
King Saud University

## Exercises

## STAT 328 (Statistical Packages)


nashmiah r.alshammari

328 stat

Excel
and
Minitab

## MATHEMATICAL FUNCTIONS

Write the commands of the following:

|  | $\begin{array}{c}\text { By Excel } \\ \text { (using }(f x))\end{array}$ | $\begin{array}{c}\text { By Minitab } \\ \text { calc } \rightarrow \text { calculator }\end{array}$ |  |
| :--- | :--- | :--- | :--- |
| Absolute value | $\|-4\|=4$ | ABS(-4) |  |
| Combinations | $\binom{10}{6}=10 \mathrm{C}=210$ | COMBIN(10;6) |  |
| $\begin{array}{l}\text { The exponential } \\ \text { function }\end{array}$ | $e^{-1.6=0.201897}$ | EXP(-1.6) |  |
| Factorial | $110!=1.5882 \mathrm{E}+178$ | FACT(110) |  |
| Floor function | $[-3.15]=-4$ | INT(-3.15) |  |
| Natural logarithm | $\ln (23)=3.135494216$ | LN(23) |  |
| $\begin{array}{l}\text { Logarithm with } \\ \text { respect to any } \\ \text { base }\end{array}$ | $\log 9(4)=0.630929754$ | LOG(4;9) |  |
| $\begin{array}{l}\text { Logarithm with } \\ \text { respect to base } 10\end{array}$ | $\begin{array}{l}\log (12)= \\ 1.079181246\end{array}$ | LOG10(12) |  |
| $\begin{array}{l}\text { Multinomial } \\ \text { Coefficient }\end{array}$ | $\left(\begin{array}{c}9 \\ 2\end{array} \quad 5\right)=756$ | MULTINOMIAL(2;2;5) |  |$]$

## MATRICES

Write the commands of the following:

|  |  | By Excel <br> (using $(f \times x)$ ) | By Minitab <br> 1) data $\rightarrow$ copy $\rightarrow$ columns in matrix <br> display data |
| :---: | :---: | :---: | :---: |
| Addition of Matrices | $\begin{aligned} & A=\left[\begin{array}{cc} -5 & 0 \\ 4 & 1 \end{array}\right], B=\left[\begin{array}{cc} 6 & -3 \\ 2 & 3 \end{array}\right] \\ & \Rightarrow A+B=\left[\begin{array}{cc} -5+6 & 0+-3 \\ 4+2 & 1+3 \end{array}\right]=\left[\begin{array}{ll} 1 & -3 \\ 6 & 4 \end{array}\right] \end{aligned}$ |  |  |
| Subtract of Matrices | $\begin{aligned} & C=\left[\begin{array}{cc} 1 & 2 \\ -2 & 0 \\ -3 & -1 \end{array}\right], D=\left[\begin{array}{cc} 1 & -1 \\ 1 & 3 \\ 2 & 3 \end{array}\right] \\ & \Rightarrow C-D=\left[\begin{array}{ll} 1-1 & 2-(-1) \\ -3-1 & 0-3 \\ -3-2 & -1-3 \end{array}\right]=\left[\begin{array}{cc} 0 & 3 \\ -3 & -3 \\ -5 & -4 \end{array}\right] \end{aligned}$ |  |  |
| Additive Inverse of Matrix | $\begin{aligned} & A=\left[\begin{array}{ccc} 1 & 0 & 2 \\ 3 & -1 & 5 \end{array}\right] \\ & \Rightarrow-A=\left[\begin{array}{lll} -1 & 0 & -2 \\ -3 & 1 & -5 \end{array}\right] \end{aligned}$ |  |  |
| Scalar <br> Multiplication <br> of Matrices | $\begin{aligned} D & =\left[\begin{array}{cc} -3 & 0 \\ 4 & 5 \end{array}\right] \\ \Rightarrow 3 D & =\left[\begin{array}{ll} -9 & 0 \\ 12 & 15 \end{array}\right] \end{aligned}$ |  |  |
| Matrix <br> Multiplication | $\begin{aligned} & E=\left[\begin{array}{lll} 1 & 4 & 7 \\ 2 & 5 & 8 \\ 3 & 6 & 9 \end{array}\right], F=\left[\begin{array}{ll} 1 & 4 \\ 2 & 5 \\ 3 & 6 \end{array}\right] \\ & \Rightarrow E \times F=\left[\begin{array}{ll} 30 & 66 \\ 36 & 81 \\ 42 & 96 \end{array}\right] \end{aligned}$ |  |  |
| Determinant and Inverse Matrices | $\begin{gathered} G=\left[\begin{array}{cc} 3 & -1 \\ -5 & 2 \end{array}\right] \\ \Rightarrow \operatorname{det}(G)=1 \text { and } G^{-1}=\left[\begin{array}{ll} 2 & 1 \\ 5 & 3 \end{array}\right] \end{gathered}$ |  |  |

## CONDITIONAL FUNCTION (IF) AND COUNT CONDITIONAL FUNCTION

## By Excel

## (using (fx))

We have grades of 10 students

| 73 | 45 | 32 | 85 | 98 | 78 | 82 | 87 | 60 | 25 | 64 | 72 | 12 | 90 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

1. Print student case being successful (Mark $>=60$ ) and being a failure (Mark $<60$ ).
2. How many successful students?
3. How many students whose grades are less than or equal to 80 ?

## DESCRIPTIVE STATISTICS

We have students' weights as follows: $44,40,42,48,46,44$. Find:

|  | By Excel <br> (using ( $f x$ ) and (Data Analysis)) | $\qquad$ |
| :---: | :---: | :---: |
| Mean=44 | AVERAGE(C2:C7) |  |
| Median=44 | MEDIAN(C2:C7) |  |
| Mode=44 | MODE.SNGL(C2:C7) |  |
| Sample standard deviation=2.828 | STDEV.S(C2:C7) |  |
| Sample variance $=8$ | VAR.S(C2:C7) |  |
| Kurtosis=-0.3 | KURT(C2:C7) |  |
| Skewness=4.996E-17 | SKEW(C2:C7) |  |
| Minimum=40 | $\operatorname{MIN}(\mathrm{C} 2: \mathrm{C} 7)$ |  |
| Maximum=48 | MAX (C2:C7) |  |
| Range $=8$ | $\operatorname{MAX}(\mathrm{C} 2: \mathrm{C} 7)-\mathrm{MIN}(\mathrm{C} 2: \mathrm{C} 7)$ |  |
| Count=6 | COUNT(C2:C7) |  |
| Coefficient of variation $=6.428 \%$ | STDEV.S(C2:C7)/AVERAGE(C2:C7)*100 |  |

* Range $=$ Maximum-Minimum
$\star \star$ Coefficient of variation $=\frac{\text { Sample standard deviation }}{\text { Mean }} \times 100 \%$


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## PEARSON CORRELATION COEFFICIENT

We have the table illustrates the age X and blood pressure Y for eight female.

| 68 | 49 | 60 | 42 | 55 | 63 | 36 | 42 | X |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 152 | 145 | 155 | 140 | 150 | 140 | 118 | 125 | Y |

Find:

|  | By Excel <br> (using $(f x)$ and (Data Analysis)) | By Minitab <br> stat $\rightarrow$ basic statistics $\rightarrow$ correlation <br> + <br> $\checkmark$ Display $p$-value |
| :--- | :---: | :---: |
| Correlation $=0.791832$ | CORREL(M3:M10;N3:N10) |  |

## PROBABILITY DISTRIBUTION FUNCTIONS

## Discrete Distributions

## Notes

If X is discrete random variable, then

1) $P(a<X \leq b)=P(X \leq b)-P(X \leq a)$
and so, if
$P(a \leq X<b)=P((a-1)<X \leq(b-1))=P(X \leq(b-1))-P(X \leq(a-1))$ or
$P(a \leq X \leq b)=P((a-1)<X \leq b)=P(X \leq b)-P(X \leq(a-1))$ or
$P(a<X<b)=P(a<X \leq(b-1))=P(X \leq(b-1))-P(X \leq a)$.
2) $P(X>a)=1-P(X \leq a)$, $P(X \geq a)=1-P(X<a)=1-P(X \leq(a-1))$, $P(X<a)=P(X \leq(a-1))$

## 1. Binomial Distribution

A biased coin is tossed 6 times. The probability of heads on any toss is 0.3 . Let $X$ denote the number of heads that come up.
Calculate:
(i) If we call heads a success then this $X$ has a binomial distribution with parameters $n=6$ and $p=0.3$.

$$
P(X=2)=\binom{6}{2}(0.3)^{2}(0.7)^{4}=0.324135
$$

(ii)

$$
P(X=3)=\binom{6}{3}(0.3)^{3}(0.7)^{3}=0.18522
$$

(iii) We need $P(1<X \leq 5)$

$$
\begin{aligned}
& P(X=2)+P(X=3)+P(X=4)+P(X=5) \\
= & 0.324+0.185+0.059+0.01 \\
= & 0.578
\end{aligned}
$$

|  | By Excel <br> (using (fx)) | By Minitab <br> calc $\rightarrow$ probability distribution |
| :---: | :---: | :---: |
| 1 |  |  |
| ii |  |  |
| iii |  |  |

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## 2. Poisson Distribution

Births in a hospital occur randomly at an average rate of 1.8 births per hour.
What is the probability of observing 4 births in a given hour at the hospital?
Let $X=$ No. of births in a given hour
(i) Events occur randomly $\Rightarrow X \sim \operatorname{Po}(1.8)$
(ii) Mean rate $\lambda=1.8$

We can now use the formula to calculate the probability of observing exactly 4 births in a given hour
$P(X=4)=\mathrm{e}^{-1.8 \frac{1.8^{4}}{4!}}=0.0723$

What about the probability of observing more than or equal to 2 births in a given hour at the hospital?

We want $P(X \geq 2)=P(X=2)+P(X=3)+\ldots$
i.e. an infinite number of probabilities to calculate
but

$$
\begin{aligned}
P(X \geq 2) & =P(X=2)+P(X=3)+\ldots \\
& =1-P(X<2) \\
& =1-(P(X=0)+P(X=1)) \\
& =1-\left(\mathrm{e}^{-1.8} \frac{1.8^{0}}{0!}+\mathrm{e}^{-1.8} \frac{1.8^{1}}{1!}\right) \\
& =1-(0.16529+0.29753) \\
& =0.537
\end{aligned}
$$



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## Continuous Distributions

## Notes

If X is continuous symmetric random variable (as Normal distribution and Student's t distribution), then

1) $P(X \geq x)=1-P(X \leq x)$ and $P(X \leq x)=1-P(X \geq x)$
2) $P(X \leq x)=1-P(X \leq-x)$ and $P(X \geq x)=1-P(X \geq-x)$

## 1. Exponential Distribution

On the average, a certain computer part lasts 10 years. The length of time the computer part lasts is exponentially distributed.

