King Saud University

College of Engineering

IE – 341: "Human Factors Engineering"

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Chapter 3. Information Input and Processing
Part – 4: Signal Detection Theory

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Chapter Overview
Information Processing and Compatibility

1. Information Display – Coding (Ch. 3)

2. Fitts' Law (Ch. 3, Ch. 9)

3. Hick Hyman Law (Ch. 3)

4. Signal Detection Theory (Ch. 3)

5. Memory - Attention (Ch. 3)

6. Compatibility - Part 1 - Spatial Compatibility (Ch. 10)

7. Compatibility - Part 2 - Movement - Modality Compatibility (Ch. 10, Ch.3)
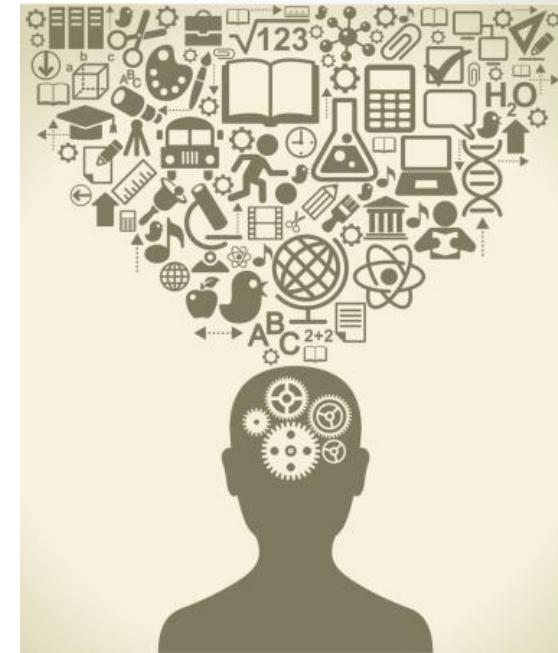
Contents

- Signal Detection Theory

Signal Detection Theory

Signal Detection Theory

- Overview of Signal Detection Theory (SDT)
  - What is Signal Detection Theory (1954)?
    - theory predicting how/when we detect:
    - the presence of a faint stimulus ("**signal**"),
    - in the presence of background stimulation ("**noise**")
    - i.e. no single absolute threshold for a signal
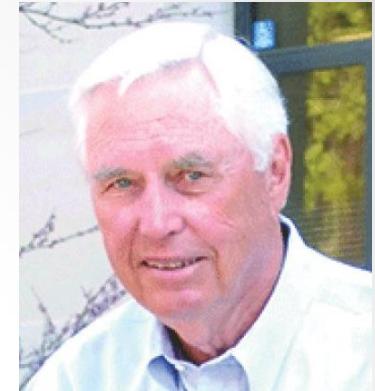
  - Involves situations where:
    - Two discrete situations exist: signal / no signal
    - Situations cannot be easily discriminated

  - Examples:
    - Detecting cavity on tooth x-ray
    - Detecting defective component in a factory
    - Detecting rain in weather forecast

John A. Swets
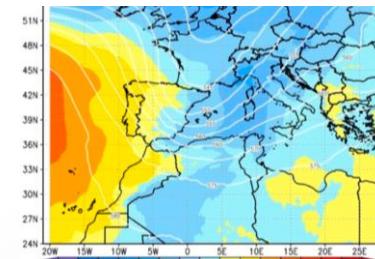
Signal Detection Theory

- Concepts Associated with SDT:
1. Concept of noise
2. Possible outcomes
3. Concept of response criterion
4. Influencing the response criterion
5. Concept of sensitivity
6. Applications of SDT

