vicinity of the foundation in granular soil can reduce the soil stiffness and, hence, produce additional settlement.**
- **Terzaghi (1943) concluded that when the water table rises from very deep to the foundation level, the settlement will be doubled in granular soil.**

# Effect of the Rise of Water Table on Elastic Settlement

## Method of Shahriar et al. (2014)

Provided that the settlement is doubled when the entire sand layer beneath the foundation is submerged, laboratory model test results and numerical modeling work by Shahriar et al. (2014) show that the additional settlement produced by the rise of water table to any height can be expressed as

$$S_{e, \text{additional}} = \frac{A_w}{A_f} S_e$$

where  $S_e$  is the elastic settlement computed in dry soil,  $A_w$  is the area of the strain influence diagram submerged due to water table rise, and  $A_f$  is the total area of the strain influence diagram under the foundation.

# EXAMPLE 9.12

## EXAMPLE 9.12

Consider the shallow foundation given in Example 9.7. Due to flooding, the groundwater table rose from  $D_w = 4$  m to 2 m. Estimate the total elastic settlement  $S'_e$  after the rise of the water table.

A shallow foundation measuring  $1.75 \text{ m} \times 1.75 \text{ m}$  is to be constructed over a layer of sand. Given  $D_f = 1$  m;  $N_{60}$  is generally increasing with depth;  $\bar{N}_{60}$  in the depth of stress influence = 10,  $q_{\text{net}} = 120 \text{ kN/m}^2$ . The sand is normally consolidated. Estimate the elastic settlement of the foundation.

### SOLUTION

$$S'_e = S_e C_w$$

$$C_w = \frac{1}{0.5 + 0.5 \left( \frac{D_w}{D_f + B} \right)} = \frac{1}{0.5 + 0.5 \left( \frac{2}{1 + 1.75} \right)} = 1.158$$

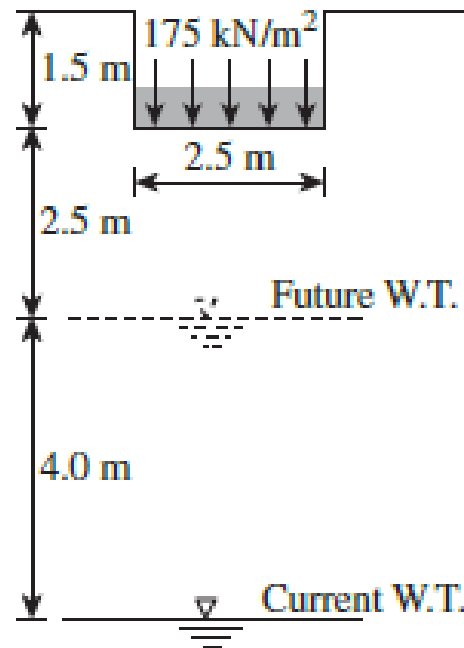
Hence,

$$S'_e = (11.8 \text{ mm})(1.158) = 13.66 \text{ mm}$$

# EXAMPLE 9.13

## EXAMPLE 9.13

A pad foundation  $2.5 \text{ m} \times 2.5 \text{ m}$  in plan, when placed at a depth of  $1.5 \text{ m}$  in sand, applies  $175 \text{ kN/m}^2$  pressure to the underlying ground. Given:  $\gamma = 18.0 \text{ kN/m}^3$ . Currently the water table is at  $6.5 \text{ m}$  below the foundation, and the expected settlement is  $15.0 \text{ mm}$ . In the future, as the worst-case scenario, it is expected that the water table could rise by  $4.0 \text{ m}$ , as shown in Figure . What would be the total settlement of the foundation if this occurs? .



# EXAMPLE 9.13

## SOLUTION

The influence factor diagram needs to be drawn first.

$$I_{z(m)} = 0.5 + 0.1 \sqrt{\frac{\bar{q} - q}{q'_{z(1)}}} = 0.5 + 0.1 \sqrt{\frac{175 - (18.0)(1.5)}{(18.0) \left[ 1.5 + \left( \frac{2.5}{2} \right) \right]}} = 0.67$$

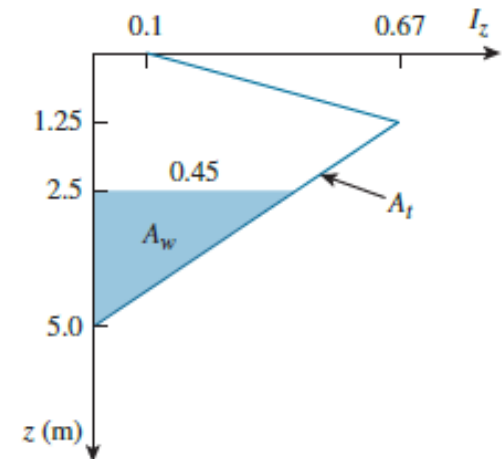
The  $I_z$  versus  $z$  diagram is shown in Figure . Currently, the water table is below the influence zone.  $S_e = 15.0$  mm. The total area of the influence diagram  $A_t$  is given by

$$A_t = \left( \frac{0.10 + 0.67}{2} \right) \times 1.25 + \frac{1}{2} \times 0.67 \times 3.75 = 1.738 \text{ m}$$

