

King Saud University

College of Engineering

IE – 341: “Human Factors Engineering”

Spring – 2024 (2nd Sem. 1445H)

Chapter 3. Information Input and Processing

Part – 3: Choice Reaction Time Experiments

Prepared by: Ahmed M. El-Sherbeeny, PhD

Chapter Overview

Information Processing and Compatibility

1. Information Display – Coding (Ch. 3)
2. Fitts' Law (Ch. 3, Ch. 9)
3. **Hick Hyman Law (Ch. 3)**
4. Signal Detection Theory (Ch. 3)
5. Memory - Attention (Ch. 3)
6. Compatibility - Part 1 - Spatial Compatibility (Ch. 10)
7. Compatibility - Part 2 - Movement - Modality
Compatibility (Ch. 10, Ch.3)



Contents

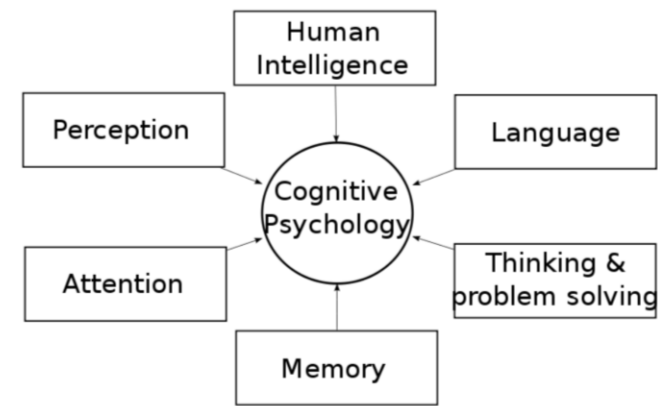
- Information Theory
 - Unit of Measure of Information
- Reaction Time Experiments
 1. Simple reaction time tasks (SRT)
 2. Choice response time tasks (CRT) - Hick's Law
 3. Hick-Hyman Law
- Summary

Information Theory

Information Theory

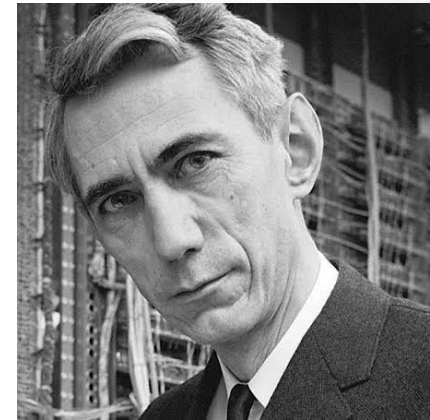
- Information Processing is AKA:

- Cognitive Psychology
- Cognitive Engineering
- Engineering Psychology



- Objectives of Information Theory:

- Finding an operational definition of information (1948)
- Finding a method for measuring information
- Note, most concepts of Info. Theory are descriptive (i.e. **qualitative** vs. **quantitative**)



Claude Shannon

- Information (Definition):

- "Reduction of Uncertainty"
- Emphasis is on "highly unlikely" events
- Example (information in car):
 - "Fasten seat belt": likely event \Rightarrow not imp. in Info. Th.
 - "Temperature warning": unlikely event \Rightarrow imp.



Unit of Measure of Information

- Case 1: ≥ 1 **equally likely alternative events:**

$$H = \log_2 N = \frac{\log N}{\log 2}$$

- H : amount of information [**Bits**]

- N : number of equally likely alternatives

- e.g.: 2 equally likely alternatives $\Rightarrow H = \log_2 2 = 1$
 \Rightarrow **Bit** (Defⁿ): “amount of info. to decide between **two** equally likely (i.e. 50%-50%) alternatives”

- e.g.: 4 equally likely alternatives $\Rightarrow H = \log_2 4 = 2$

- e.g.: equally likely digits (0-9) $\Rightarrow H = \log_2 10 = 3.32$

- e.g.: equally likely letters (a-z) $\Rightarrow H = \log_2 26 = 4.70$

Note, for each of above, unit [bit] must be stated. ●₆

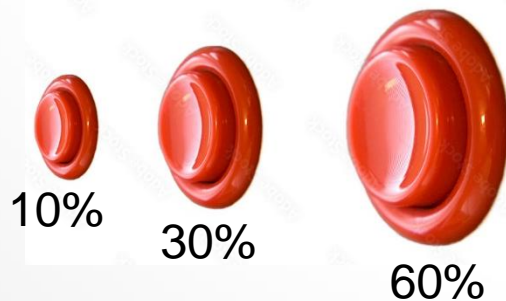


Cont. Unit of Measure of Information

- Case 2: ≥ 1 non-equally likely alternatives:

$$h_i = \log_2 \frac{1}{p_i}$$

- h_i : amount of information [Bits] for single event, i
- p_i : probability of occurrence of single event, i
- Note, this is not usually significant
(i.e. for individual event basis)