What is the probability that a computer part lasts more than 7 years?

## Solution

Let $X=$ the amount of time (in years) a computer part lasts.

$$
\mu=10 \text { so } m=\frac{1}{\mu}=\frac{1}{10}=0.1
$$

$P(X>7)=1-P(X<7)$.
$P(X>7)=e^{-0.1 \cdot 7}=0.4966$. The probability that a computer part lasts more than 7 years is 0.4966 .


## 328 stat

2. Normal Distribution

|  | By Excel (using $(f x)$ ) | By Minitab <br> calc $\rightarrow$ probability distribution |
| :---: | :---: | :---: |
| $\begin{gathered} P(X \leq 25) \\ =P(X<25) \\ \text { at } \\ \mu=20 \\ \quad \text { and } \\ \sigma=3 \end{gathered}$ |  |  |
| $\begin{gathered} f_{X}(25) \\ a t \\ \mu=20 \\ \text { and } \\ \sigma=3 \end{gathered}$ |  |  |
| $\begin{aligned} & P\left(X \leq x_{0}\right) \\ & =P\left(X<x_{0}\right) \\ & =.55 \\ & \quad \text { at } \\ & \quad \mu=20 \\ & \quad \text { and } \\ & \sigma=3 \end{aligned}$ |  |  |
| $\begin{gathered} P(Z \leq 1.78) \\ =P(Z<1.78) \\ a t \\ \mu=0 \\ a n d \\ \sigma=1 \end{gathered}$ |  |  |
| $\begin{gathered} P\left(Z \leq Z_{0}\right) \\ =.55 \\ a t \\ \mu=0 \\ a n d \\ \sigma=1 \end{gathered}$ |  |  |

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3．Student＇s t Distribution


Find：
（a）$t_{0.025}$ when $v=14$
（b）$t_{0.01}$ when $v=10$
（c）$t_{0.995}$ when $v=7$

|  | By Excel $(\operatorname{using}(f x))$ | By Minitab <br> calc $\rightarrow$ probability distribution |
| :---: | :---: | :---: |
| $\begin{aligned} & (a) \\ & P\left(T_{14} \leq t\right) \\ & =0.025 \end{aligned}$ | $=T . I N V(.025 ; 14)$ $\square$ $\cdot \cdot r_{0}=\text { 屋霊 } .025$ $1 \varepsilon=$ $\square$ Deg＿freedom <br> عدد صعيح موجب يشير إلى عدد درجات الحربة التى تميز التوزيع．Deg＿freedom |  |
| $\begin{aligned} & (b) \\ & P\left(T_{10}<t\right) \\ & =0.01 \end{aligned}$ | 5，VTTV19ミ0月－＝ <br> عدد صحيح موجب يشير إلى عدد درجات الحرية التى تميز التوزيع．Deg＿freedom |  |
| $\begin{aligned} & \text { (c) } \\ & P\left(T_{7}<t\right) \\ & =0.995 \end{aligned}$ | ```-.,90 = P最 0.995 Probability v = 稂 标None``` <br> إرجاع عكس توزي8 t للطالب ذي الطرف الأيسر． <br> عدد صحبح موحب يشـير اللى عدد در＞ات الاحربة التق تميز التوزي8．Deg＿freedom |  |

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Given a random sample of size $\mathbf{2 4}$ from a normal distribution, find $\mathbf{k}$ such that:
(a) $P(-1.7139<T<k)=0.90$
(b) $P(k<T<2.807)=0.95$
(c) $P(-k<T<k)=0.90$
(a)
$P\left(-1.7139<T_{23}<k\right)=0.9$
$\leftrightarrow P\left(T_{23}<k\right)-P\left(T_{23}<-1.7139\right)=0.9$
$\leftrightarrow P\left(T_{23}<k\right)=0.9+P\left(T_{23}<-1.7139\right)$
$\leftrightarrow P\left(T_{23}<k\right)=0.949997$

| By Excel <br> (using (fx)) | By Minitab <br> calc $\rightarrow$ probability distribution |
| :---: | :---: |
|   <br> OIn excel you might make it in one step too $\begin{aligned} & P\left(T_{23}<k\right)=0.9+P\left(T_{23}<-1.7139\right) \\ & \text { so, } \quad=\operatorname{T.INV}(0.9+\operatorname{T.DIST}(-1.7139,23,1), 23)=1.713839369 \end{aligned}$ |  |

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(b)
$P\left(k<T_{23}<2.807\right)=0.95$
$\leftrightarrow P\left(T_{23}<2.807\right)-P\left(T_{23}<k\right)=0.95$
$\leftrightarrow P\left(T_{23}<k\right)=\left(T_{23}<2.807\right)-0.95$
$\leftrightarrow P\left(T_{23}<k\right)=0.044996$


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(c)

$$
\begin{aligned}
& \text { (i) } P\left(T_{23}<k\right)-P\left(T_{23}<-k\right)=.9 \\
& \leftrightarrow P\left(T_{23}<k\right)-\left\{1-P\left(T_{23}<k\right)\right\}=0.9 \\
& \leftrightarrow 2 P\left(T_{23}<k\right)-1=0.9 \\
& \leftrightarrow 2 P\left(T_{23}<k\right)=1.9 \\
& \leftrightarrow P\left(T_{23}<k\right)=0.95 \\
& \text { so } \quad=T . \operatorname{inv}(0.95,23)=1.71387 \\
& \text { (ii) } P\left(T_{23}<k\right)-P\left(T_{23}<-k\right)=.9 \\
& \leftrightarrow 1-P\left(T_{23}>k\right)-P\left(T_{23}<-k\right)=0.9 \\
& \leftrightarrow 1-P\left(T_{23}>k\right)-\left\{1-P\left(T_{23}>-k\right)\right\}=0.9 \\
& \leftrightarrow 1-P\left(T_{23}>k\right)-\left\{1-\left[1-P\left(T_{23}>k\right)\right]\right\}=0.9 \\
& \leftrightarrow 1-P\left(T_{23}>k\right)-\left\{1-1+P\left(T_{23}>k\right)\right\}=0.9 \\
& \leftrightarrow 1-P\left(T_{23}>k\right)-P\left(T_{23}>k\right)=0.9 \\
& \leftrightarrow 1-2 P\left(T_{23}>k\right)=0.9 \\
& \leftrightarrow 2 P(T 23>k)=0.1 \\
& \text { so } \quad=T . \operatorname{inv} .2 t(0.1,23)=1.71387
\end{aligned}
$$



## 328 stat

4. Chi-Square Distribution

Notes in Excel

1) $=\mathbf{C H I S Q} . \operatorname{DIST}(x, v, 0) \leftrightarrow f_{\chi_{v}}(x)$
2) $=$ CHISQ. $\operatorname{DIST}(\boldsymbol{x}, \boldsymbol{v}, \mathbf{1}) \quad \leftrightarrow P\left(\chi_{v} \leq x\right)$
3) $=$ CHISQ. DIST.RT $(x, v, 1) \leftrightarrow P\left(\chi_{v} \geq x\right)$
4) $=\operatorname{CHISQ} \cdot \operatorname{INV}(\boldsymbol{p}, v) \quad \leftrightarrow P\left(\chi_{v} \leq x_{0}\right)=p$
5) $=\mathbf{C H I S Q} \cdot \operatorname{INV} \cdot \operatorname{RT}(\boldsymbol{p}, \boldsymbol{v}) \quad \leftrightarrow P\left(\chi_{v} \geq x_{0}\right)=p$

By using chi- square distribution, Find:
$\chi_{0.995}^{2}$ when $v=19$

|  | By Excel (using (fx)) | By Minitab <br> calc $\rightarrow$ probability distribution |
| :---: | :---: | :---: |
| $\begin{gathered} \mathrm{P}\left(\chi_{19}<\mathrm{x}\right) \\ =0.995 \end{gathered}$ |  |  |

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5. F Distribution

Notes in Excel

$$
\begin{array}{ll}
\text { 1) }=\mathbf{F} . \operatorname{DIST}\left(\boldsymbol{f}, \boldsymbol{v}_{1}, v_{2}, \mathbf{0}\right) & \leftrightarrow f_{F_{v_{1}}, v_{2}}(f) \\
\text { 2) }=\mathbf{F} . \operatorname{DIST}\left(\boldsymbol{f}, \boldsymbol{v}_{1}, v_{2}, \mathbf{1}\right) & \leftrightarrow P\left(F_{v_{1}, v_{2}} \leq f\right) \\
\text { 3) } & =\text { F.DIST.RT }\left(\boldsymbol{f}, \boldsymbol{v}_{1}, v_{2}, \mathbf{1}\right) \\
\text { 4) } & =\text { F.INV }\left(\boldsymbol{p}, \boldsymbol{v}_{1}, \boldsymbol{v}_{2}\right)
\end{array}
$$

From the tables of F - distribution , Find:

$$
F_{0.995,15,22}
$$



## 328 stat

## HYPOTHESIS TESTING STATISTICS AND CONFIDENCES INTERVAL

|  | By Excel <br> (using (Data <br> Analysis)) | By Minitab |
| :--- | :---: | :---: |

[^0]In the programs (Excel and Spss for symmetric distribution), how to find $p$-value for the one tail from $p$-value for two tail?

| $p-$ value one tail <br> $p-$ value $_{\text {two tail }}$ | test statistical $>0$ | Then we have $p-$ value $_{\text {one tail }(>)}$ <br> and $p-$ value $_{\text {one tail }(<)}=1-p-$ value $_{\text {one tail }(>)}$ |
| :--- | :--- | :--- |
|  | test statistical $<0$ | Then we have $p-$ value $_{\text {one tail }(<)}$ <br> and $p-$ value $_{\text {one tail }(>)}=1-p-$ value $_{\text {one tail }(<)}$ |

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1) 

For a sample of 10 fruits from thirteen-year-old acidless orange trees, the fruit shape (determined as adiameter divided by height ) wae measured [ Shaheen and Hamouda (1984b)]:
$\begin{array}{llllllllll}1.066 & 1.084 & 1.076 & 1.051 & 1.059 & 1.020 & 1.035 & 1.052 & 1.046 & 0.976\end{array}$
Assuming that fruit shapes are approximately normally distributed, find and interpret a $90 \%$ confidence interval for the average fruit shape.
( T test one sample for mean with unknown variance By Minitab)


## One-Sample T: Q1

| Variable | N | Mean | StDev | SE Mean | 908 CI |
| :--- | ---: | ---: | ---: | ---: | :---: |
| Q1 | 10 | 1.04650 | 0.03103 | 0.00981 | $(1.02851 ; ~ 1.06449)$ |

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2) 

[In a sample of 185 people in the Western Region who had a particular bacterial infection, the mean egg count ( per gram of stool) was 141 [Ghandour et. al. (1991)]. Assume that egg counts of such people are normally distributed with a variance of 3025.]