$$A_w = \frac{1}{2} \times 2.5 \times 0.45 = 0.563 \text{ m}$$

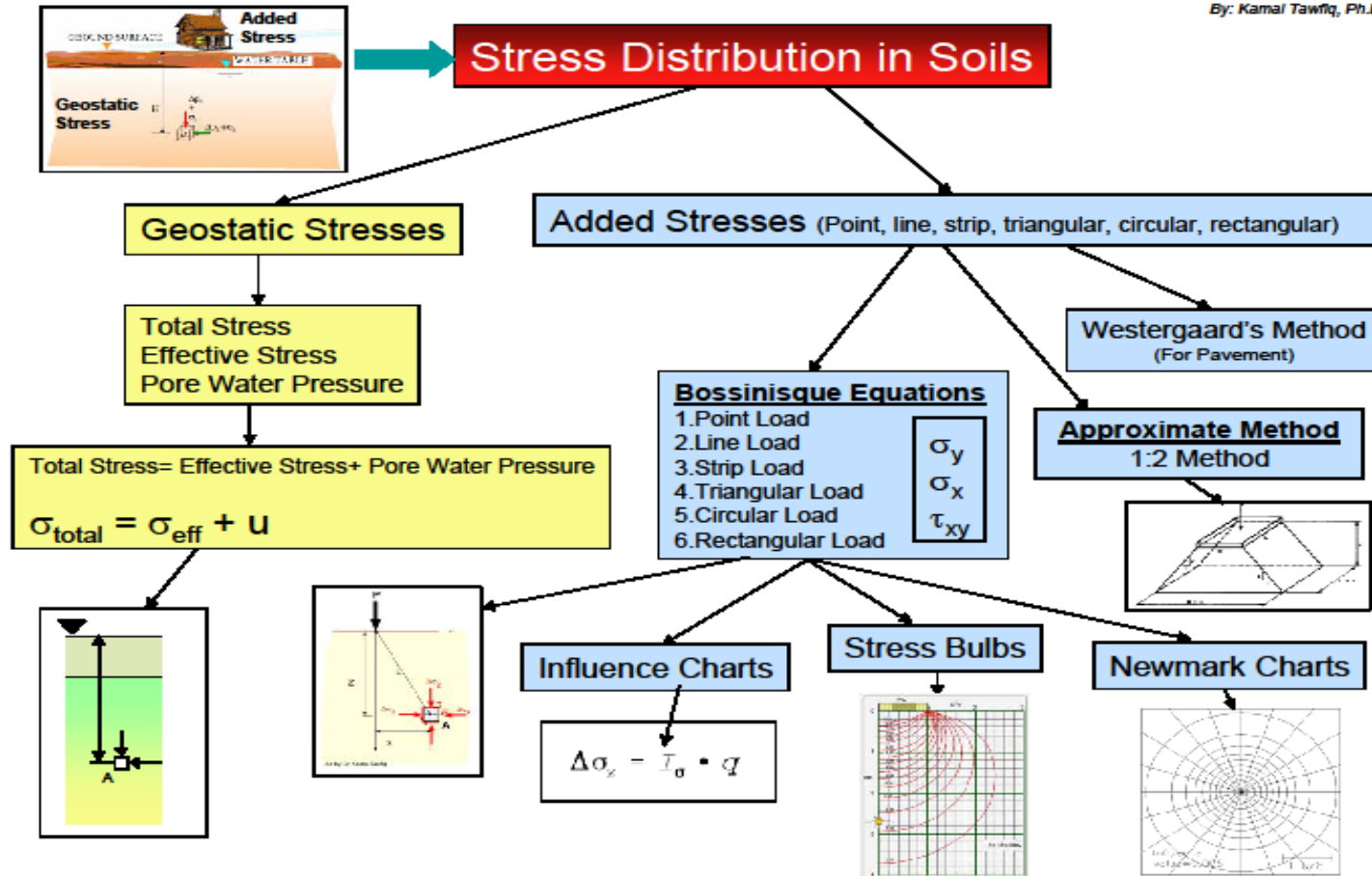
$$S_{e, \text{additional}} = \frac{A_w}{A_t} S_e = \frac{0.563}{1.738} \times 15.0 = 4.9 \text{ mm}$$

The total settlement would be  $15.0 + 4.9 = 19.9$  mm.



# Stresses Distribution in Soils

By: Kamal Tawfiq, Ph.D., P.E



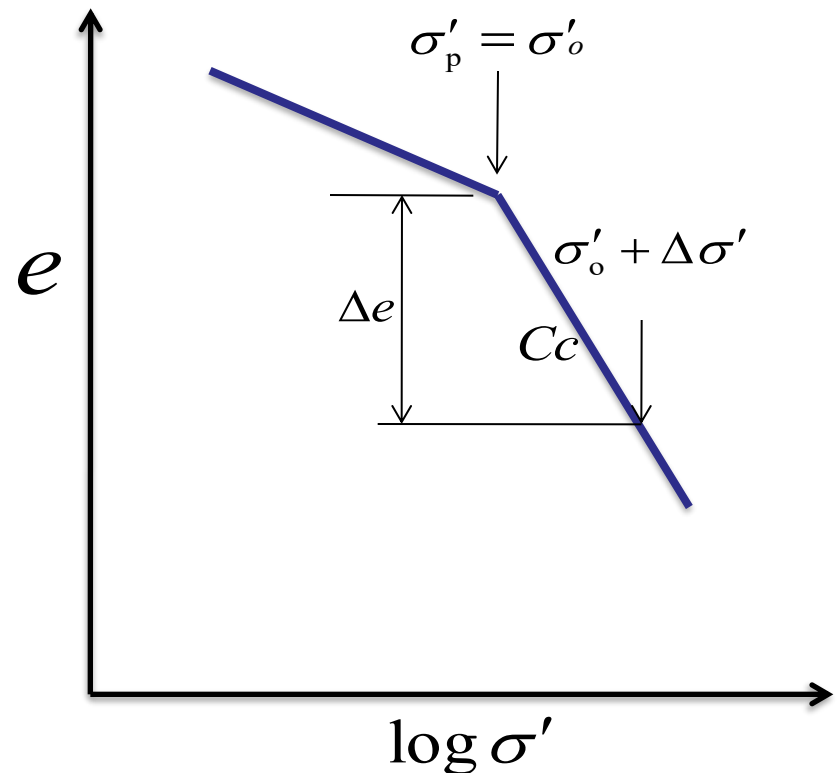
# Calculation of Primary Consolidation Settlement

## a) Normally Consolidated Clay ( $\sigma'_0 = \sigma_c'$ )

$$S_c = \frac{\Delta e}{1 + e_0} H$$

$$\Delta e = C_c \log \left( \frac{\sigma'_0 + \Delta \sigma}{\sigma'_0} \right)$$

$$S_c = \frac{C_c H}{1 + e_0} \log \left( \frac{\sigma'_0 + \Delta \sigma'}{\sigma'_0} \right)$$