Cont. Signal Detection Theory

1. Concept of Noise
   o Nature of Noise:
     • Involved with any situation
     • Interferes with detection of signal

   o Noise is generated:
     • Externally (e.g. false radar return on radar screen)
     • Internally: within person (e.g. miscellaneous neural activity)

   o Noise value:
     • Intensity varies from low to high with time
     • Forms normal (bell-shaped) distribution

   o When "signal" occurs:
     • Intensity is added to background noise
     • Person must decide if input
       (what s/he senses) consists of:
         o Only noise, or
         o Noise + signal

$$y = \frac{1}{\sigma\sqrt{2\pi}}\, e^{-\frac{x^2}{2\sigma^2}}$$
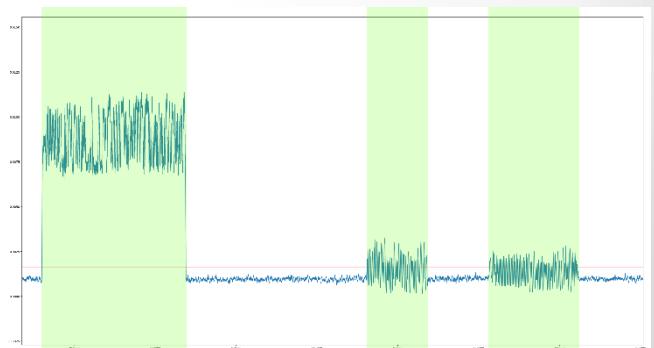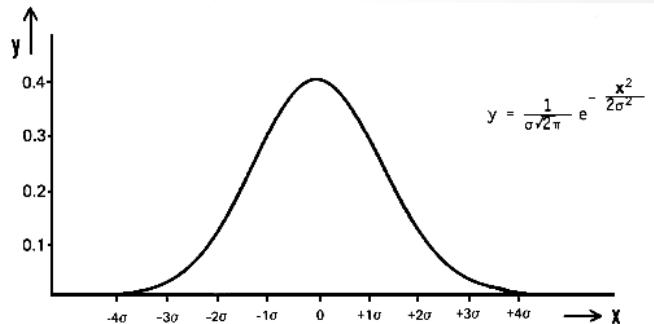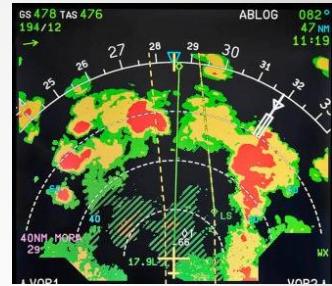
Cont. Signal Detection Theory

2. Possible Outcomes

o First note the following:

- Person must decide: signal occurred / did not occur (2 possibilities)
- There are two realities: signal *did* occur / *did not* occur

o Thus, there are four possible outcomes:

- *Hit* (aka true positive):
  saying "signal" where there is signal
- *False Alarm* (FA, aka false positive):
  saying "signal"/there's no signal
- *Miss* (aka false negative):
  saying "no signal" / there is signal
- *Correct Rejection* (*CR,* aka true negative):
  saying "no signal" / there's no signal

Response	Signal	
	Yes	**No**
Yes	s / y	s / n
No	ns / y	ns / n

⇓

Response	Signal	
	Yes	**No**
Yes	*HIT*	*FA*
No	*MISS*	*CR*

Cont. Signal Detection Theory

3. Concept of Response Criterion

   o SDT helps with understanding how detection process works

   o Basis of SDT:
   - People set criterion along "hypothetical continuum of sensory activity"*
   - People then use this as a basis for making their decisions
   - We then find out position of criterion along continuum
   - This determines probability of four outcomes (*last slide*)
   - This process is illustrated in next slide (Figure 3-3)
   - Try also this SDT interactive learning tool:
     https://eshedmargalit.com/dprime_calculator/

   o Notes regarding Figure 3-3:
   - Figure shows hypothetical distributions of sensory activity in cases:
     o Only noise is present
     o Signal is added to noise
   - The two distributions (noise and signal + noise overlap)
     o $\Rightarrow$ noise level alone may be > signal + noise (in which case?)