Find and interpret a $90 \%$ confidence interval for the average egg count.
**
In a sample of 185 people in the Western Region who had a particular bacterial infection, the mean egg count ( per gram of stool ) was 141 . Assume that egg counts of such people are normally distributed with a variance of 3025 . Can we conclude that the true mean egg count is different from 130. . Use $\alpha=0.10$.
( Z test one sample for mean with known variance By Minitab)


## 328 stat

3) 

The phosphorus content was measured for independent samples of skim and whole Whole: $94.95 \quad 95.15 \quad 94.85 \quad 94.55 \quad 94.55 \quad 93.40$

Assuming normal populations with equal variances
a) Test whether the average phosphorus content of skim milk is less than the average phosphorus content of whole milk. Use $\alpha=0.01$
b) Find and interpret a $99 \%$ confidence interval for the difference in average phosphorus contents of whole and skim milk
( T test two samples for means assuming equal variance By Minitab)


## Two-Sample T-Test and CI: skim; whole

Two-sample $T$ for skim vs whole

|  | $N$ | Mean | StDev | SE Mean |
| :--- | ---: | ---: | ---: | ---: |
| skim | 10 | 91.340 | 0.483 | 0.15 |
| whole | 10 | 94.645 | 0.503 | 0.16 |

Difference $=\mu$ (skim) $-\mu$ (whole)
Estimate for difference: -3.305
998 upper bound for difference: -2.742
T-Test of difference $=0$ (vs <): I -Value $=-14.99 \quad \mathrm{P}$-Value $=0.000 \quad \mathrm{DF}=18$
Both use Pooled StDev $=0.4931$

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## Two-Sample T-Test and CI: skim; whole

|
Two-sample I for skim vs whole

|  | $N$ | Mean | StDev | SE Mean |
| :--- | ---: | ---: | ---: | ---: |
| skim | 10 | 91.340 | 0.483 | 0.15 |
| whole | 10 | 94.645 | 0.503 | 0.16 |

Difference $=\mu(s k i m)-\mu$ (whole)
Estimate for difference: -3.305
99\% CI for difference: ( -3.940 ; -2.670 )
$T$-Test of difference $=0(\mathrm{vs} \neq): \mathrm{T}$-Value $=-14.99 \quad \mathrm{P}$-Value $=0.000 \quad \mathrm{DF}=18$
Both use Pooled StDev $=0.4931$

Or

| C6 | C7-T | Two-Sample t for the Mean |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 91.25 | skim | C1 Q1 <br> C3 skim <br> C4 whole | Both samples are in one column |  |  |  |
| 91.80 | skim |  | Samples: $\quad$ C6 |  |  |  |
| 91.50 | skim |  |  |  |  |  |
| 91.65 | skim |  | Sample IDs: $\mathrm{C7}$ |  |  |  |
| 91.15 | skim |  |  |  |  |  |
| 90.25 | skim |  |  |  |  |  |
| 91.90 | skim |  |  |  |  |  |
| 91.25 | skim | Select |  | Options... | Graphs... |  |
| 91.65 | skim |  |  |  |  |  |
| 91.00 | skim |  |  |  |  |  |
| 94.95 | whole | Help |  | OK |  |  |
| 95.15 | whole | Two-Sample t: Options |  |  | $\times$ |  |
| 94.85 | whole | Difference $=($ sample 1 mean $)-($ sample 2 mean $)$ |  |  |  |  |
| 94.55 | whole |  |  |  |  |  |
| 94.55 | whole | Confidence level: $\quad 39$ |  |  |  |  |
| 93.40 | whole | Hypothesized difference: | 0.0 |  |  |  |
| 95.05 | whole |  |  |  |  |  |
| 94.35 | whole | Alternative hypothesis: | Difference < hypothesized difference |  | - |  |
| 94.70 | whole | $\checkmark$ Assume equal variances |  |  |  |  |
| 94.90 | whole |  |  |  |  |  |
|  |  | Help |  | OK Cancel |  |  |

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## Two-Sample T-Test and CI: C6; C7

Two-sample $T$ for C6

| C7 | N | Mean | StDev | SE Mean |
| :--- | ---: | ---: | ---: | ---: |
| skim | 10 | 91.340 | 0.483 | 0.15 |
| whole | 10 | 94.645 | 0.503 | 0.16 |

Difference $=\mu$ (skim) $-\mu$ (whole)
Estimate for difference: -3.305
$99 \%$ upper bound for difference: -2.742
T-Test of difference $=0(\mathrm{Vs} \mathrm{<} \mathrm{)} \mathrm{:} \mathrm{T-Value}=-14.99 \quad \mathrm{P}$-Value $=0.000 \quad \mathrm{DF}=18$
Both use Pooled StDev $=0.4931$

## Two-Sample t: Options

Difference $=($ sample 1 mean $)-($ sample 2 mean $)$
Confidence level:
99
Hypothesized difference: 0.0
Alternative hypothesis: Difference $\neq$ hypothesized difference
$\checkmark$ Assume equal variances

Help

## Two-Sample T-Test and CI: C6; C7

```
Two-sample I for C6
\begin{tabular}{lrrrr} 
C7 & N & Mean & StDev & SE Mean \\
skim & 10 & 91.340 & 0.483 & 0.15 \\
whole & 10 & 94.645 & 0.503 & 0.16
\end{tabular}
Difference = \mu (skim) - \mu (whole)
Estimate for difference: -3.305
99% CI for difference: (-3.940; -2.670)
I-Test of difference = 0 (vs f): T-Value = -14.99 P-Value = 0.000 DF = 18
Both use Pooled StDev =0.4931
```

(T test two samples for means assuming equal variance By Excel)


t-Test: Two-Sample Assuming Equal Variances

|  | skim | whole |
| :--- | ---: | ---: |
| Mean | 91.34 | 94.645 |
| Variance | 0.233222 | 0.253028 |
| Observations | 10 | 10 |
| Pooled Variance | 0.243125 |  |
| Hypothesized Mean Difference | 0 |  |
| df | 18 |  |
| t Stat | -14.9879 |  |
| $\mathrm{P}(\mathrm{T}<=\mathrm{t})$ one-tail | $6.53 \mathrm{E}-12$ |  |
| t Critical one-tail | 2.55238 |  |
| $\mathrm{P}(\mathrm{T}<=\mathrm{t})$ two-tail | $1.31 \mathrm{E}-11$ |  |
| t Critical two-tail | 2.87844 |  |

## 328 stat

4) 

In an experiment comparing 2 feeding methods for caves, eight pairs of twins were used one twin receiving Method A and other twin receiving Method B. At the end of a given time, the calves were slaughtered and cooked, and the meat was rated for its taste ( with a higher number indicating a better taste):

| Twin pair | Method A | Method B |
| :--- | :--- | :--- |
| 1 | 27 | 23 |
| 2 | 37 | 28 |
| 3 | 31 | 30 |
| 4 | 38 | 32 |
| 5 | 29 | 27 |
| 6 | 35 | 29 |
| 7 | 41 | 36 |
| 8 | 37 | 31 |

Assuming approximate normality, test if the average taste score for calves fed by Method B is less than the average taste foe calves fed by Method A. Use $\alpha=0.05$.
( T test parried two samples for means By Minitab)


## 328 stat

## Paired T－Test and CI：Method B；Method A

Paired I for Method B－Method A

|  | N | Mean | StDev | SE Mean |
| :--- | ---: | ---: | ---: | ---: |
| Method B | 8 | 29.50 | 3.82 | 1.35 |
| Method A | 8 | 34.38 | 4.87 | 1.72 |
| Difference | 8 | -4.875 | 2.532 | 0.895 |

｜95\％upper bound for mean difference：-3.179
I－Test of mean difference $=0(\mathrm{vs}<0): \mathrm{T}$－Value $=-5.45 \quad \mathrm{P}$－Value $=0.000$
（T test parried two samples for means By Excel）

| $\times \quad$ ¢ | Data Analysis |  | Method B | Method A |
| :---: | :---: | :---: | :---: | :---: |
|  |  |  | 23 | 27 |
| OK |  | Analysis Tools | 28 | 37 |
|  | $\wedge$ | Exponential Smoothing | 30 | 31 |
| Cancel |  | Fourier Analysis | 32 | 38 |
| İ． |  | Moving Averagam | 27 | 29 |
|  |  | Random Number Generation | 29 | 35 |
|  |  | Rank and Percentile | 36 | 41 |
|  |  | Regression Sampling | 31 | 37 |
|  |  | Paired Two Samole for Means |  |  |

x $\quad$ ¢ －Test：Paired Two Sample for Means

| OK | 閜 SFS1：\＄F59 |  | $\begin{array}{r} \text { Input } \\ : \text { Variable } \underline{1} \text { Range } \end{array}$ |  |
| :---: | :---: | :---: | :---: | :---: |
| Cancel | 罭 SE\＄1：\＄ET9 |  | ：Vari | Range |
| تعليمات | 0 |  | ：Hypothesized Mean Difference <br> Labels $\sqrt{V}$ |  |
|  |  |  |  |  |
|  |  |  | 0.05 | ：Alpha |
|  |  |  |  | options |
|  | 䦗 |  | ：Outpu | ange |
|  |  |  | ：New Works | Ply $\bigcirc$ |
|  |  |  | New W | book 0 |

t－Test：Paired Two Sample for Means

|  | Method B | Method A |
| :--- | ---: | ---: |
| Mean | 29.5 | 34.375 |
| Variance | 14.57143 | 23.69643 |
| Observations | 8 | 8 |
| Pearson Correlation | 0.857204 |  |
| Hypothesized Mean Difference | 0 |  |
| df | 7 |  |
| t Stat | -5.44586 |  |
| $\mathrm{P}(\mathrm{T}<=\mathrm{t})$ one－tail | 0.00048 |  |
| t Critical one－tail | 1.894579 |  |
| $\mathrm{P}(\mathrm{T}<=\mathrm{t})$ two－tail | 0.00096 |  |
| t Critical two－tail | 2.364624 |  |
|  |  |  |

## 328 stat

## 5)

Two independent samples of dates were taken-one from dates in the Khalal stage and one from dates at the Tamr stage. The calcium (in $\mathrm{mg} / \mathrm{loog}$ ) was measured [Sawaya (1986)]:

Khalal:30,57,29,23,55,50,49,74,101,97,79,158,112,107,93,63,70,90,98,48,75,64,71,72,146,37, $82,19,115,36,34,27,38,42,18,21,75,37,80,72,73,198,107,107,35,56,25,35,26,40,75,109,27,101$
Tamr: $14,25,21,18,28,14,19,20,44,18,24,47,19,52,31,38,41,39,35,16,47,26,26,30,81,18,42,9,49,2$ $3,27,14,15,17,10,16,18,14,13,32,42,55,42,27,30,17,24,14,20,17,48,20,76$
Assuming normal populations with unequal variances ( $\alpha=0.05$ )
a) Test whether the average calcium of dates at the khalal stage is more than this average for Tamar stage dates
b) Find the confidence interval for the difference in the average calcium of dates at the two stage