# Calculation of Primary Consolidation Settlement

## b) Overconsolidated Clays

$$S_c = \frac{\Delta e}{1 + e_o} H$$

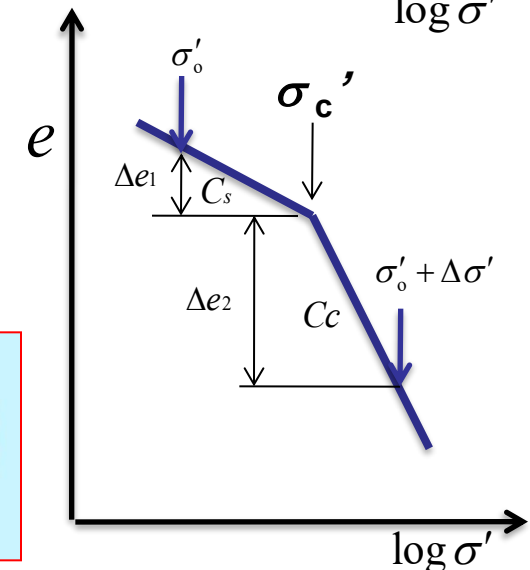
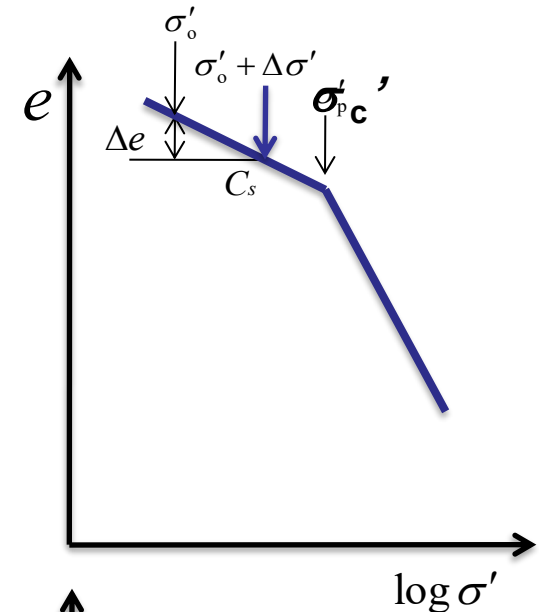
Case I:  $\sigma'_o + \Delta\sigma' \leq \sigma'_{pc}$

$$\Delta e = C_s [\log(\sigma'_o + \Delta\sigma') - \log \sigma'_o]$$

$$S_c = \frac{C_s H}{1 + e_o} \log \left( \frac{\sigma'_o + \Delta\sigma'}{\sigma'_o} \right)$$

Case II:  $\sigma'_o + \Delta\sigma' > \sigma'_{pc}$

$$S_c = \frac{C_s H}{1 + e_o} \log \frac{\sigma'_c}{\sigma'_o} + \frac{C_c H}{1 + e_o} \log \left( \frac{\sigma'_o + \Delta\sigma'}{\sigma'_c} \right)$$



# Calculation of Primary Consolidation Settlement

$$S_{c(p)} = \frac{C_c H_c}{1 + e_o} \log \frac{\sigma'_o + \Delta\sigma'_{av}}{\sigma'_o} \quad (\text{for normally consolidated clays})$$

$$S_{c(p)} = \frac{C_s H_c}{1 + e_o} \log \frac{\sigma'_o + \Delta\sigma'_{av}}{\sigma'_o} \quad \text{for overconsolidated clays with } \sigma'_o + \Delta\sigma'_{av} < \sigma'_c$$

$$S_{c(p)} = \frac{C_s H_c}{1 + e_o} \log \frac{\sigma'_c}{\sigma'_o} + \frac{C_c H_c}{1 + e_o} \log \frac{\sigma'_o + \Delta\sigma'_{av}}{\sigma'_c} \quad \text{for overconsolidated clays with } \sigma'_o < \sigma'_c < \sigma'_o + \Delta\sigma'_{av}$$

where

$\sigma'_o$  = average effective pressure on the clay layer before the construction of the foundation

$\Delta\sigma'_{av}$  = average increase in effective pressure on the clay layer caused by the construction of the foundation

$\sigma'_c$  = preconsolidation pressure

$e_o$  = initial void ratio of the clay layer

$C_c$  = compression index

$C_s$  = swelling index

$H_c$  = thickness of the clay layer

# Summary of calculation procedure

1. Calculate  $\sigma'_o$  at the middle of the clay layer
2. Determine  $\sigma'_c$  from the e-log  $\sigma'$  plot (if not given)
3. Determine whether the clay is N.C. or O.C.
4. Calculate  $\Delta\sigma$
5. Use the appropriate equation

• If N.C. 
$$S_c = \frac{C_c H}{1 + e_o} \log\left(\frac{\sigma'_o + \Delta\sigma'}{\sigma'_o}\right)$$

• If O.C. 
$$S_c = \frac{C_s H}{1 + e_o} \log\left(\frac{\sigma'_o + \Delta\sigma'}{\sigma'_o}\right) \quad \underline{\text{If } \sigma'_o + \Delta\sigma \leq \sigma'_c}$$

$$S_c = \frac{C_s H}{1 + e_o} \log \frac{\sigma'_c}{\sigma'_o} + \frac{C_c H}{1 + e_o} \log\left(\frac{\sigma'_o + \Delta\sigma'}{\sigma'_c}\right) \quad \underline{\text{If } \sigma'_o + \Delta\sigma > \sigma'_c}$$