Cont. Unit of Measure of Information

- Case 3: **Average info. of non-equally likely series of events:**

$$H_{av} = \sum_{i=1}^N p_i \left(\log_2 \frac{1}{p_i} \right)$$

- H_{av} : average information [Bits] from all events
- p_i : probability of occurrence of single event, i
- N : num. of non-equally likely alternatives/events
- e.g.: 2 alternatives ($N = 2$)

- Enemy attacks by land, $p_1 = 0.9$

- Enemy attacks by sea, $p_2 = 0.1$

- \Rightarrow
$$H_{av} = \sum_{i=1}^2 p_i \left(\log_2 \frac{1}{p_i} \right) = p_1 \left(\log_2 \frac{1}{p_1} \right) + p_2 \left(\log_2 \frac{1}{p_2} \right)$$
$$= 0.9 \left(\log_2 \frac{1}{0.9} \right) + 0.1 \left(\log_2 \frac{1}{0.1} \right) = 0.47$$



Cont. Unit of Measure of Information

- Case 4: **Redundancy**:

- If 2 occurrences: equally likely \Rightarrow

- $p_1 = p_2 = 0.5$ (i.e. 50% each)

- $\Rightarrow H = H_{max} = 1$



- In e.g. in last slide, departure from max. info.

- $= 1 - 0.47 = 0.53 = 53\%$



- $\% \text{ Redundancy} = \left(1 - \frac{H_{av}}{H_{max}} \right) * 100$

- Note, as departure from equal prob. $\uparrow \Rightarrow \% \text{Red.} \uparrow$

- e.g.: not all English letters equally likely: “th”, “qu”

- $\Rightarrow \% \text{Red. of English language} = 68 \%$

- ps. how about Arabic language?

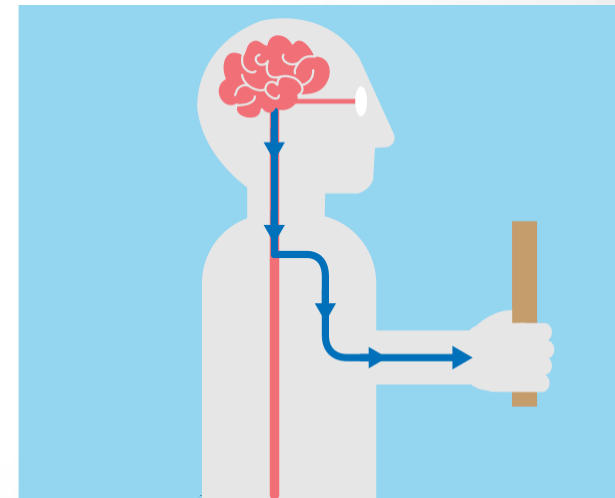
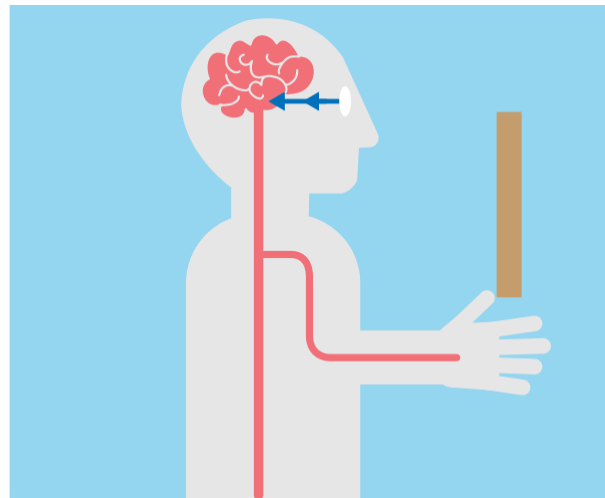
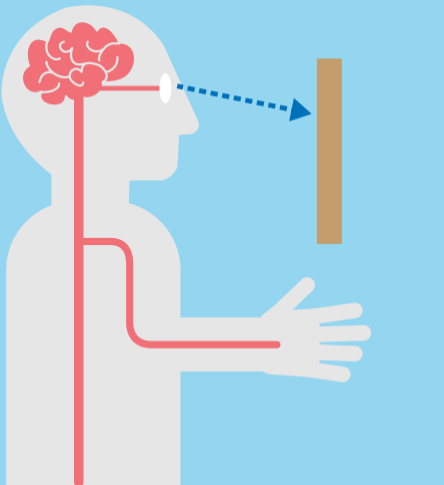
kh-aa	H-aa	j-eem	th-ag	t-aa	b-aa	a-lif
خ	ح	ج	ث	ت	ب	ا
S-aad	sh-een	s-een	z-aa	r-aa	dh-aal	d-aal
ص	ش	س	ز	ر	ذ	د
q-aaf	f-aa	gh-qin	3-ain	Dh-aa	T-aa	D-aad
ق	ف	ع	ع	ظ	ط	ض
y-aa	w-aaw	h-a	n-oon	m-eem	l-aam	k-aaf
ي	و	ه	ن	م	ل	ك