Cont. Signal Detection Theory

Signal absent ← → Signal present

Criterion

Correct Rejection

Noise only

Noise + Signal

Hit

Miss

False alarm

Signal Strength
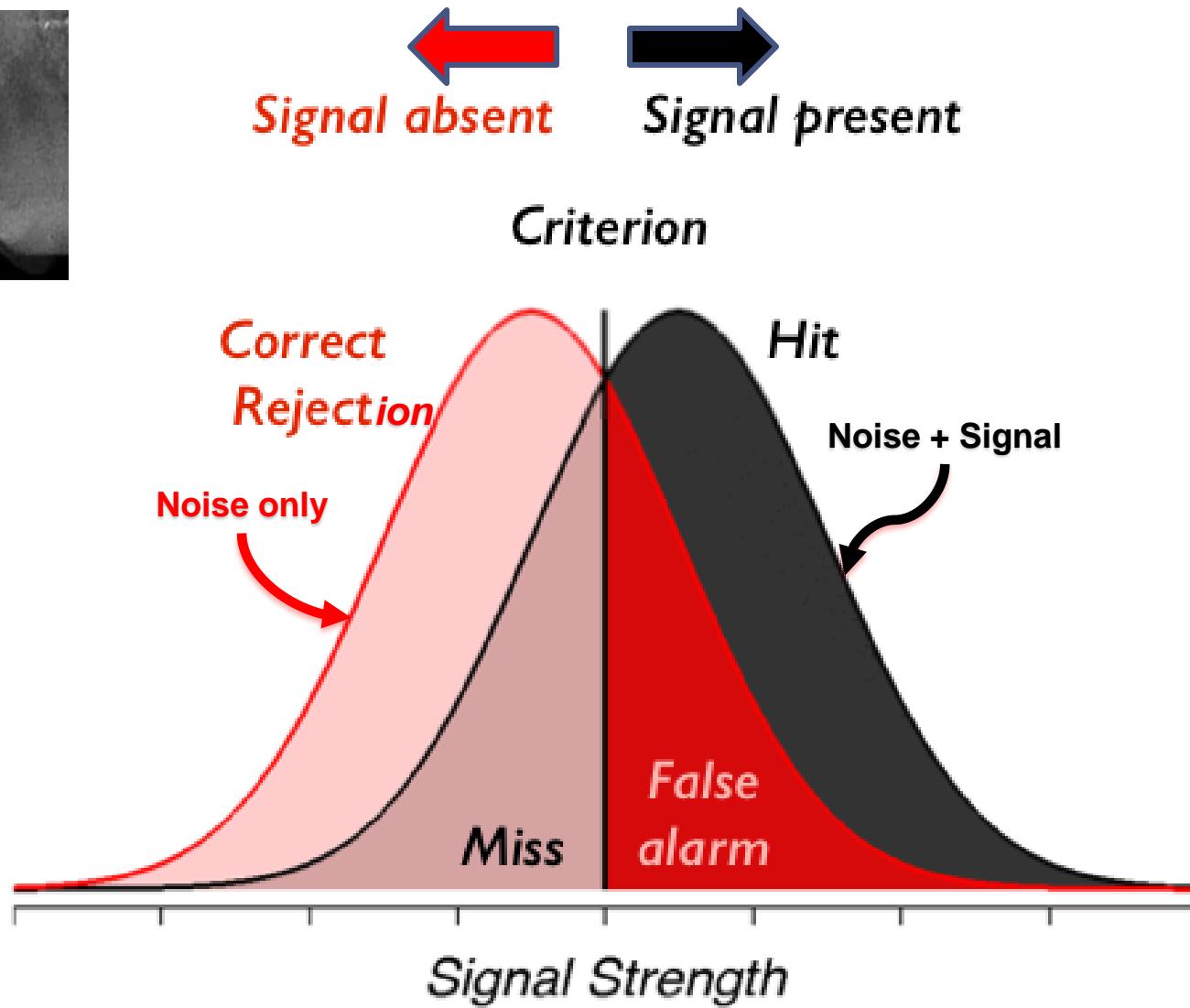
Cont. Signal Detection Theory