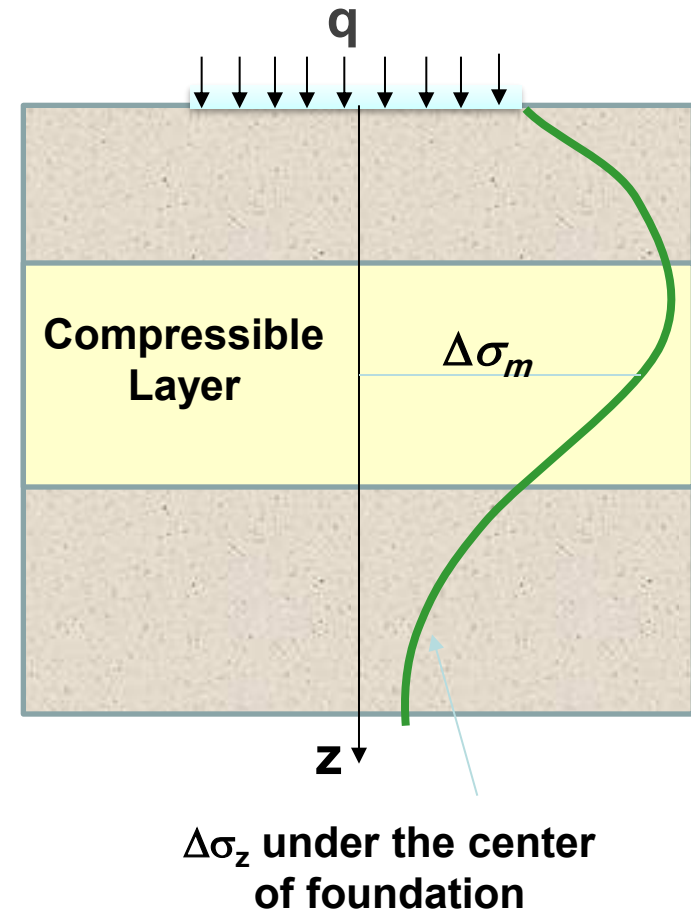
# Nonlinear pressure increase

## Approach 1: Middle of layer (midpoint rule)

- For settlement calculation, the pressure increase  $\Delta\sigma_z$  can be approximated as :

$$\Delta\sigma_z = \Delta\sigma_m$$

where  $\Delta\sigma_m$  represent the increase in the effective pressure in the **middle** of the layer.

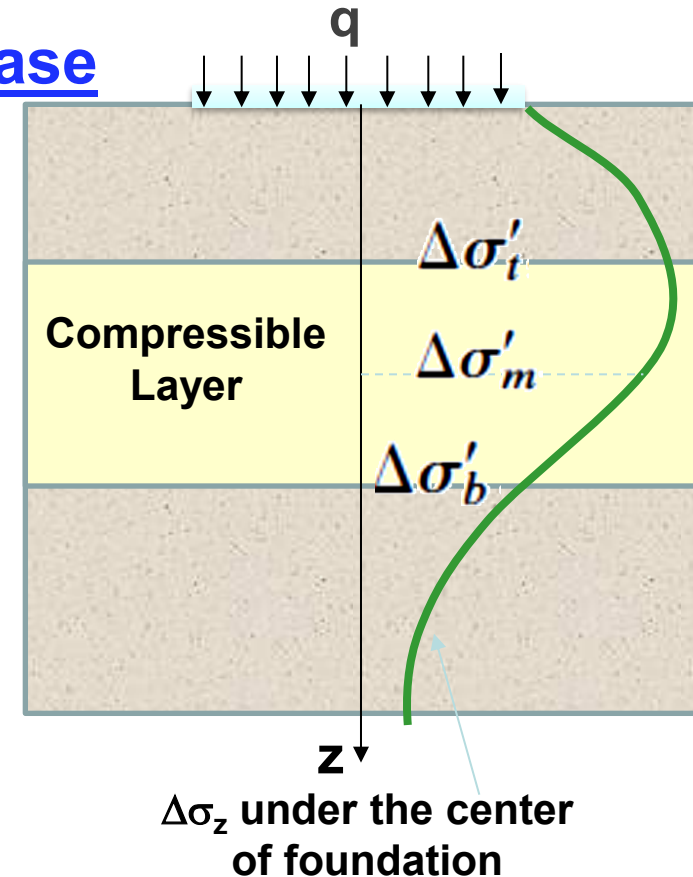


# Nonlinear pressure increase

## Approach 2: Average pressure increase

- For settlement calculation we will use the average pressure increase  $\Delta\sigma_{av}$ , using weighted average method (**Simpson's rule**):

$$\Delta\sigma'_{av} = \frac{\Delta\sigma'_t + 4\Delta\sigma'_m + \Delta\sigma'_b}{6}$$

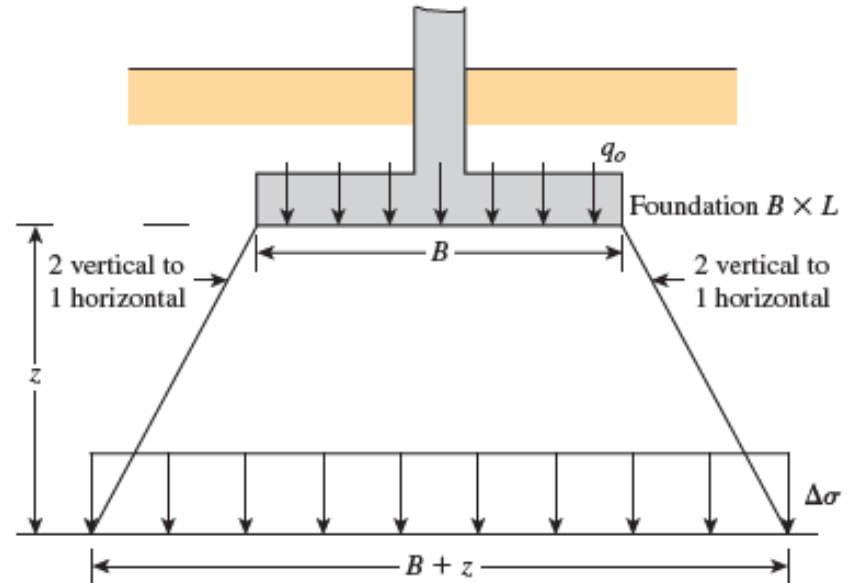


where  $\Delta\sigma_t$ ,  $\Delta\sigma_m$  and  $\Delta\sigma_b$  represent the increase in the pressure at the **top**, **middle**, and **bottom** of the clay, respectively, under the center of the footing.

