

Student's Name	Student's ID	Group No.	Lecturer's Name

Question No.	Ι	II	III	IV	Total
Mark					

[I] Determine whether the following is **True** or **False**. Justify your answer.

(1) The following system has infinitely many solutions

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$$\begin{aligned} x - 3y - 2z &= 0\\ -x + 2y + z &= 0\\ 2x + 4y + 6z &= 0 \end{aligned}$$

(2) For $A = [a_{ij}]_{n \times n}$, if $A^2 = 0_{n \times n}$ then $A = 0_{n \times n}$

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(3) There is a lower triangular matrix A for which $A^2 = \begin{bmatrix} 4 & 0 \\ 9 & 1 \end{bmatrix}$ ()

(4) The matrix
$$\begin{bmatrix} 0 & 1 & 0 \\ 1 & 0 & 0 \\ -1 & 0 & 1 \end{bmatrix}$$
 is elementary ()

[II] Choose the correct answer.

(1)
$$\begin{vmatrix} 5 & 2 & 2 \\ -1 & 1 & 2 \\ 3 & 0 & 0 \end{vmatrix}$$
 equals
(a) -18 (b) 6 (c) -6 (d) None
(2) If $A = \begin{bmatrix} t & 0 \\ 0 & t \end{bmatrix}$ where t is a nonzero constant, then
(a) A commutes with every 2 × 2 matrix (b) The system $A\mathbf{x} = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$ is inconsistent (c) $tr(A) = t^2$ (d) None
(3) The values of k for which the matrix $A = \begin{bmatrix} k & -k & 3 \\ 0 & k+1 & 1 \\ k & -8 & k-1 \end{bmatrix}$ is singular are
(a) $k = 0, 1$ (b) $k = 1, 2$ (c) $k = 0, 2$ (d) None

(4) (a) (b) (c) (d) None

[III] Solve the following matrix equations for X where $A = \begin{bmatrix} -1 \\ 2 \end{bmatrix}$, $B = \begin{bmatrix} 4 & 2 \end{bmatrix}$, $C = \begin{bmatrix} 3 & 0 \\ 1 & -2 \end{bmatrix}$ and $D = \begin{bmatrix} 2 & 0 & 0 \\ 1 & 2 & 0 \\ 0 & 1 & 2 \end{bmatrix}$

(a)
$$X - (2AB + C^T)^{-1} = 0_{2 \times 2}$$

(b)
$$DX = \begin{bmatrix} 1 & 0 & -1 \\ 2 & 3 & 0 \end{bmatrix}$$

(1) _____

(2)