FIGURE 3-3

Illustration of the key concepts of signal detection theory. Shown are two hypothetical distributions of internal sensory activity, one generated by noise alone and the other generated by signal plus noise. The probabilities of four possible outcomes are depicted as the respective areas under the curves based on the setting of a criterion at X. Here d' is a measure of sensitivity, and beta is a measure of response bias. The letters a and b correspond to the height of the signal-plus-noise and noise-only distributions at the criterion.
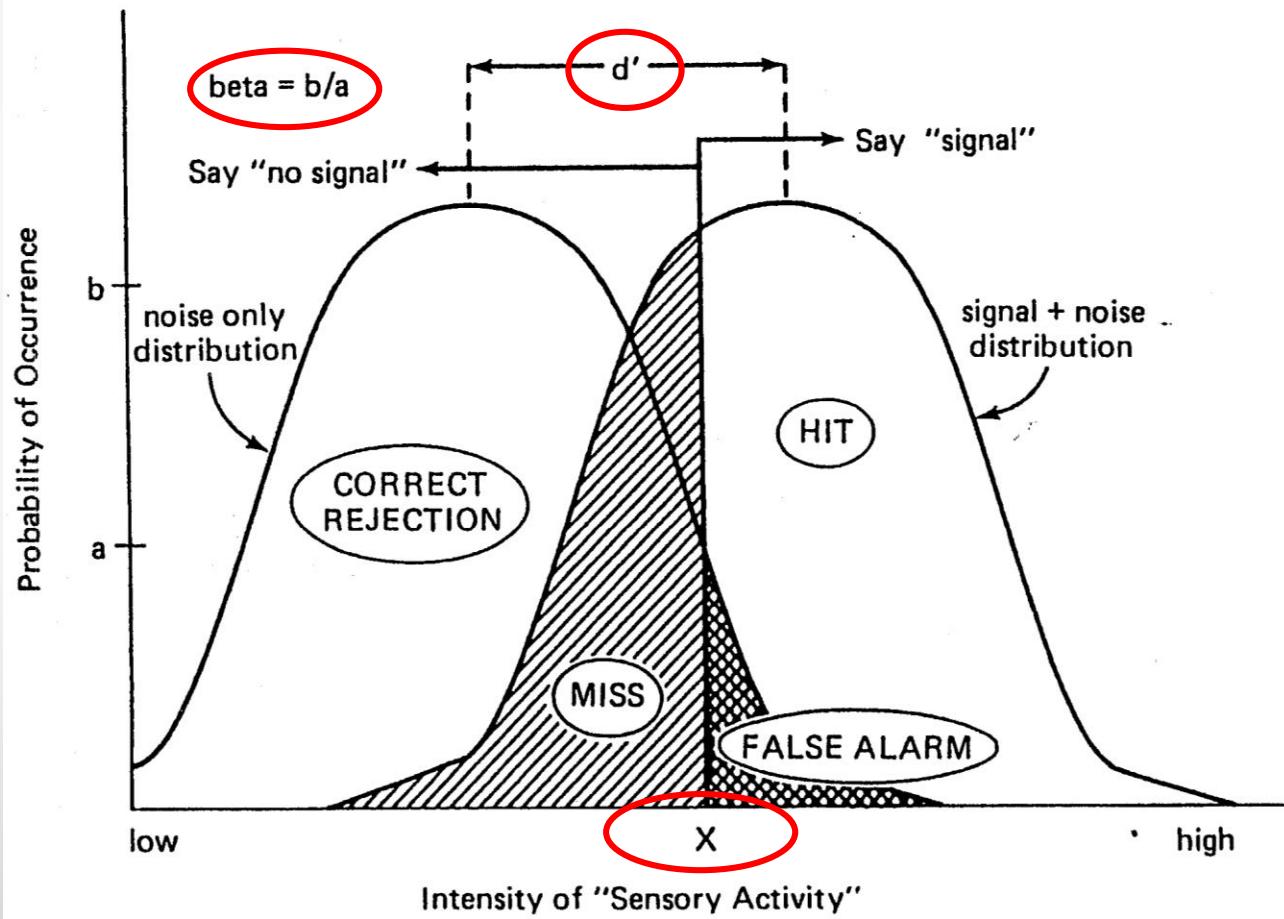
Cont. Signal Detection Theory

3. Cont. Concept of Response Criterion (RC)

o SDT assumes person sets criterion, such that when:

- Level of sensory activity > set criterion $\Rightarrow$ person says: "signal present"
- Level of sensory activity < set criterion $\Rightarrow$ person says: "no signal"
- Probabilities of four outcomes determined based on criterion (*Figure*)

o Quantity "beta" (aka response criterion / response bias)