## 328 stat

(T test two samples for means assuming unequal variance By Minitab)

|  | Khalal | Tamr |
| :---: | :---: | :---: |
| 1 | 30 | 14 |
| 2 | 57 | 25 |
| 3 | 29 | 21 |
| 4 | 23 | 18 |
| 5 | 55 | 28 |
| 6 | 50 | 14 |
| 7 | 49 | 19 |
| 8 | 74 | 20 |
| 9 | 101 | 44 |
| 10 | 97 | 18 |
| 11 | 79 | 24 |
| 12 | 158 | 47 |
| 13 | 112 | 19 |
| 14 | 107 | 52 |
| 15 | 93 | 31 |
| 16 | 63 | 38 |
| 17 | 70 | 41 |
| 18 | 90 | 39 |
| 19 | 98 | 35 |
| 20 | 48 | 16 |
| 21 | 75 | 47 |
| 22 | 64 | 26 |
| 23 | 71 | 26 |
| 24 | 72 | 30 |


| 25 | 146 | 81 |
| :---: | :---: | :---: |
| 26 | 37 | 18 |
| 27 | 82 | 42 |
| 28 | 19 | 9 |
| 29 | 115 | 49 |
| 30 | 36 | 23 |
| 31 | 34 | 27 |
| 32 | 27 | 14 |
| 33 | 38 | 15 |
| 34 | 42 | 17 |
| 35 | 18 | 10 |
| 36 | 21 | 16 |
| 37 | 75 | 18 |
| 38 | 37 | 14 |
| 39 | 80 | 13 |
| 40 | 72 | 32 |
| 41 | 73 | 42 |
| 42 | 198 | 55 |
| 43 | 107 | 42 |
| 44 | 107 | 27 |
| 45 | 35 | 30 |
| 46 | 56 | 17 |
| 47 | 25 | 24 |
| 48 | 35 | 14 |
| 49 | 26 | 20 |
| 50 | 40 | 17 |
| 51 | 75 | 48 |
| 52 | 109 | 20 |
| 53 | 27 | 76 |
| 54 | 101 |  |

## 328 stat



Two-Sample T-Test and CI: Khalal; Tamr
Two-sample I for Khalal vs Tamr

|  | N | Mean | StDev | SE Mean |
| :--- | ---: | ---: | ---: | ---: |
| Khalal | 54 | 67.7 | 38.0 | 5.2 |
| Tamr | 53 | 28.7 | 15.7 | 2.2 |

Difference $=\mu($ Khalal $)-\mu$ (Tamr)
Estimate for difference: 39.02
$95 \%$ upper bound for difference: 48.36
T -Test of difference $=0$ (vs <): T-Value $=6.97 \quad \mathrm{P}$-Value $=1.000 \quad \mathrm{DF}=70$


## Two-Sample T-Test and CI: Khalal; Tamr

```
Two-sample I for Khalal vs Tamr
\begin{tabular}{lrrrr} 
& N & Mean & StDev & SE Mean \\
Khalal & 54 & 67.7 & 38.0 & 5.2 \\
Tamr & 53 & 28.7 & 15.7 & 2.2
\end{tabular}
Difference = \mu (Khalal) - \mu (Tamr)
Estimate for difference: 39.02
95% CI for difference: (27.85; 50.20)
T-Test of difference = 0 (vs 手): T-Value = 6.97 P-Value = 0.000 DF = 70
```


## 328 stat

（ T test two samples for means assuming unequal variance By Excel）


| ¢ t－Test：Two－Sample Assuming Unequal Variances |  |  |  | t－Test：Two－Sample Assuming Unequal Variances |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| OK | 凰 | \＄1\＄1：\＄1\＄55 | ：Variable 1 Range |  | Khalal | Tamr |
| Cancel | 蔵 | \＄］\＄1：\＄1\＄54 | ：Variable $\underline{2}^{\text {Range }}$ | Mean | 67.74074074 | 28.71698 |
|  |  |  |  | Variance | 1443.139064 | 247.2837 |
| － | 0 |  | ：Hypothesized Mean Difference | Observations | 54 | 53 |
|  |  |  | Labels $\square$ | Hypothesized Mean Difference | 0 |  |
|  |  |  | 0.05 ：Alpha | df | 71 |  |
|  |  |  |  | t Stat | 6.965139095 |  |
|  |  |  | Output options | $\mathrm{P}(\mathrm{T}<=\mathrm{t})$ one－tail | $6.80179 \mathrm{E}-10$ |  |
|  | 闌 |  | ：Output Range | t Critical one－tail | 1.666599658 |  |
|  |  |  | ：New Worksheet Ply $\bigcirc$ | $\mathrm{P}(\mathrm{T}<=\mathrm{t})$ two－tail | $1.36036 \mathrm{E}-09$ |  |
|  |  |  | New Workbook | t Critical two－tail | 1.993943368 |  |

## 328 stat

6) 

Formation of vitamin $D$ depends on exposure to ultraviolet radiation in sunlight. A sample of Saudis was classified by the type of residence and the level of vitamin D [Sedrani et al. (1992)]:

Vitamin D Level

| Residence type | Insufficient <br> $<5 \mathrm{ng} / \mathrm{ml}$ | Low <br> $5-10 \mathrm{ng} / \mathrm{ml}$ | Sufficient <br> $>10 \mathrm{ng} / \mathrm{ml}$ | Total |
| :---: | :---: | :---: | :---: | :---: |
| Tent | 6 | 31 | 97 | 134 |
| Mud house | 16 | 73 | 349 | 438 |
| Flat | 45 | 174 | 652 | 871 |
| Villa | 64 | 323 | 1061 | 1448 |
| Brick house | 51 | 250 | 886 | 1187 |
| Total | 182 | 851 | 3045 | 4078 |

Test whether the Vitamin D level of Saudis is related to the type of residence. Use a level of significance of 0.05 .
(Independent test By Minitab)


## 328 stat

## Chi-Square Test for Association: Worksheet rows; Worksheet columns

Rows: Worksheet rows Columns: Worksheet columns

|  | C16 | C17 | C18 | All |
| :--- | ---: | ---: | ---: | ---: |
| 1 | 6 | 31 | 97 | 134 |
|  | 6.0 | 28.0 | 100.1 |  |
| 2 | 16 | 73 | 349 | 438 |
|  | 19.5 | 91.4 | 327.1 |  |
| 3 | 45 | 174 | 652 | 871 |
|  | 38.9 | 181.8 | 650.4 |  |
| 4 | 64 | 323 | 1061 | 1448 |
|  | 64.6 | 302.2 | 1081.2 |  |
| 5 | 51 | 250 | 886 | 1187 |
|  | 53.0 | 247.7 | 886.3 |  |
| All | 182 | 851 | 3045 | 4078 |
| Cell Contents: |  | Count |  |  |
|  |  |  | Expected count |  |

Pearson Chi-Square $=9.461$; $\mathrm{DF}=8$; P -Value $=0.305$
Likelihood Ratio Chi-Square $=9.668$; $\mathrm{DF}=8$; P-Value $=0.289$
Or


## 328 stat

## Tabulated Statistics: C21; C22

Using frequencies in C20

Rows: C21 Columns: C22

|  | 1 | 2 | 3 | All |
| :---: | :---: | :---: | :---: | :---: |
| 1 | 6 | 31 | 97 | 134 |
|  | 6.0 | 28.0 | 100.1 |  |
| 2 | 16 | 73 | 349 | 438 |
|  | 19.5 | 91.4 | 327.1 |  |
| 3 | 45 | 174 | 652 | 871 |
|  | 38.9 | 181.8 | 650.4 |  |
| 4 | 64 | 323 | 1061 | 1448 |
|  | 64.6 | 302.2 | 1081.2 |  |
| 5 | 51 | 250 | 886 | 1187 |
|  | 53.0 | 247.7 | 886.3 |  |
| All | 182 | 851 | 3045 | 4078 |
| Cell Contents: |  |  | Count |  |
|  |  |  | Expecte | coun |

Pearson Chi-Square $=9.461 ; \mathrm{DF}=8$; P -Value $=0.305$
Likelihood Ratio Chi-Square $=9.668 ; \mathrm{DF}=8 ; \mathrm{P}$-Value $=0.289$

## 328 stat

7) 

A firm wishes to compare four programs for training workers to perform a certain manual task. Twenty new employees are randomly assigned to the training programs, with 5 in each program. At the end of the training period, a test is conducted to see how quickly trainees can perform the task. The number of times the task is performed per minute is recorded for each trainee, with the following results:

| Observation | Program 1 | Program 2 | Program 3 | Program 4 |
| ---: | ---: | ---: | ---: | ---: |
| 1 | 9 | 10 | 12 | 9 |
| 2 | 12 | 6 | 14 | 8 |
| 3 | 14 | 9 | 11 | 11 |
| 4 | 11 | 9 | 13 | 7 |
| 5 | 13 | 10 | 11 | 8 |

## (One-way ANOVA by Minitab)



## 328 stat



## One-Way Analysis of Variance: Comparisons $x$

Error rate for comparisons: 5

Comparison procedures assuming equal variances
$\sqrt{V}$ Iukey
$\Gamma$ Eisher
「 Dunnett Control group level: $\mathrm{C} 25 \quad \square$
$\Gamma$ Hsu MCB
Best:
Largest mean is best

Results
I Interval plot for differences of means

- Grouping information
$\Gamma$ Tests

Help
QK
Cancel

One-way ANOVA: C25; C26; C27; C28
Method
Null hypothesis All means are equal
Alternative hypothesis At least one mean is different Significance level $\quad \alpha=0.05$

Equal variances were assumed for the analysis.

Factor Information
Factor Levels Values
Factor $\quad 4$ C25; C26; C27; C28

Analysis of Variance
Source DF Adj SS Adj MS F-Value P-Value

| Factor | 3 | 54.95 | 18.317 | 7.04 | 0.003 |
| :--- | ---: | ---: | ---: | ---: | ---: |

Error $16 \quad 41.60 \quad 2.600$

Total $19 \quad 96.55$

Tukey Simultaneous 95\% Cls


## 328 stat

Or



One-Way Analysis of Variance: Comparisons

```
Error rate for comparisons: [5
Comparison procedures assuming equal variances
    V Iukey
    \ulcorner \text { Fisher}
    \unnett
                Control group level: C25
    Hsu MCB
                Best
    Results
    Interval plot for differences of means
    Grouping information
    \Gamma ~ T e s t s
    Help
                            OK
                Cancel
```


## 328 stat

## One-way ANOVA: C30 versus C31

## Method

Null hypothesis
All means are equal
Alternative hypothesis At least one mean is different Significance level $\alpha=0.05$

Equal variances were assumed for the analysis.