# Stress from Approximate Method

## 2:1 Method

$$\Delta\sigma = \frac{q_o \times B \times L}{(B + z)(L + z)}$$



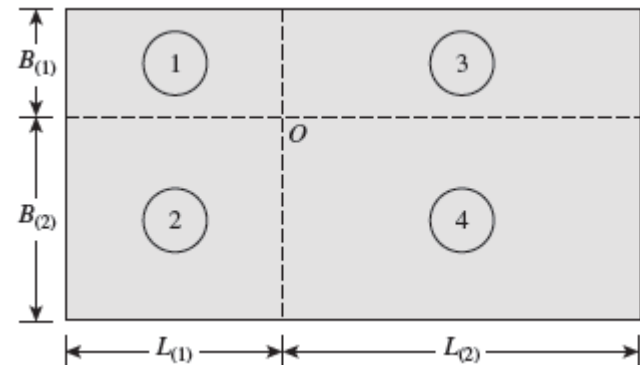
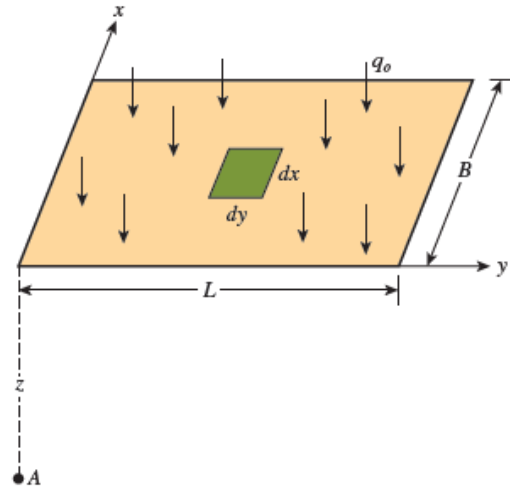
# Stress below a Rectangular Area

$$\Delta\sigma = \int_{y=0}^L \int_{x=0}^B \frac{3q_o (dx dy)z^3}{2\pi(x^2 + y^2 + z^2)^{5/2}} = q_o I$$

$$I = \text{influence factor} = \frac{1}{4\pi} \left( \frac{2mn\sqrt{m^2 + n^2 + 1}}{m^2 + n^2 + m^2n^2 + 1} \cdot \frac{m^2 + n^2 + 2}{m^2 + n^2 + 1} \right. \\ \left. + \tan^{-1} \frac{2mn\sqrt{m^2 + n^2 + 1}}{m^2 + n^2 + 1 - m^2n^2} \right)$$

$$m = \frac{B}{z}$$

$$n = \frac{L}{z}$$



# Stress below a Rectangular Area

**TABLE 8.5** Variation of Influence Value  $I$  [Eq. (8.11)]<sup>a</sup>

$m$	$n$									
	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9	1.0
0.1	0.00470	0.00917	0.01323	0.01678	0.01978	0.02223	0.02420	0.02576	0.02698	0.02794
0.2	0.00917	0.01790	0.02585	0.03280	0.03866	0.04348	0.04735	0.05042	0.05283	0.05471
0.3	0.01323	0.02585	0.03735	0.04742	0.05593	0.06294	0.06858	0.07308	0.07661	0.07938
0.4	0.01678	0.03280	0.04742	0.06024	0.07111	0.08009	0.08734	0.09314	0.09770	0.10129
0.5	0.01978	0.03866	0.05593	0.07111	0.08403	0.09473	0.10340	0.11035	0.11584	0.12018
0.6	0.02223	0.04348	0.06294	0.08009	0.09473	0.10688	0.11679	0.12474	0.13105	0.13605
0.7	0.02420	0.04735	0.06858	0.08734	0.10340	0.11679	0.12772	0.13653	0.14356	0.14914
0.8	0.02576	0.05042	0.07308	0.09314	0.11035	0.12474	0.13653	0.14607	0.15371	0.15978
0.9	0.02698	0.05283	0.07661	0.09770	0.11584	0.13105	0.14356	0.15371	0.16185	0.16835
1.0	0.02794	0.05471	0.07938	0.10129	0.12018	0.13605	0.14914	0.15978	0.16835	0.17522
1.2	0.02926	0.05733	0.08323	0.10631	0.12626	0.14309	0.15703	0.16843	0.17766	0.18508
1.4	0.03007	0.05894	0.08561	0.10941	0.13003	0.14749	0.16199	0.17389	0.18357	0.19139
1.6	0.03058	0.05994	0.08709	0.11135	0.13241	0.15028	0.16515	0.17739	0.18737	0.19546
1.8	0.03090	0.06058	0.08804	0.11260	0.13395	0.15207	0.16720	0.17967	0.18986	0.19814
2.0	0.03111	0.06100	0.08867	0.11342	0.13496	0.15326	0.16856	0.18119	0.19152	0.19994
2.5	0.03138	0.06155	0.08948	0.11450	0.13628	0.15483	0.17036	0.18321	0.19375	0.20236
3.0	0.03150	0.06178	0.08982	0.11495	0.13684	0.15550	0.17113	0.18407	0.19470	0.20341
4.0	0.03158	0.06194	0.09007	0.11527	0.13724	0.15598	0.17168	0.18469	0.19540	0.20417
5.0	0.03160	0.06199	0.09014	0.11537	0.13737	0.15612	0.17185	0.18488	0.19561	0.20440
6.0	0.03161	0.06201	0.09017	0.11541	0.13741	0.15617	0.17191	0.18496	0.19569	0.20449
8.0	0.03162	0.06202	0.09018	0.11543	0.13744	0.15621	0.17195	0.18500	0.19574	0.20455
10.0	0.03162	0.06202	0.09019	0.11544	0.13745	0.15622	0.17196	0.18502	0.19576	0.20457
$\infty$	0.03162	0.06202	0.09019	0.11544	0.13745	0.15623	0.17197	0.18502	0.19577	0.20458

# Three-Dimensional Effect on Primary Consolidation Settlement

## Skempton–Bjerrum Modification (1957) for a consolidation settlement calculation

$$S_{c(p)-\text{oed}} = \int \frac{\Delta e}{1 + e_o} dz = \int m_v \Delta \sigma'_{(1)} dz$$

$S_{c(p)-\text{oed}}$  = one-dimensional consolidation settlement calculated by using oedometer data