- Based on position of criterion
- $beta = b / a$
- i.e. beta is ratio of signal : noise, or ratio of height of 2 curves @ criterion
- Values of beta (*see next slide*)
    - o Beta = 1, when two distributions intersect (can you show this?)
    - o When criterion is shifted to right $\Rightarrow$
        - Beta increases (i.e. > 1.0)
        - Person says "signal" less $\Rightarrow$ hits ↓, but also FA ↓
        - Person is considered: "**conservative**"
    - o When criterion is shifted to left $\Rightarrow$
        - Beta decreases (i.e. < 1.0)
        - Person says "signal" more $\Rightarrow$ hits ↑, but also FA ↑
        - Person is considered: "risky" (aka "**liberal**")*

Cont. Signal Detection Theory

Effect of changing
$beta$ criterion
(constant d')

d' = 1

Hits = 97.5%
False alarms = 84%

Hits = 84%
False alarms = 50%

Hits = 50%
False alarms = 16%
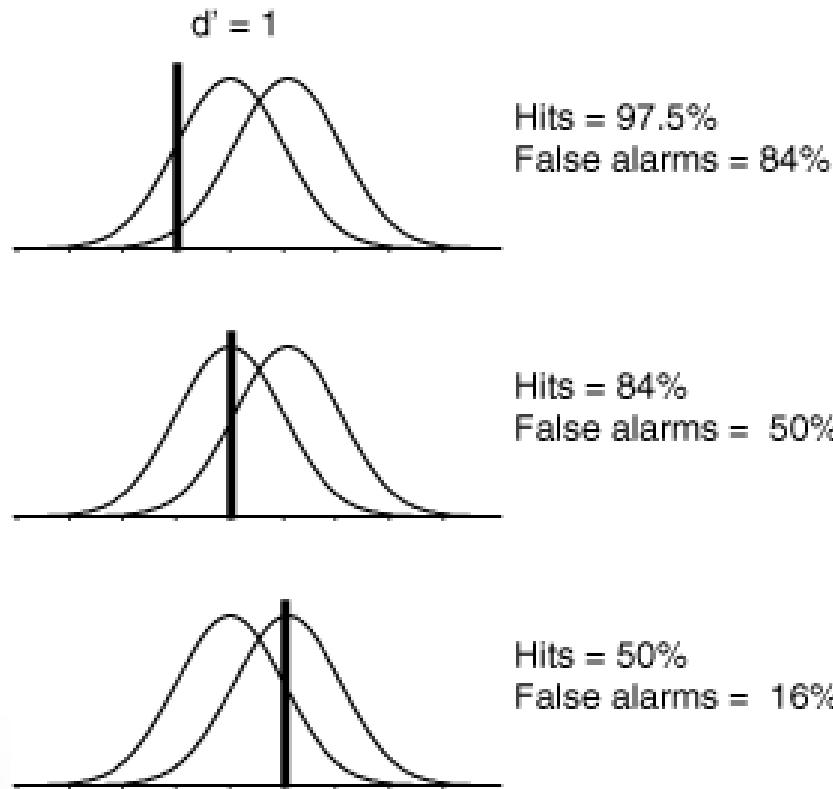
Cont. Signal Detection Theory

4. Influencing the Response Criterion

o Two variables affect setting the criterion

   1. Probability of detecting a signal
   2. Costs and benefits associated with 4 possible outcomes

1. Probability of detecting a signal:
   - e.g. If you told dentist tooth was hurting you $\Rightarrow$
   - Probability that you have cavity ↑
   - $\Rightarrow$ after seeing suspicious spot on x-ray $\Rightarrow$ dentist will likely say: "cavity"
   - $\Rightarrow$ criterion ↓ (i.e. beta ↓) $\Rightarrow$ i.e. dentist can make "risky" assessment

2. Costs and benefits associated with 4 possible outcomes
   - What is cost of *false alarm* (saying "cavity", when there's no cavity)?
     - o $\Rightarrow$ tooth gets drilled without need
   - What is cost of *miss* (saying "no cavity", when there is cavity)?
     - o $\Rightarrow$ cavity worsens $\Rightarrow$ may lose tooth
   - So, what should dentist do? (i.e. after weighing costs?)
     - o Most likely: set low criterion $\Rightarrow$ call suspicious spot: "cavity"
     - o But what if you go regularly? $\Rightarrow$ he will be more conservative (why?)* $\Rightarrow$ will set a high criterion, and will not call it "cavity"