Factor Information
Factor Levels Values
C31 $\quad 4$ 1; 2; 3; 4

Analysis of Variance
Source DF Adj SS Adj MS F-Value P-Value
$\begin{array}{llllll}\text { C31 } & 3 & 54.95 & 18.317 & 7.04 & 0.003\end{array}$
Error $16 \quad 41.60 \quad 2.600$
Total $19 \quad 96.55$

## Tukey Simultaneous 95\% Cls

(One-way ANOVA by Excel)


| $\times \quad ¢$ | Anova: Single Factor |  |  |
| :---: | :---: | :---: | :---: |
| OK |  |  | Input |
| OK |  |  | :Input Range |
| Cancel | Columns <br> Rows |  | :Grouped By |
| تـعليمات |  |  |  |
|  |  |  | Labels in first row $\square$ |
|  |  |  | 0.05 :Alpha |
|  |  |  | Output options |
|  | 區 |  | :Qutput Range $\bigcirc$ |
|  |  |  | :New Worksheet Ply $\bigcirc$ |
|  |  |  | New Workbook |

## 328 stat

| Anova: Single Factor |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| SUMMARY |  |  |  |  |  |  |
| Groups | Count | Sum | Average | Variance |  |  |
| Column 1 | 5 | 59 | 11.8 | 3.7 |  |  |
| Column 2 | 5 | 44 | 8.8 | 2.7 |  |  |
| Column 3 | 5 | 61 | 12.2 | 1.7 |  |  |
| Column 4 | 5 | 43 | 8.6 | 2.3 |  |  |
|  |  |  |  |  |  |  |
| ANOVA |  |  |  |  |  |  |
| Source of Variation | SS | df | MS | $F$ | $P$-value | Fcrit |
| Between Groups | 54.95 | 3 | 18.31667 | 7.044872 | 0.003113 | 3.238872 |
| Within Groups | 41.6 | 16 | 2.6 |  |  |  |
| Total | 96.55 | 19 |  |  |  |  |

## 328 stat

8) 

Ten Corvettes between 1 and 6 years old were randomly selected from last year's sales records in Virginia Beach, Virginia. The following data were obtained, where x denotes age, in years, and y denotes sales price, in hundreds of dollars.

| $x$ | 6 | 6 | 6 | 4 | 2 | 5 | 4 | 5 | 1 | 2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 125 | 115 | 130 | 160 | 219 | 150 | 190 | 163 | 260 | 260 |

a) Determine the regression equation for the data.
b) Compute and interpret the coefficient of determination, $\mathrm{r}^{2}$.
c) Obtain a point estimate for the mean sales price of all 4 -year-old Corvettes.
(Linear regression by Minitab)


## 328 stat

## Regression Analysis: y versus x

|
Model Summary

| S | R-sq | R-sq(adj) | R-sq(pred) |
| ---: | ---: | ---: | ---: |
| 14.2465 | $93.68 \%$ | $92.89 \%$ | $90.16 \%$ |


| Coefficients |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: |
|  |  |  |  |  |  |
| Term | Coef | SE Coef | T-Value | P-Value | VIF |
| Constant | 291.6 | 11.4 | 25.51 | 0.000 |  |
| x | -27.90 | 2.56 | -10.89 | 0.000 | 1.00 |

Regression Equation
$y=291.6-27.90 x$
(Linear regression by Excel)


| $\times$ ¢ | Regression |  |  |
| :---: | :---: | :---: | :---: |
|  | 臨 \$ $\$ \$ 1: \$ 5 \$ 11$ |  | $\begin{array}{r} \text { Input } \\ \text { :Input } \underset{\text { R Range }}{ } \end{array}$ |
|  |  |  |  |
| Cancel |  |  | :Input $\underline{X}$ Range |
| تِعليمات | $\begin{array}{r} \text { Constant is Zero } \square \\ \% 95 \end{array}$ |  | Labels $\square$ :Confidence Level $\square$ |
|  |  |  |  |
|  | 瀶 |  | Output options |
|  |  |  | :Output Range $\bigcirc$ |
|  |  |  | :New Worksheet Ply $\bigcirc$ |
|  | New Workbook © |  |  |
|  | Residual Plots $\square$ <br> Line Fit Plots $\square$ |  | Residuals <br> Residuals $\square$ <br> Standardized Residuals $\square$ |
|  |  |  |  |
|  |  |  |  |
|  | Normal Probability <br> Normal Probability Plots |  |  |
|  |  |  |  |  |

## 328 stat

| SUMMARY OUTPUT |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |
| Regression Statistics |  |  |  |  |  |  |  |  |
| Multiple R | 0.967871585 |  |  |  |  |  |  |  |
| R Square | 0.936775406 |  |  |  |  |  |  |  |
| Adjusted R Square | 0.928872332 |  |  |  |  |  |  |  |
| Standard Error | 14.24652913 |  |  |  |  |  |  |  |
| Observations | 10 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |
| ANOVA. |  |  |  |  |  |  |  |  |
|  | df | SS | MS | $F$ | Significance $F$ |  |  |  |
| Regression | 1 | 24057.89126 | 24057.89 | 118.533 | $4.48427 \mathrm{E}-06$ |  |  |  |
| Residual | 8 | 1623.708738 | 202.9636 |  |  |  |  |  |
| Total | 9 | 25681.6 |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |
|  | Coefficients | Standard Error | $t$ Stat | $P$-value | Lower 95\% | Upper 95\% | Lower 95.0\% | Upper 95.0\% |
| Intercept | 291.6019417 | 11.43289905 | 25.50551 | $5.98 \mathrm{E}-09$ | 265.2376293 | 317.9662542 | 265.2376293 | 317.9662542 |
| x | -27.90291262 | 2.562889198 | -10.8873 | 4.48E-06 | -33.81294571 | -21.99287953 | -33.81294571 | -21.99287953 |

Spss

Q1)
For a sample of 10 fruits from thirteen-year-old acidless orange trees, the fruit shape (determined as adiameter divided by height) wae measured [ Shaheen and Hamouda (1984b)]: $\begin{array}{llllllllll}1.066 & 1.084 & 1.076 & 1.051 & 1.059 & 1.020 & 1.035 & 1.052 & 1.046 & 0.976\end{array}$
Assuming that fruit shapes are approximately normally distributed, find and interpret a $90 \%$ confidence interval for the average fruit shape.

Q2)
The phosphorus content was measured for independent samples of skim and whole
Whole: $94.95 \quad 95.1594 .8594 .55 \quad 94.55 \quad 93.40 \quad 95.05 \quad 94.35 \quad 94.7094 .90$
Skim: $91.25 \quad 91.80 \quad 91.50 \begin{array}{llllllllllllllllll} & 91.65 & 91.15 & 90.25 & 91.90 & 91.25 & 91.65 & 91.00\end{array}$
Assuming normal populations with equal variances
a) Test whether the average phosphorus content of skim milk is less than the average phosphorus content of whole milk. Use $\alpha=0.01$
b) Find and interpret a $99 \%$ confidence interval for the difference in average phosphorus contents of whole and skim milk

Q3)
What is the relationship between the gender of the students and the assignment of a Pass or No Pass test grade? (Pass = score 70 or above).

|  | Pass | No Pass | Row Totals |
| :--- | :--- | :--- | :--- |
| Males | 12 | 3 | 15 |
| Females | 13 | 2 | 15 |
| Column Totals | 25 | 5 | 30 |

Q4)
A firm wishes to compare four programs for training workers to perform a certain manual task. Twenty new employees are randomly assigned to the training programs, with 5 in each program. At the end of the training period, a test is conducted to see how quickly trainees can perform the task. The number of times the task is performed per minute is recorded for each trainee, with the following results:

| Observation | Program 1 | Program 2 | Program 3 | Program 4 |
| ---: | ---: | ---: | ---: | ---: |
| 1 | 9 | 10 | 12 | 9 |
| 2 | 12 | 6 | 14 | 8 |
| 3 | 14 | 9 | 11 | 11 |
| 4 | 11 | 9 | 13 | 7 |
| 5 | 13 | 10 | 11 | 8 |

## 328 stat

Q5)
Ten Corvettes between 1 and 6 years old were randomly selected from last year's sales records in Virginia Beach, Virginia. The following data were obtained, where x denotes age, in years, and y denotes sales price, in hundreds of dollars.

| $x$ | 6 | 6 | 6 | 4 | 2 | 5 | 4 | 5 | 1 | 2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 125 | 115 | 130 | 160 | 219 | 150 | 190 | 163 | 260 | 260 |

a) Compute and interpret the linear correlation coefficient, r .
b) Determine the regression equation for the data.
c) Compute and interpret the coefficient of determination, $\mathrm{r}^{2}$.
d) Obtain a point estimate for the mean sales price of all 4 -year-old Corvettes.

Q1) to use the T- test, we need to make sure that the population follows a normal distribution i.e.
$H_{0}$ : the population follows a normal distribution Vs
$H_{1}$ : the population does not follow a normal distribution
However, we find the question he said that the population follows a normal distribution, so is not necessary to make this test.