$\Delta \sigma'_{(1)}$  = effective vertical stress increase

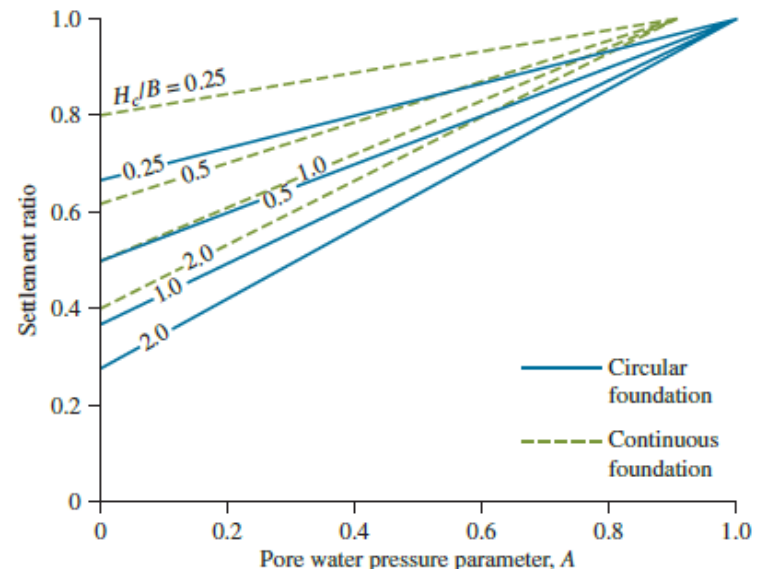
$m_v$  = volume coefficient of compressibility

$$\Delta u = \Delta \sigma_{(3)} + A[\Delta \sigma_{(1)} - \Delta \sigma_{(3)}]$$

where  $A$  = pore water pressure parameter

$$K_{\text{cir}} = \frac{S_{c(p)}}{S_{c(p)-\text{oed}}}$$

where  $K_{\text{cir}}$  = settlement ratio for circular foundations.



# Three-Dimensional Effect on Primary Consolidation Settlement

Leonards (1976) examined the correction factor  $K_{cr}$  for a three-dimensional consolidation effect in the field for a circular foundation located over *overconsolidated clay*.

$$S_{c(p)} = K_{cr(OCR)} S_{c(p)-oed}$$

$$K_{cr(OCR)} = f\left(OCR, \frac{B}{H_c}\right)$$

$$OCR = \text{overconsolidation ratio} = \frac{\sigma'_c}{\sigma'_o}$$

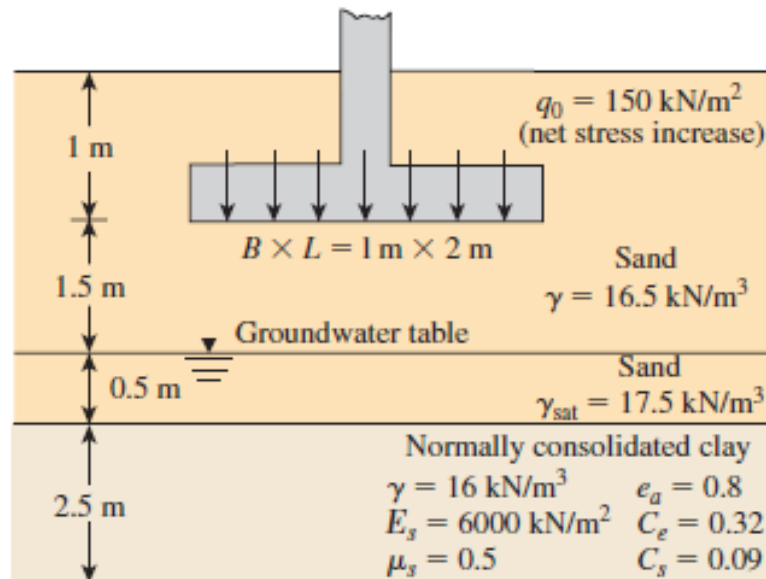
TABLE 9.9 Variation of  $K_{cr(OCR)}$  with OCR and  $B/H_c$

OCR	$K_{cr(OCR)}$		
	$B/H_c = 4.0$	$B/H_c = 1.0$	$B/H_c = 0.2$
1	1	1	1
2	0.986	0.957	0.929
3	0.972	0.914	0.842
4	0.964	0.871	0.771
5	0.950	0.829	0.707
6	0.943	0.800	0.643
7	0.929	0.757	0.586
8	0.914	0.729	0.529
9	0.900	0.700	0.493
10	0.886	0.671	0.457
11	0.871	0.643	0.429
12	0.864	0.629	0.414
13	0.857	0.614	0.400
14	0.850	0.607	0.386
15	0.843	0.600	0.371
16	0.843	0.600	0.357

# EXAMPLE 9.14

## EXAMPLE 9.14

A plan of a foundation  $1\text{ m} \times 2\text{ m}$  is shown in Figure      Estimate the consolidation settlement of the foundation, taking into account the three-dimensional effect.  
Given:  $A = 0.6$ .



# EXAMPLE 9.14

The clay is normally consolidated. Thus,

$$S_{c(p)-\text{oad}} = \frac{C_c H_c}{1 + e_o} \log \frac{\sigma'_o + \Delta\sigma'_{\text{av}}}{\sigma'_o}$$

so

$$\begin{aligned} \sigma'_o &= (2.5)(16.5) + (0.5)(17.5 - 9.81) + (1.25)(16 - 9.81) \\ &= 41.25 + 3.85 + 7.74 = 52.84 \text{ kN/m}^2 \end{aligned}$$

$$\Delta\sigma'_{\text{av}} = \frac{1}{6}(\Delta\sigma'_t + 4\Delta\sigma'_m + \Delta\sigma'_b)$$

We divide the foundation into four quarters, compute the stress increase under a corner of each quarter and multiply by four. For each quarter,  $B = 0.5$  m and  $L = 1.0$  m.