Cont. Signal Detection Theory

5. Concept of Sensitivity

o What is sensitivity? It is keenness / resolution of sensory system

o RC vs. sensitivity in SDT: they are both independent of each other

o How to measure sensitivity (aka: d')
- Sensitivity: d' = separation between 2 distributions (*see Figure 3-3*)
- Measured in units of standard deviation: (aka Z-score or calculator)
- SD's of 2 distributions are assumed equal
- As separation ↑ ⇒ sensitivity ↑ ⇒ d' ↑ (note, best to have high d' *)
- Most applications: $d' = [0.5 - 2]$ (*see next slide*)

o Factors affecting d'
1. Some signal systems have more noise than others, thus:
   - o As noise ↑ ⇒ d' ↓
   - o Also note, as signal ↓ ⇒ d' ↓ (*can you show this on Figure 3-3?*)
2. Ability of people to memorize physical characteristics of signal
   - o Memory aids ⇒ d' ↑
   - o e.g. for dentist: d' ↑ by:
     - Using better x-ray equipment
     - Comparing x-ray of patient with previous x-rays of cavities

Receiver Operating Characteristic

- ## ROC curves

d' = 1 (lots of overlap)

d' = 3 (not much overlap)

Effect of changing _d′_

ROC curves

d'=4
d'=3
d'=2
d'=1
d'=0

Hits
1.0
0.5
0.0

False alarms
0.0   0.5   1.0
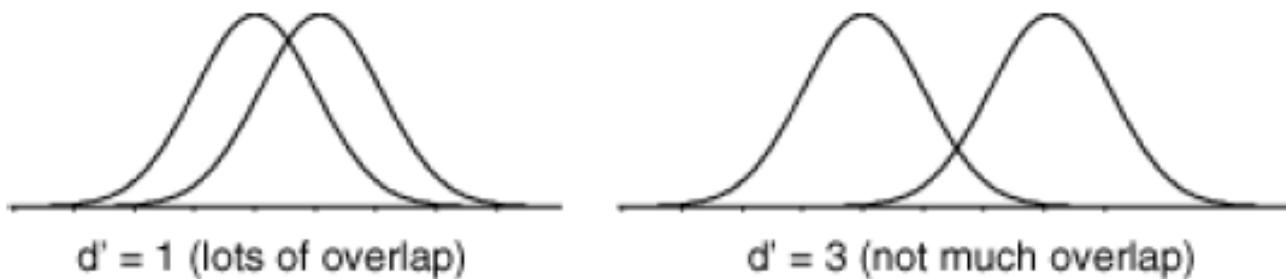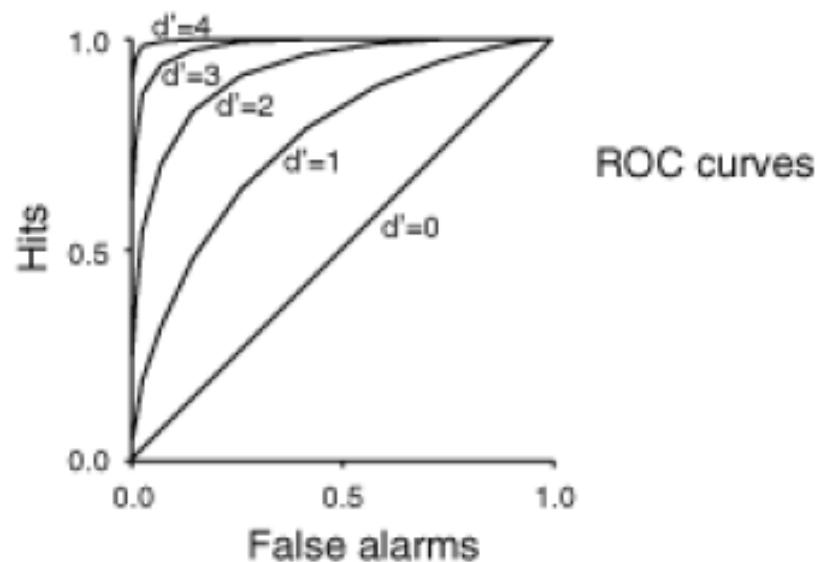
Cont. Signal Detection Theory