Now, $\mathbf{9 0 \%}$ Confidence interval of the mean can be found in two ways:

1) The first method:



## $\Rightarrow$ T.Test

[DataSet0]

One-Sample Statistics

|  | $N$ | Mean | Std. Deviation | Std. Error <br> Mean |
| :--- | ---: | ---: | ---: | ---: |
| FruitShape | 10 | 1.0465 | .03103 | .00981 |

One-Sample Test

C.I for the mean

## 328 stat

2) The second method:


It helps in the calculation of the confidence interval and find the statistical measures



## 328 stat

## $\Rightarrow$ Explore

Case Processing Summary

|  | Cases |  |  |  |  |  |
| :---: | :---: | ---: | ---: | ---: | ---: | ---: |
|  | Valid |  | Missing |  | Total |  |
|  | N | Percent | N |  | Percent | N |
| Percent |  |  |  |  |  |  |
| FruitShape | 10 | $50.0 \%$ | 10 | $50.0 \%$ | 20 | $100.0 \%$ |

Descriptives


Tests of Normality

|  | Kolmogorov-Smirnov $^{\text {a }}$ |  |  | Shapiro-Wilk |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | :--- | :---: |
|  | Statistic | df | Sig. | Statistic | df | Sig. |  |
| FruitShape | .194 | 10 | $200^{*}$ | .907 | 10 | -260 |  |

*. This is a lower bound of the true signiffeance.
a. Lilliefors Significance Correction

$$
\text { As } \mathrm{P}-\text { value }>.1
$$

So, we except $H_{0}$ : the population follows a normal distribution

## 328 stat

Q2) to use the T- test for two sample, we need to make sure that

1) The independence of the two samples: It is very clear that there is no correlation between the values of the two samples.
2) The populations follow a normal distribution
$\square$ i.e.

$$
\begin{aligned}
& H_{0} \text { : the two populations follow a normal distribution } \\
& \qquad V s \\
& H_{1} \text { : the two populations do not follow a normal distribution }
\end{aligned}
$$

However, we find the question he said that the populations follows a normal distribution, so is not necessary to make this test.
*To make sure no more $\qquad$


|  | Variable | grouping | var |
| :---: | :---: | :---: | :---: |
| - | 94.95 | Whole |  |
| - | 95.15 | Whole |  |
| - | 94.85 | Whole |  |
| - | 94.55 | Whole |  |
| - | 94.55 | Whole |  |
| - | 93.40 | Whole |  |
| - | 95.05 | Whole |  |
| - | 94.35 | Whole |  |
| - | 94.70 | Whole |  |
| - | 94.90 | Whole |  |
| - | 91.25 | Skim |  |
| - | 91.80 | Skim |  |
| - | 91.50 | Skim |  |
| - | 91.65 | Skim |  |
| - | 91.15 | Skim |  |
| - | 90.25 | Skim |  |
| - | 91.90 | Skim |  |
| - | 91.25 | Skim |  |
| - | 91.65 | Skim |  |
| - | 91.00 | Skim |  |
|  |  |  |  |
|  |  |  |  |
|  |  |  |  |

## 328 stat



It helps in the calculation of the confidence interval and find statistical measures for each sample



Helps in the normality test

## 328 stat

## Explore

grouping

| Case Processing Summary |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | grouping | Cases |  |  |  |  |  |
|  |  | Valid |  | Missing |  | Total |  |
|  |  | N | Percent | N | Percent | N | Percent |
| Variable | Skim | 10 | 100.0\% | 0 | 0.0\% | 10 | 100.0\% |
|  | Whole | 10 | 100.0\% | 0 | 0.0\% | 10 | 100.0\% |

Descriptives

| grouping |  |  |  | Statistic | Std. Error | $\mathcal{Z}$ | C.I for the mean for the skim |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Variable | Skim | Mean |  | 91.3400 | . 15272 |  |  |
|  |  | 99\% Confidence Interval | Lower Bound | 90.8437 |  |  |  |
|  |  | for Mean | Upper Bound | 91.8363 |  |  |  |
|  |  | 5\% Trimmed Mean |  | 91.3694 |  |  |  |


|  |  |  |  |  | $\cdots$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Interquartile Range |  | . 57 |  | $1$ |  |
|  | Skewness |  | -1.241 | 687 |  |  |
|  | Kurtosis |  | 2.035 | 1.334 |  |  |
| Whole | Mean |  | 94.6450 | . 15907 |  | C.I for the mean for the whole |
| $\begin{array}{\|c\|} \hline \begin{array}{c} \text { Double-click to } \\ \text { activate } \end{array} \\ \hline \end{array}$ | 99\% Confidence Interval for Mean | Lower Bound Upper Bound | $\begin{aligned} & 94.1281 \\ & 95.1619 \\ & \hline \end{aligned}$ |  |  |  |
|  | 5\% Trimmed Mean |  | 94.6861 |  |  |  |
|  | Median |  | 94.7750 |  |  |  |



As $\mathrm{P}-$ value $>.01$ for both populations.
So, we except $H_{0}$ : the two populations follow a normal distribution

## 328 stat

Now, the goal of the question:
a) $H_{0}: \mu_{\text {whole }}-\mu_{\text {skim }}=0$ Vs $\quad H_{1}: \mu_{\text {whole }}-\mu_{\text {skim }}>0$ at $\alpha=.01$ and
b) $90 \%$ Confidence interval of $\mu_{\text {whole }}-\mu_{\text {skim }}$



## 328 stat

This for test

$$
H_{0}: \sigma_{\text {whole }}^{2}=\sigma_{\text {skim }}^{2} \quad \text { Vs } \quad H_{1}: \sigma_{\text {whole }}^{2} \neq \sigma_{\text {skim }}^{2}
$$

As $\mathrm{P}-$ value $>.01$. So, we except $H_{0}$. However, it is given in question.

\section*{$\Rightarrow$ T-Test <br> | Group Statistics |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | grouping | N | Mean | Std. Deviation | $\begin{gathered} \hline \text { Std. Error } \\ \text { Mean } \end{gathered}$ |
| Variable | Whole | 10 | 94.6450 | . 50302 | . 15907 |
|  | Skim | 10 | 91.3400 | . 48293 | . 15272 |

Infependent Samples Test

|  |  | Levene's Test for Equality of Variances |  | t-testor Equality of Means |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | F | $\begin{aligned} & \\ & \\ & \text { sig. } \\ & \hline \end{aligned}$ | $t$ | df | Sig. (2-tailed) | $\begin{aligned} & \text { Mean } \\ & \text { Difference } \end{aligned}$ | Std. Eror Difference | $99 \%$ Confidence Interval of the Difference |  |
|  |  | Lower |  |  |  |  |  |  | Upper |
| Variable | Equal variances assumed |  | . 009 | . 924 | 14.988 |  | -000 | 3.30500 | . 22051 | 2.67027 | ${ }^{3.93973}$ |
|  | Equal variances not assumed |  |  | 14.988 |  | . 000 | 3.30500 | . 22051 | 2.67015 | $3.93985$ |
| $4.988>0 \text { so } P-\text { value }=P\left(T_{18}>t\right)=0$ <br> then we reject $H_{0}: \mu_{\text {whole }}-\mu_{\text {skim }}=0$. |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

$$
99 \% \text { C.I for } \mu_{\text {whole }}-\mu_{\text {skim }}
$$

## Q3)

$H_{0}$ : the gender of the students is indep. of a Pass or No Pass test grade

## Vs

$H_{1}$ : the gender of the students is not indep. of a Pass or No Pass test grade

| Count | PassOrNot | Gender | var |
| ---: | ---: | ---: | ---: | ---: |
| 1.00 | 1.00 | 1.00 |  |
| 2.00 | 1.00 | 1.00 |  |
| 3.00 | 1.00 | 1.00 |  |
| 4.00 | 1.00 | 1.00 |  |
| 5.00 | 1.00 | 1.00 |  |
| 6.00 | 1.00 | 1.00 |  |
| 7.00 | 1.00 | 1.00 |  |
| 8.00 | 1.00 | 1.00 |  |
| 9.00 | 1.00 | 1.00 |  |
| 10.00 | 1.00 | 1.00 |  |
| 12.00 | 1.00 | 1.00 |  |
| 13.00 | 1.00 | 1.00 |  |
| 14.00 | 2.00 | 1.00 |  |
| 15.00 | 2.00 | 1.00 |  |
| 17.00 | 2.00 | 1.00 |  |
| 1.00 | 1.00 | 2.00 |  |
| 19.00 | 1.00 | 2.00 |  |
| 19.00 | 1.00 | 2.00 |  |
| 20.00 | 1.00 | 2.00 |  |
| 21.00 | 1.00 | 2.00 |  |
| 22.00 | 1.00 | 2.00 |  |
| 23.00 | 1.00 | 2.00 |  |
| 24.00 | 1.00 | 2.00 |  |
| 25.00 | 1.00 | 2.00 |  |
| 26.00 | 1.00 | 2.00 |  |
| 27.00 | 1.00 | 2.00 |  |
| 28.00 | 1.00 | 2.00 |  |
| 29.00 | 1.00 | 2.00 |  |
|  | 2.00 | 2.00 |  |
|  |  |  |  |


| 30.00 | 2.00 | 2.00 |  |
| ---: | ---: | ---: | ---: |
|  |  |  |  |





## 328 stat

## Crosstabs

| Case Processing Summary |  |  |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: |
|  | Cases |  |  |  |  |  |
|  | Valid |  | Missing |  | Total |  |
|  | N | Percent | N | Percent | N | Percent |
|  | 30 | $100.0 \%$ | 0 | $0.0 \%$ | 30 | $100.0 \%$ |

Gender *PassOrNot Crosstabulation

|  |  | PassOrNot |  |  |  |
| :--- | :--- | :--- | ---: | ---: | ---: |
|  |  | 1.00 | 2.00 | Total |  |
| Gender | 1.00 | Count | 12 | 3 | 15 |
|  |  | Expected Count | 12.5 | 2.5 | 15.0 |
|  | 2.00 | Count | 13 | 2 | 15 |
|  |  | Expected Count | 12.5 | 2.5 | 15.0 |
| Total |  | Count | 25 | 5 | 30 |
|  |  | Expected Count | 25.0 | 5.0 | 30.0 |

The Chi-Square statistic


|  | Value | df Asymp. Sig. <br> (2-sides)  | Exact Sig. (2sided) | $\begin{aligned} & \text { Exact Sig. (1- } \\ & \text { sided) } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: |
| Pearson Chi-Square | $240^{\text {a }}$ | $1 \quad 624$ |  |  |
| Continuity Correction ${ }^{\text {b }}$ | . 000 | $1 \quad 1.000$ |  |  |
| Likelihood Ratio | . 241 | 1 . 623 |  |  |
| Fisher's Exact Test |  | \| | 1.000 | . 500 |
| Linear-by-Linear Association | . 232 |  |  |  |
| N of Valid Cases | 30 | $1$ |  |  |
| a. 2 cells $(50.0 \%)$ have expected count less thar 5 . The minimum expected count is 2.50 . |  |  |  |  |
| b. Computed only for a |  |  |  |  |

$P-$ value $>(\alpha=.05)$ so we except $H_{0}$

As we can see that 2 cells have expected count less than 5 because these 2 cells contain less than 5 observations. So the solution is will
be Merge cells until we get the expectation greater than 5 but here it is not possible, so take a larger sample.