Location	$z$ (m)	$m = B/z$	$n = L/z$	$I$	$\Delta\sigma' = 4q_o I$
Top	2.0	0.25	0.50	0.0475	28.5 = $\Delta\sigma'_t$
Middle	3.25	0.154	0.308	$\approx 0.0213$	12.75 = $\Delta\sigma'_m$
Bottom	4.5	0.111	0.222	$\approx 0.0113$	6.75 = $\Delta\sigma'_b$

Now,

$$\Delta\sigma'_{\text{av}} = \frac{1}{6}(28.5 + 4 \times 12.75 + 6.75) = 14.38 \text{ kN/m}^2$$

so

$$\begin{aligned} S_{c(p)-\text{oad}} &= \frac{(0.32)(2.5)}{1 + 0.8} \log \left( \frac{52.84 + 14.38}{52.84} \right) = 0.0465 \text{ m} \\ &= 46.5 \text{ mm} \end{aligned}$$

# EXAMPLE 9.14

Now assuming that the 2:1 method of stress increase holds, the area of distribution of stress at the top of the clay layer will have dimensions

$$B' = \text{width} = B + z = 1 + (1.5 + 0.5) = 3 \text{ m}$$

and

$$L' = \text{width} = L + z = 2 + (1.5 + 0.5) = 4 \text{ m}$$

The diameter of an equivalent circular area,  $B_{\text{eq}}$ , can be given as

$$\frac{\pi}{4} B_{\text{eq}}^2 = B' L'$$

so that

$$B_{\text{eq}} = \sqrt{\frac{4B'L'}{\pi}} = \sqrt{\frac{(4)(3)(4)}{\pi}} = 3.91 \text{ m}$$

Also,

$$\frac{H_c}{B_{\text{eq}}} = \frac{2.5}{3.91} = 0.64$$

From Figure 9.32, for  $A = 0.6$  and  $H_c/B_{\text{eq}} = 0.64$ , the magnitude of  $K_{\text{cr}} \approx 0.78$ . Hence,

$$S_{e(p)} = K_{\text{cir}} S_{e(p) - \text{oed}} = (0.78)(46.5) \approx 36.3 \text{ mm}$$

# Secondary Consolidation Settlement

- The magnitude of the secondary consolidation can be calculated as:

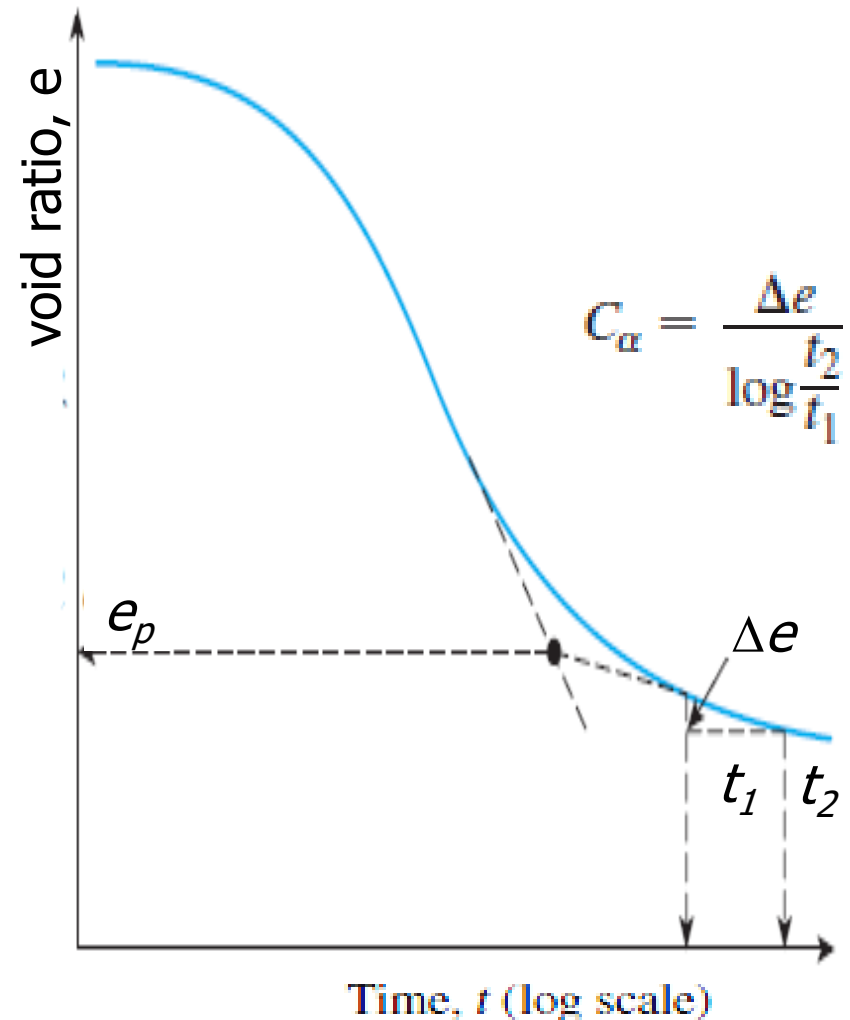
$$S_s = \frac{H}{1 + e_p} \Delta e$$

$e_p$  void ratio at the end of primary consolidation,  
 $H$  thickness of clay layer.

$$\Delta e = C_\alpha \log (t_2/t_1)$$

$C_\alpha$  = coefficient of secondary compression

$$S_s = \frac{C_\alpha H}{1 + e_p} \log \left( \frac{t_2}{t_1} \right)$$



# Secondary Consolidation Settlement

$$C_{\alpha} = \frac{\Delta e}{\log t_2 - \log t_1} = \frac{\Delta e}{\log(t_2/t_1)}$$

where

$C_{\alpha}$  = secondary compression index

$\Delta e$  = change of void ratio

$t_1, t_2$  = time

The magnitude of the secondary consolidation can be calculated as

$$S_{c(s)} = C'_{\alpha} H_c \log(t_2/t_1)$$

where

$$C'_{\alpha} = C_{\alpha} / (1 + e_p)$$

$e_p$  = void ratio at the end of primary consolidation

$H_c$  = thickness of clay layer

Mesri (1973) correlated  $C'_{\alpha}$  with the natural moisture content ( $w$ ) of several soil, from which it appears that

$$C'_{\alpha} \approx 0.0001w$$

where  $w$  = natural moisture content, in percent. For most overconsolidated soil,  $C'_{\alpha}$  varies between 0.0005 to 0.001.