6. Applications of SDT

   o Many <u>practical applications</u> (from various studies):

      • Sonar target applications

      • Industrial inspection tasks

      • Medical Diagnosis

      • Forensic science

      • Eye witness testimony

      • Air traffic control

      • Weather forecasting
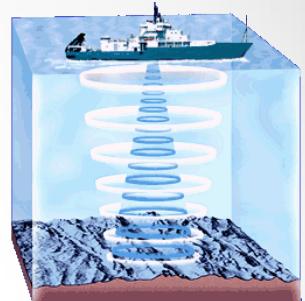
   o Reservations

      • SDT should not be accepted without criticism (use with "grain of salt")

         o Using in some situations may $\Rightarrow$ invalid results

      • Reasons:

         o Theory developed in lab (controlled conditions/experiments)

         o Subjects given many, many trials

         o Controlled signals and background noise levels

         o Some applications don't match these conditions

Table of Standard Normal Probabilities for Negative Z-scores
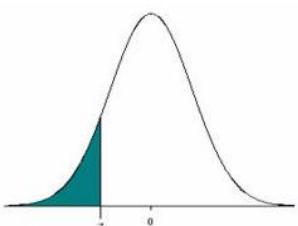
z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
-3.4	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0003	0.0002
-3.3	0.0005	0.0005	0.0005	0.0004	0.0004	0.0004	0.0004	0.0004	0.0004	0.0003
-3.2	0.0007	0.0007	0.0006	0.0006	0.0006	0.0006	0.0006	0.0005	0.0005	0.0005
-3.1	0.0010	0.0009	0.0009	0.0009	0.0008	0.0008	0.0008	0.0008	0.0007	0.0007
-3.0	0.0013	0.0013	0.0013	0.0012	0.0012	0.0011	0.0011	0.0011	0.0010	0.0010
-2.9	0.0019	0.0018	0.0018	0.0017	0.0016	0.0016	0.0015	0.0015	0.0014	0.0014
-2.8	0.0026	0.0025	0.0024	0.0023	0.0023	0.0022	0.0021	0.0021	0.0020	0.0019
-2.7	0.0035	0.0034	0.0033	0.0032	0.0031	0.0030	0.0029	0.0028	0.0027	0.0026
-2.6	0.0047	0.0045	0.0044	0.0043	0.0041	0.0040	0.0039	0.0038	0.0037	0.0036
-2.5	0.0062	0.0060	0.0059	0.0057	0.0055	0.0054	0.0052	0.0051	0.0049	0.0048
-2.4	0.0082	0.0080	0.0078	0.0075	0.0073	0.0071	0.0069	0.0068	0.0066	0.0064
-2.3	0.0107	0.0104	0.0102	0.0099	0.0096	0.0094	0.0091	0.0089	0.0087	0.0084
-2.2	0.0139	0.0136	0.0132	0.0129	0.0125	0.0122	0.0119	0.0116	0.0113	0.0110
-2.1	0.0179	0.0174	0.0170	0.0166	0.0162	0.0158	0.0154	0.0150	0.0146	0.0143
-2.0	0.0228	0.0222	0.0217	0.0212	0.0207	0.0202	0.0197	0.0192	0.0188	0.0183
-1.9	0.0287	0.0281	0.0274	0.0268	0.0262	0.0256	0.0250	0.0244	0.0239	0.0233
-1.8	0.0359	0.0351	0.0344	0.0336	0.0329	0.0322	0.0314	0.0307	0.0301	0.0294
-1.7	0.0446	0.0436	0.0427	0.0418	0.0409	0.0401	0.0392	0.0384	0.0375	0.0367
-1.6	0.0548	0.0537	0.0526	0.0516	0.0505	0.0495	0.0485	0.0475	0.0465	0.0455
-1.5	0.0668	0.0655	0.0643	0.0630	0.0618	0.0606	0.0594	0.0582	0.0571	0.0559
-1.4	0.0808	0.0793	0.0778	0.0764	0.0749	0.0735	0.0721	0.0708	0.0694	0.0681
-1.3	0.0968	0.0951	0.0934	0.0918	0.0901	0.0885	0.0869	0.0853	0.0838	0.0823
-1.2	0.1151	0.1131	0.1112	0.1093	0.1075	0.1056	0.1038	0.1020	0.1003	0.0985
-1.1	0.1357	0.1335	0.1314	0.1292	0.1271	0.1251	0.1230	0.1210	0.1190	0.1170
-1.0	0.1587	0.1562	0.1539	0.1515	0.1492	0.1469	0.1446	0.1423	0.1401	0.1379
-0.9	0.1841	0.1814	0.1788	0.1762	0.1736	0.1711	0.1685	0.1660	0.1635	0.1611
-0.8	0.2119	0.2090	0.2061	0.2033	0.2005	0.1977	0.1949	0.1922	0.1894	0.1867
-0.7	0.2420	0.2389	0.2358	0.2327	0.2296	0.2266	0.2236	0.2206	0.2177	0.2148
-0.6	0.2743	0.2709	0.2676	0.2643	0.2611	0.2578	0.2546	0.2514	0.2483	0.2451
-0.5	0.3085	0.3050	0.3015	0.2981	0.2946	0.2912	0.2877	0.2843	0.2810	0.2776
-0.4	0.3446	0.3409	0.3372	0.3336	0.3300	0.3264	0.3228	0.3192	0.3156	0.3121
-0.3	0.3821	0.3783	0.3745	0.3707	0.3669	0.3632	0.3594	0.3557	0.3520	0.3483
-0.2	0.4207	0.4168	0.4129	0.4090	0.4052	0.4013	0.3974	0.3936	0.3897	0.3859
-0.1	0.4602	0.4562	0.4522	0.4483	0.4443	0.4404	0.4364	0.4325	0.4286	0.4247
-0.0	0.5000	0.4960	0.4920	0.4880	0.4840	0.4801	0.4761	0.4721	0.4681	0.4641

