

King Saud University

College of Engineering

IE – 341: “Human Factors”

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Chapter 3. Information Input and Processing

Part – I\*

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# Chapter Overview

- Information:
  - How it can be measured (part I)
  - How it can be displayed (part II)
  - How it can be coded (part II)

# Information Theory

- Information Processing is AKA:
  - Cognitive Psychology
  - Cognitive Engineering
  - Engineering Psychology
- Objectives of Information Theory:
  - Finding an operational definition of information
  - Finding a method for measuring information
  - Note, most concepts of Info. Theory are descriptive (i.e. **qualitative** vs. **quantitative**)
- Information (Def<sup>n</sup>):
  - "Reduction of Uncertainty"
  - Emphasis is on "highly unlikely" events
  - Example (information in car):
    - "Fasten seat belt": likely event ⇒ not imp. in Info. Th.
    - "Temperature warning": unlikely event ⇒ imp.

# Unit of Measure of Information

- Case 1:  $\geq 1$  equally likely alternative events:

$$H = \log_2 N = \frac{\log N}{\log 2}$$

- $H$ : amount of information [**Bits**]
- $N$ : number of equally likely alternatives
- e.g.: 2 equally likely alternatives  $\Rightarrow H = \log_2 2 = 1$   
 $\Rightarrow$  **Bit** (Def<sup>n</sup>): "amount of info. to decide between **two** equally likely (i.e. 50%-50%) alternatives"
- e.g.: 4 equally likely alternatives  $\Rightarrow H = \log_2 4 = 2$
- e.g.: equally likely digits (0-9)  $\Rightarrow H = \log_2 10 = 3.32$
- e.g.: equally likely letters (a-z)  $\Rightarrow H = \log_2 26 = 4.70$
- Note, for each of above, unit [bit] must be stated. •<sub>4</sub>

## Cont. Unit of Measure of Information

- Case 2:  $\geq 1$  non-equally likely alternatives:

$$h_i = \log_2 \frac{1}{p_i}$$

- $h_i$  : amount of information [Bits] for single event,  $i$
- $p_i$  : probability of occurrence of single event,  $i$
- Note, this is not usually significant  
(i.e. for individual event basis)

## Cont. Unit of Measure of Information

- Case 3: Average info. of non-equally likely series of events:

$$H_{av} = \sum_{i=1}^N p_i \left( \log_2 \frac{1}{p_i} \right)$$

◦  $H_{av}$ : average information [Bits] from all events

◦  $p_i$ : probability of occurrence of single event,  $i$

◦  $N$ : num. of non-equally likely alternatives/events

◦ e.g.: 2 alternatives ( $N = 2$ )

- Enemy attacks by land,  $p_1 = 0.9$

- Enemy attacks by sea,  $p_2 = 0.1$

- $\Rightarrow H_{av} = \sum_{i=1}^2 p_i \left( \log_2 \frac{1}{p_i} \right) = p_1 \left( \log_2 \frac{1}{p_1} \right) + p_2 \left( \log_2 \frac{1}{p_2} \right)$   
 $= 0.9 \left( \log_2 \frac{1}{0.9} \right) + 0.1 \left( \log_2 \frac{1}{0.1} \right) = 0.47$

# Cont. Unit of Measure of Information

- Case 4: **Redundancy**:
  - If 2 occurrences: equally likely  $\Rightarrow$ 
    - $p_1 = p_2 = 0.5$  (i.e. 50 % each)
    - $\Rightarrow H = H_{\max} = 1$
  - In e.g. in last slide, departure from max. info.
    - $= 1 - 0.47 = 0.53 = 53\%$
  - ***% Redundancy*** =  $\left(1 - \frac{H_{av}}{H_{max}}\right) * 100$
  - Note, as departure from equal prob.  $\uparrow \Rightarrow$  %Red.  $\uparrow$
  - e.g.: not all English letters equally likely: "th", "qu"
    - $\Rightarrow$  %Red. of English language = 68 %
    - PS. How about Arabic language?

# Choice Reaction Time Experiments

- Experiments:
  - Subjects: exposed to different **stimuli**
  - **Response** time is measured
  - e.g. 4 lights – 4 buttons
- *Hick* (1952):
  - Varied number of stimuli (eq. likely alternatives)
  - He found:
    - As # of eq. likely alt.  $\uparrow \Rightarrow$  reaction time to stimulus  $\uparrow$
    - Reaction time vs. Stimulus (in Bits): **linear function**
- *Hyman* (1953):
  - Kept number of stimuli (alternatives) fixed
  - Varied prob. of occurrence of events  $\Rightarrow$  info. Varies
  - He found: “**Hick-Hyman Law**”
    - AGAIN: Reaction time vs. Stimulus (in Bits): linear function! 8