# Secondary Consolidation Settlement

Mesri and Godlewski (1977) compiled the magnitude of  $C_\alpha/C_c$  ( $C_c$  = compression index) for a number of soil. Based on their compilation, it can be summarized that

- For inorganic clays and silts:

$$C_\alpha/C_c \approx 0.04 \pm 0.01$$

- For organic clays and silts:

$$C_\alpha/C_c \approx 0.05 \pm 0.01$$

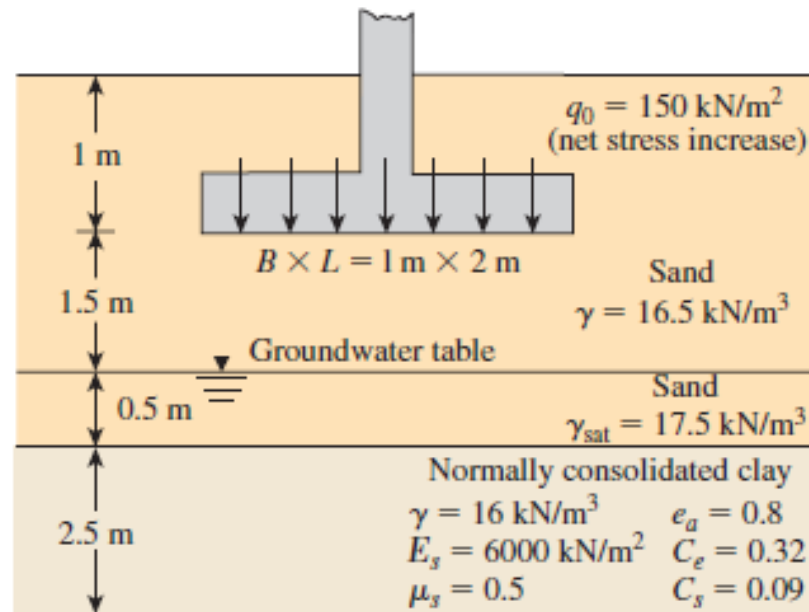
- For peats:

$$C_\alpha/C_c \approx 0.075 \pm 0.01$$

# EXAMPLE 9.15

## EXAMPLE 9.15

Refer to Example 9.14. Given for the clay layer:  $C_\alpha = 0.02$ . Estimate the total consolidation settlement five years after the completion of the primary consolidation settlement. (*Note:* Time for completion of primary consolidation settlement is 1.3 years.)



# EXAMPLE 9.15

SOLUTION

$$C_c = \frac{e_1 - e_2}{\log\left(\frac{\sigma'_2}{\sigma'_1}\right)}$$

For this problem,  $e_1 - e_2 = \Delta e$ . Referring to Example 9.14, we have

$$\begin{aligned}\sigma'_2 &= \sigma'_o + \Delta\sigma' = 52.84 + 14.38 = 67.22 \text{ kN/m}^2 \\ \sigma'_1 &= \sigma'_o = 52.84 \text{ kN/m}^2 \\ C_c &= 0.32\end{aligned}$$

Hence,

$$\Delta e = C_c \log\left(\frac{\sigma'_o + \Delta\sigma}{\sigma'_o}\right) = 0.32 \log\left(\frac{67.22}{52.84}\right) = 0.0335$$

Given:  $e_o = 0.8$ . Hence,

$$e_p = e_o - e = 0.8 - 0.0335 = 0.7665$$

$$C'_\alpha = \frac{C_\alpha}{1 + e_p} = \frac{0.02}{1 + 0.7665} = 0.0113$$

# EXAMPLE 9.15

$$S_{c(s)} = C'_a H_c \log \left( \frac{t_2}{t_1} \right)$$

Note:  $t_1 = 1.3$  years;  $t_2 = 1.3 + 5 = 6.3$  years.

Thus,

$$S_{c(s)} = (0.0113)(2.5 \text{ m}) \log \left( \frac{6.3}{1.3} \right) = 0.0194 \text{ m} = 19.4 \text{ mm}$$

Total consolidation settlement is

$$\underline{36.3 \text{ mm}} + 19.4 = 55.7 \text{ mm}$$



Example 9.14

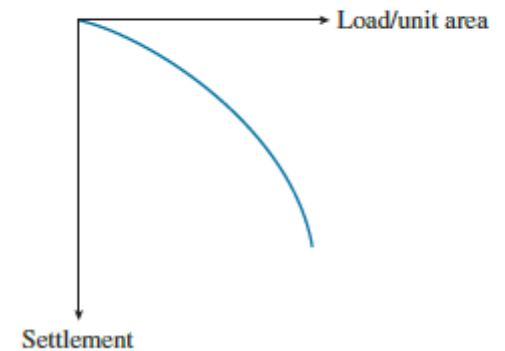
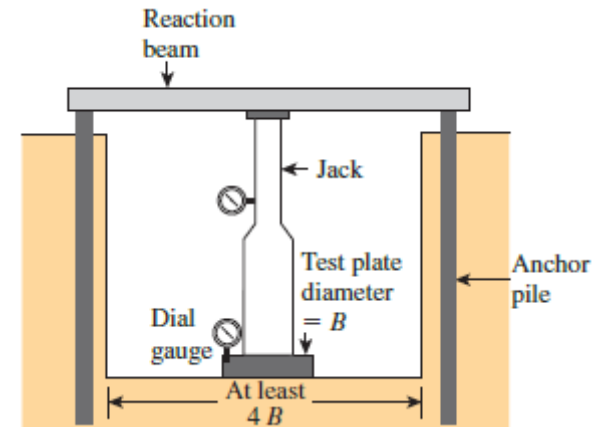
(primary  
consolidation  
settlement)

# Field Load Test

## The Plate Load Test (PLT)



Plate load test in the field



# Field Load Test

For tests in clay,

$$q_{u(F)} = q_{u(P)}$$

where

$q_{u(F)}$  = ultimate bearing capacity of the proposed foundation

$q_{u(P)}$  = ultimate bearing capacity of the test plate

the ultimate bearing capacity in clay is virtually independent of the size of the plate.

For tests in sandy soil,

$$q_{u(F)} = q_{u(P)} \frac{B_F}{B_P}$$

where

$B_F$  = width of the foundation

$B_P$  = width of the test plate

# Field Load Test

The allowable bearing capacity of a foundation, based on settlement considerations and for a given intensity of load,  $q_o$ , is

$$S_F = S_P \frac{B_F}{B_P} \quad \text{(for clayey soil)}$$

and

$$S_F = S_P \left( \frac{2B_F}{B_F + B_P} \right)^2 \quad \text{(for sandy soil)}$$



**THE END**