Table of Standard Normal Probabilities for Positive Z-scores
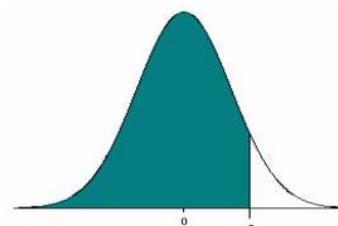
z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
0.7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852
0.8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9772	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9979	0.9980	0.9981
2.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
3.0	0.9987	0.9987	0.9987	0.9988	0.9988	0.9989	0.9989	0.9989	0.9990	0.9990
3.1	0.9990	0.9991	0.9991	0.9991	0.9992	0.9992	0.9992	0.9992	0.9993	0.9993
3.2	0.9993	0.9993	0.9994	0.9994	0.9994	0.9994	0.9994	0.9995	0.9995	0.9995
3.3	0.9995	0.9995	0.9995	0.9996	0.9996	0.9996	0.9996	0.9996	0.9996	0.9997
3.4	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9998

Note that the probabilities given in this table represent the area to the LEFT of the z-score.
The area to the RIGHT of a z-score = 1 − the area to the LEFT of the z-score

Videos

- Watch these videos on Signal Detection Theory:

  - ***Basics and Some Examples***
    https://youtu.be/QjF8QP2bf9Q?si=CdqLE3aHeQyg3vsE

  - ***Basics and Medical Application***:
    https://youtu.be/W3LF0BMNgVI?si=MyLl_mG2yedHxKEY

  - ***How to Calculate the Z-Score***:
    https://youtu.be/558s2nkmdA4?si=E6m1hhhYGr_yWhST

References

o **Human Factors in Engineering and Design**. Mark S. Sanders, Ernest J. McCormick. 7th Ed. McGraw: New York, 1993. ISBN: 0-07-112826-3.

o **An interactive tool for learning about signal detection theory** https://eshedmargalit.com/dprime_calculator/

o **Z-score and Probability Converter**

o **Web Interface for Statistics Education (WISE).** Signal Detection: Overview. http://wise.cgu.edu/wise-tutorials/tutorial-signal-detection-theory/signal-detection-overview-2/