## 328 stat

Q4) to use the one way ANOVA- test, we need to make sure that

1) The independence of the four samples: It is very clear that there is no correlation between the values of the four samples.
2) The populations follow a normal distribution
$H_{0}$ : the four populations follow a normal distribution
Vs
$H_{1}$ : the four populations do not follow a normal distribution


## 328 stat




## 328 stat

Explore
[DataSet1] E: \328\7 انـلـ
TypesOfProgram

Case Processing Summary

| TypesOfProgram |  | Cases |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Valid |  | Missing |  | Total |  |
|  |  | N | Percent | N | Percent | N | Percent |
| NumberOfTask | 1.00 | 5 | 100.0\% | 0 | 0.0\% | 5 | 100.0\% |
|  | 2.00 | 5 | 100.0\% | 0 | 0.0\% | 5 | 100.0\% |
|  | 3.00 | 5 | 100.0\% | 0 | 0.0\% | 5 | 100.0\% |
|  | 4.00 | 5 | 100.0\% | 0 | 0.0\% | 5 | 100.0\% |

Descriptives

| TypesOfProgram |  |  |  | Statistic | Std. Error |
| :---: | :---: | :---: | :---: | :---: | :---: |
| NumberOfTask | 1.00 | Mean |  | 11.8000 | . 86023 |
|  |  | 95\% Confidence Interval | Lower Bound | 9.4116 |  |
|  |  |  | Upper Bound | 14.1884 |  |
|  |  | 5\% Trimmed Mean |  | 11.8333 |  |
|  |  | Median |  | 12.0000 |  |
|  |  | Variance |  | 3.700 |  |
|  |  | Std. Deviation |  | 1.92354 |  |
|  |  | Minimum |  | 9.00 |  |
|  |  | Maximum |  | 14.00 |  |
|  |  | Range |  | 5.00 |  |
|  |  | Interquartile Range |  | 3.50 |  |
|  |  | Skewness |  | -. 590 | . 913 |
|  |  | Kurtosis |  | -. 022 | 2.000 |
|  | 2.00 | Mean |  | 8.8000 | . 73485 |



|  | TypesOfProgram | Kolmogorov-Smirnov ${ }^{\text {a }}$ |  |  | Shapiro-Wilk |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Statistic | df | Sig. | Statistic | df | Sig. |
| NumberOfTask | 1.00 | .141 | 5 | .200* | . 979 | 5 | . 928 |
|  | 2.00 | . 348 | 5 | . 047 | . 779 | 5 | . 054 |
|  | 3.00 | . 221 | 5 | .200* | . 902 | 5 | -. 421 |
|  | 4.00 | . 254 | 5 | .200* | . 914 | - 5 | . 492 |

*. This is a lower bound of the true significance.
a. Lilliefors Significance Correction

$$
\text { As } \mathrm{P}-\text { value }>.05 \text { for the four populations. }
$$

So, we except $H_{0}$ : the four populations follow a normal distribution

## 328 stat

3) Homogeneity of Variance (to get a test of the assumption of homogeneity of variance) i.e.

$$
H_{0}: \sigma_{\text {program } 1}^{2}=\sigma_{\text {program } 2}^{2}=\sigma_{\text {program } 3}^{2}=\sigma_{\text {program } 4}^{2}
$$

i.e. the variances of each sample are equal Vs
$H_{1}$ : The variances are not all equal
This will be clear later.
Now, the goal of the question:

$$
\begin{gathered}
H_{0}: \mu_{\text {program } 1}=\mu_{\text {program } 2}=\mu_{\text {program } 3}=\mu_{\text {program } 4} \\
\text { i.e. treatments are equally effective }
\end{gathered}
$$

## Vs

$H_{1}$ : The means are not all equal

$$
\text { at } \alpha=.05
$$



Helps in the homogeneity of variance test

## 328 stat

If we reject $\mathrm{H}_{0}$ in Analysis of Variance (ANOVA one way-test) we need to look at the multiple comparisons output by use the appropriate post hoc procedure (LSD) to determine whether unique pairwise comparisons are significant.

as $P-$ value $<.05$,then we reject $H_{0}: \mu_{\text {program } 1}=\mu_{\text {program } 2}=\mu_{\text {program } 3}=\mu_{\text {program } 4}$.

| Multiple Comparisons |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Dependent Variable: NumberOfTaskLSD |  |  |  |  |  |  |
| (1) TypesOfProgram | (J) TypesOfProgram | Mean Difference (IJ) | Std. Error | Sig. | 95\% Confidence Interval |  |
|  |  |  |  |  | Lower Bound | Upper Bound |
| 1.00 | 2.00 | $3.00000^{*}$ | 1.01980 | . 010 | . 8381 | 5.1619 |
|  | 3.00 | -. 40000 | 1.01980 | . 700 | -2.5619 | 1.7619 |
|  | 4.00 | $3.20000^{*}$ | 1.01980 | . 006 | 1.0381 | 5.3619 |
| 2.00 | 1.00 | -3.00000* | 1.01980 | . 010 | -5.1619 | -. 8381 |
|  | 3.00 | -3.40000* | 1.01980 | . 004 | -5.5619 | -1.2381 |
|  | 4.00 | . 20000 | 1.01980 | . 847 | -1.9619 | 2.3619 |
| 3.00 | 1.00 | . 40000 | 1.01980 | . 700 | -1.7619 | 2.5619 |
|  | 2.00 | $3.40000^{*}$ | 1.01980 | . 004 | 1.2381 | 5.5619 |
|  | 4.00 | $3.60000^{*}$ | 1.01980 | . 003 | 1.4381 | 5.7619 |
| 4.00 | 1.00 | -3.20000* | 1.01980 | . 006 | -5.3619 | -1.0381 |
|  | 2.00 | -. 20000 | 1.01980 | . 847 | -2.3619 | 1.9619 |
|  | 3.00 | $-3.60000^{*}$ | 1.01980 | . 003 | -5.7619 | -1.4381 |

*. The mean difference is significant at the 0.05 level


1) $H_{0}: \mu_{\text {program }_{1}}=\mu_{\text {program }_{2}}$ vs $H_{1}: \mu_{\text {program }_{1}} \neq \mu_{\text {program }_{2}}$ at $\alpha=.05$ as $P-$ value $=.01<.05$, then we reject $H_{0}$.
2) $H_{0}: \mu_{\text {program }_{1}}=\mu_{\text {program }_{3}}$ vs $H_{1}: \mu_{\text {program }_{1}} \neq \mu_{\text {program }_{3}}$ at $\alpha=.05$ as $\mathrm{P}-$ value $=.7>.05$, then we except $H_{0}$.
3) $H_{0}: \mu_{\text {program }_{1}}=\mu_{\text {program } 4}$ vs $H_{1}: \mu_{\text {program }_{1}} \neq \mu_{\text {program }_{4}}$ at $\alpha=.05$ as $P-$ value $=.006<.05$, then we reject $H_{0}$.
4) $H_{0}: \mu_{\text {program }_{2}}=\mu_{\text {program } 3}$ vs $H_{1}: \mu_{\text {program }_{2}} \neq \mu_{\text {program }_{3}}$ at $\alpha=.05$ as $P-$ value $=.004<.05$, then we reject $H_{0}$.
5) $H_{0}: \mu_{\text {program } 2}=\mu_{\text {program }_{4}}$ vs $H_{1}: \mu_{\text {program }_{2}} \neq \mu_{\text {program }_{4}}$ at $\alpha=.05$ as $\mathrm{P}-$ value $=.847>.05$, then we except $H_{0}$.
6) $H_{0}: \mu_{\text {program }_{3}}=\mu_{\text {program } 4}$ vs $H_{1}: \mu_{\text {program }_{3}} \neq \mu_{\text {program }_{4}}$ at $\alpha=.05$ as $P-$ value $=.003<.05$, then we reject $H_{0}$.

## 328 stat

## Q5)

Enter the age values into one variable and the corresponding sales price values into another variable (see figure, below).

| $\times$ | $Y$ | var |
| :---: | :---: | :---: |
| 6.00 | 125.00 |  |
| 6.00 | 115.00 |  |
| 6.00 | 130.00 |  |
| 4.00 | 160.00 |  |
| 2.00 | 219.00 |  |
| 5.00 | 150.00 |  |
| 4.00 | 190.00 |  |
| 5.00 | 163.00 |  |
| 1.00 | 260.00 |  |
| 2.00 | 260.00 |  |
| - | $\checkmark$ |  |
| - | - |  |
| - | - |  |
| - | - |  |
| - | - |  |
| - | - |  |
| - | - |  |
| - | - |  |
| - | - |  |
| - | - |  |
| - | - |  |
| - | - |  |
| - | - |  |
| - | - |  |
| - | - |  |
| - | - |  |

## 328 stat

a) Select Analyze $\diamond$ Correlate $\diamond$ Bivariate... (see figure, below).

| Statistics Data Editor |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| prm | Analyze | Direct Marketing | Graphs | $\underline{\text { Utilities }}$ | Add-ons |
| $\square$ | Reports <br> Descriptive Statistics <br> Tables |  | $\downarrow$ | 8\% |  |
|  |  |  | - |  |  |
| Pass | com | are Means | - | AR00004 | NumberO |
|  | Gen | ral Linear Model | - | - |  |
|  | Gen | ralized Linear Models | - | - |  |
|  | Mixe | Models | - |  |  |
|  | Corr | late | - | [12 Bivaria | te... |
|  |  | ssion | - | Prartial |  |
|  |  | near | - | 8 Distan | ces... |
|  |  | Networks | - |  |  |
|  |  | ify | - | - - |  |
|  |  | nsion Reduction | - | - |  |
|  |  |  | - | - |  |
|  |  | arametric Tests | - | - |  |
|  |  | asting | - | - |  |
|  |  |  | - | . |  |
|  |  | le Response | - | . |  |
|  | -3 Miss | g Value Analysis... |  | . |  |
|  |  | le Imputation | - | - |  |
|  |  | lex Samples | $\stackrel{ }{ }$ | - |  |
|  | 閊 Sim | ation... |  | - |  |
|  |  | Control | - | - |  |
|  | $\square \mathrm{ROC}$ | Curve... |  | - |  |
|  | 1.00 | 2.00 | - | - |  |
|  | 1.00 | 2.00 | - | - |  |

Select "x" and "y" as the variables, select "Pearson" as the correlation coefficient, and click " "OK" (see the left figure, below).


## 328 stat

## $\Rightarrow$ Correlations

## Correlations

|  | X | Y |  |
| :--- | :--- | ---: | ---: |
| X | Pearson Correlation | 1 | $-.968^{\wedge \pi}$ |
|  | Sig. (2-tailed) |  | .000 |
|  | N | 10 | 10 |
| Y | Pearson Correlation | $-.968^{\pi \kappa}$ | 1 |
|  | Sig. (2-tailed) | .000 |  |
|  | N | 10 | 10 |

**. Correlation is significant at the 0.01 level (2-tailed).

The correlation coefficient is -0.9679 which we can see that the relationship between $x$ and $y$ are $-v e$ and strong.
b, c and d)
Since we eventually want to predict the price of 4 -year-old Corvettes, enter the number " 4 " in the " $x$ " variable column of the data window after the last row. Enter a "." for the corresponding " $y$ " variable value (this lets SPSS know that we want a prediction for this value and not to include the value in any other computations) (see figure, below).


|  | $\times$ | Y |
| :---: | :---: | :---: |
| - | 6.00 | 125.00 |
| - | 6.00 | 115.00 |
| - | 6.00 | 130.00 |
| - | 4.00 | 160.00 |
| - | 2.00 | 219.00 |
| - | 5.00 | 150.00 |
| - | 4.00 | 190.00 |
| - | 5.00 | 163.00 |
| - | 1.00 | 260.00 |
| - | 2.00 | 260.00 |
| - | 4.00 | - |
| - | - | - |
| - | - | - |
|  |  |  |

## 328 stat

Select Analyze $\diamond$ Regression $\diamond$ Linear... (see figure).
Select " y " as the dependent variable and " x " as the independent variable. Click "Statistics", select "Estimates" and "Confidence Intervals" for the regression coefficients, select "Model fit" to obtain $r^{2}$, and click "Continue". Click "Save...", select "Unstandardized" predicted values and click "Continue". Click "OK".


## 328 stat



## 328 stat

## Regression

Model Summary ${ }^{\text {b }}$

| Model | R | R Square | Adjusted R <br> Square | Std. Error of <br> the Estimate |
| :--- | :---: | :---: | :---: | :---: |
| 1 | $.968^{\mathrm{a}}$ | .937 | .929 | 14.24653 |

a. Predictors: (Constant), X
b. Dependent Variable: $Y$

| Model |  | Sum of Squares | df | Mean Square | F | Sig. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Regression | 24057.891 | 1 | 24057.891 | 118.533 | . $000{ }^{\text {b }}$ |
|  | Residual | 1623.709 | 8 | 202.964 |  |  |
|  | Total | 25681.600 | 9 |  |  |  |

a. Dependent Variable: $Y$
b. Predictors: (Constant), X

| Model |  | Unstandardized Coefficients |  | Standardized Coefficients Beta | t | Sig. | 95.0\% Confidence Interval for B |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | B | Std. Error |  |  |  | Lower Bound | Upper Bound |
| 1 | (Constant) | 291.602 | 11.433 |  | 25.506 | . 000 | 265.238 | 317.966 |
|  | X | -27.903 | 2.563 | -. 968 | -10.887 | . 000 | -33.813 | -21.993 |

a. Dependent Variable: $Y$


From above, the regression equation is: $\mathrm{y}=29160.1942-(2790.2913)(\mathrm{x})$.
The coefficient of determination is 0.9368 ; therefore, about $93.68 \%$ of the variation in y data is explained by x .

R

## 328 stat

Q1)
i- $\binom{150}{30}, \Gamma(18), \ln (14), \log (17)$
ii- $P(2<X \leq 4) \quad$ when $\quad X \sim$ Poisson(3)
iii- Write R loop and the results to calculate

$$
f(z)=\frac{1}{\sqrt{2 \pi}} e^{-\frac{z^{2}}{2}}, z=-3.1,-3.0, \ldots-0.1,0,0.1, \ldots 3.0,3.1 .
$$

iv- Write R code and the results to calculate:

$$
\Phi(z)=\int_{-\infty}^{=} \frac{1}{\sqrt{2 \pi}} e^{\frac{t^{2}}{2}} d t, z=-3,-2,-1,0,1,2,3 .
$$

v - Write loop structure in R for generating 5 samples each of size 100 from Binomial $(5,0.7)$. Then calculate the mean, standard deviation and coefficient of variation for each sample.

Q2)
(a) Write the commends and results to calculate the following:
(i) $P(-1.0<T<1.5), \quad v=10$,
(ii) Find $k$ such that $P(T<k)=0.025, \nu=12$,
(iii) $\binom{15}{9}, \quad \log _{10}(25), 28!$

(b) Generate a random sample of size 12 from the exponential (3) distribution and save it to A. Next, write an $R$
command to create the column B such that

$$
B_{i}=\left\{\begin{array}{ll}
1, & A_{i} \leq 3 \\
2, & A_{i}>3
\end{array}, \quad i=1,2, \ldots, 12 .\right.
$$

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Q3)
(a) Find $k$ when $P(X>k)=0.04, \quad X-F(12,10)$

$$
\begin{aligned}
& \Rightarrow 1-P(x<k)=.04 \\
& \Rightarrow 1-04=P(x<k)
\end{aligned}
$$

(b) $P(3<X \leq 7)$ when $X$-Poisso n(3)

Peta'dis.


$$
=\frac{1}{\operatorname{Beta}(6,5)}
$$

(e) $\int_{0}^{1} x^{5}[1-x]^{4} d x \quad f(x)=\frac{\sqrt{6+5}}{\sqrt{6} \sqrt{5}} x^{6-1}(1-x)^{5-1}, 0 \lll 1$

Q4)

$$
A=\left[\begin{array}{cccc}
1 & 6 & 3 & -1 \\
5 & 2 & 7 & 4
\end{array}\right], B=\left[\begin{array}{ccc}
1 & 9 & 8 \\
7 & 4 & 2 \\
5 & 1 & 5 \\
1 & 1 & 9
\end{array}\right], C=\left[\begin{array}{llll}
3 & 4 & 2 & 7 \\
4 & 9 & 0 & 6 \\
3 & 8 & 3 & 2 \\
3 & 4 & 6 & 2
\end{array}\right]
$$

(a) $A * B$
(b) Determinant of C
(c) Inverse of C
(\#) The following data are two independent random samples from two independent populations $A \sim\left(\mu_{A}, \sigma^{2}\right)$ and $B \sim\left(\mu_{B}, \sigma^{2}\right)$, respectively.

$$
\begin{array}{llllllllll}
\text { A: } & 48 & 39 & 42 & 52 & 40 & 48 & 52 & 52 & 54 \\
48 \\
\text { B: } & 50 & 48 & 42 & 40 & 43 & 48 & 50 & 46 & 38 \\
38
\end{array}
$$

Write R command and the results to
i- Test whether $\mu_{A}>\mu_{B}$.
ii- Construct $90 \%$ confidence interval of the difference $\mu_{B}-\mu_{A}$.

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Q5)
(a) Write the command and result to calculate the following:
$\log (80)=$
$18=$
$\ln (40)=$


40 ! $=$
$\binom{50}{15}=$
$P(X>2.22)$, where $X \sim N(2,5)$
$\Rightarrow \quad 1-P(X<2.22)$
(b) Write the commands and results to find the determent of the matrix and its inverse

Se $\left[\begin{array}{llll}1 & 0 & 4 & 7 \\ 8 & 3 & 1 & 9 \\ 7 & 4 & 2 & 8 \\ 0 & 9 & 5 & 6\end{array}\right]$

## 328 stat

```
###Q1
##i
    choose (150,30)
    gamma(18)
    log(14); log(14,base=exp (1))
    log(17,base=10); log10(17)
##ii
    ppois(4,lambda=3) -ppois(2,lambda=3)
##iii
    z <- seq(-3.1,3.1,by=.1)
    z
    for(i in z) {
    a=dnorm(i, mean = 0, sd = 1)
    cat(i," ",a,"\n")
    }
#or
    for(i in z) {
    a=dnorm(i, mean = 0, sd = 1)
    print(c(i,a))
    }
##vi
    z<- seq(-3,3,by=1)
    z
    for(i in z) {
    b=pnorm(i, mean = 0, sd = 1)
    cat(i," ",b,"\n")
    }
#or
    for(i in z) {
    b=pnorm(i, mean = 0, sd = 1)
    print(c(i,b))
    }
##v
    generating <- seq(1,5,by=1)
    generating
    generating <- c(1,2,3,4,5)
    generating
    for(i in generating) {
    c=rbinom(100, size=5, prob=.7)
    d <- mean(c)
    e <- sd(c)
    f<- e/d
    cat("sample:",c," ","mean=",d," ","sd=",e," ","cv=",f,"\n")
    }
#or
    for(i in generating) {
    c=rbinom(n=100, size=5, prob=.7)
    d <- mean(c)
    e <- sd(c)
    f <- e/d
    print(c(c,d,e,f))
    }
```


## 328 stat

```
###Q2
##ai
    pt(1.5,df=10) -pt(-1,df=10)
##aii
    k=qt (.025, df=12)
    k
```

\#\#aiii
choose $(15,9)$
$\log (25$, base $=10) ; \log 10(25)$
factorial(28)
\#\#b
A <- rexp (12, rate=3)
A
for(i in A) \{
if(i<=3) print(1) else print(2)
\}
\#or
B <- vector(mode = "numeric")
j <-0
for(i in A)
j <- j+1
if(i<=3) $B[j]=1$ else $B[j]=2$
\}
B
\#\#\#Q3
\#\#a
$\mathrm{k}=\mathrm{qf}(1-.04, \mathrm{df} 1=12, \mathrm{df} 2=10)$
k
\#\#c
f <- function(x) \{ ( $\left.x^{\wedge} 5\right)^{*}\left((1-x)^{\wedge} 4\right)$ \}
i <- integrate (f,lower=0, upper=1) \$value
i
\#or
f <- function(x) \{ dbeta(x, shape1=6, shape2=5) * (beta (6,5)) \}
i <- integrate (f,lower=0, upper=1) \$value
i
*
\#\#Q4
a <- $c(1,6,3,-1,5,2,7,4)$
$\mathrm{A}<-$ matrix $(\mathrm{a}$, nrow $=2$, ncol $=4$, byrow=T)
A
b <- c(1, 9, 8, 7, 4, 2, 5, 1, 5, 1, 1, 9)
B <- matrix (b, nrow $=4$, ncol $=3$, byrow $=T$ )
B
c <- c $(3,4,2,7,4,9,0,6,3,8,3,2,3,4,6,2)$
$C<-$ matrix (c,nrow $=4$, ncol $=4$, byrow $=T$ )
C
\#\#a
A왕*옹
\#\#b
$\operatorname{det}(C)$
\#\#c
solve (C)

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```
##d
    A<- c(48,39,42,52,40,48,52,52,54,48)
    A
    B<- c(50,48,42,40,43,48,50,46,38,38)
    B
#or
```



```
    data <- read.csv("data.csv",header=T, sep=";")
        data
        A <- data$A
        A
        B <- data$B
    B
##di
        t.test (A,B,alternative = "greater", paired = FALSE, var.equal = T, conf.level = 0.95)
    ##dii
        t.test(B,A,alternative = "two.sided", paired = FALSE, var.equal = T, conf.level = 0.90)
    ###05
        1-pnorm(2.22, mean = 2, sd = sqrt (5))
```

+ See Appendix -3-


[^0]:    Notes

    ## p-value

    (1) $H_{1}: \theta \neq \theta_{0} \rightarrow p-$ value $_{\text {two tail }}=2 P($ distribution oftest statistical $>\mid$ test statistical $)$
    (2) $H_{1}: \theta>\theta_{0} \rightarrow p-$ value $_{\text {one tail }(>)}=P($ distribution oftest statistical $>$ test statistical $)$
    (3) $H_{1}: \theta<\theta_{0} \rightarrow p-$ value $_{\text {one tail (<) }}=P$ (distribution oftest statistical $<$ test statistical $)$