Reaction Time Experiments

Reaction Time Experiments

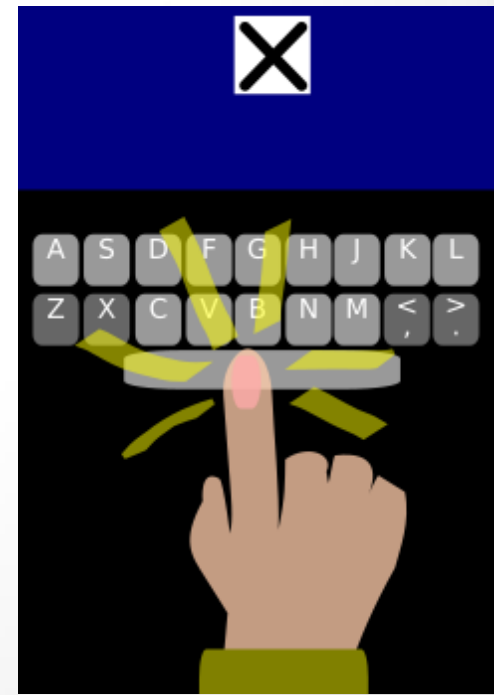
- Important information theory applications:
 1. Simple reaction time tasks (SRT)
 2. Choice response time tasks (CRT) or Hick's Law
 3. Hick-Hyman Law



Cont. Reaction Time Experiments

1. Simple Reaction Time Tasks (SRT)

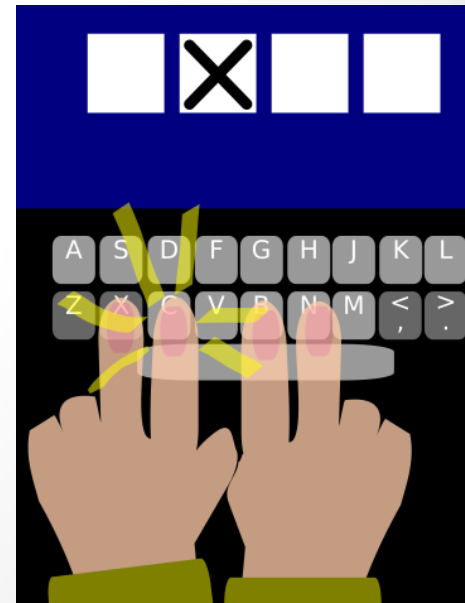
- Used to test how fast human responds in presence of 1 stimulus
- e.g. starting to run when hearing starting gun in a race, or moving car when traffic light is green, etc.
- try experiment (aka *Deary-Liewald task*):
as fast as you see icon on screen, press 'space bar':
- Note, how this tests has two aspects:
 - Correct response rate
 - How fast you respond (*ms*)
- How much did you score?
 - Experiment shows: humans can score for 1 choice: $< 200\text{ ms}$
 - How much do you expect when there is more than one choice?



Cont. Reaction Time Experiments

2. Choice Response Time task (CRT)

- Used to test how fast human responds in presence of *more than 1 stimulus*, i.e. multiple stimuli
- e.g. choosing a digit on keyboard from '0' to '9'
- Each stimulus requires a different response
- In general, more stimuli/responses \Rightarrow slower RT
- try 2nd experiment:
there are now 4 blocks (choices), with 'X' appearing in either of 4 possible positions (i.e. 4 stimuli)
- As fast as you see 'X' come on, press letter on keyboard that corresponds to it
- Note how RT/error rate are now greater



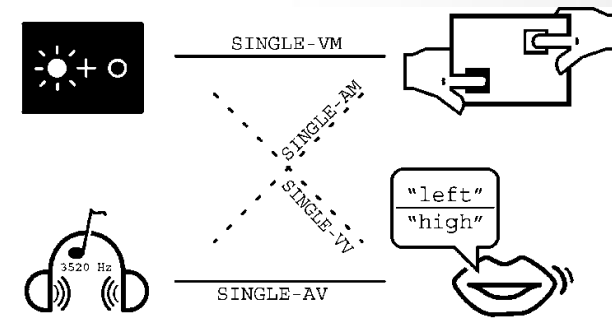
Cont. Reaction Time Experiments

2. Cont. Choice Response Time task (CRT)

- *Simplest* CRT experiment: 2 stimuli/responses \Rightarrow
 - Minimum RT = 250 ms
 - Typical average: 350 – 450 ms
- Note, results greatly affected by type of stimulus & response mode (e.g. verbal/ written/ physical, etc.)*

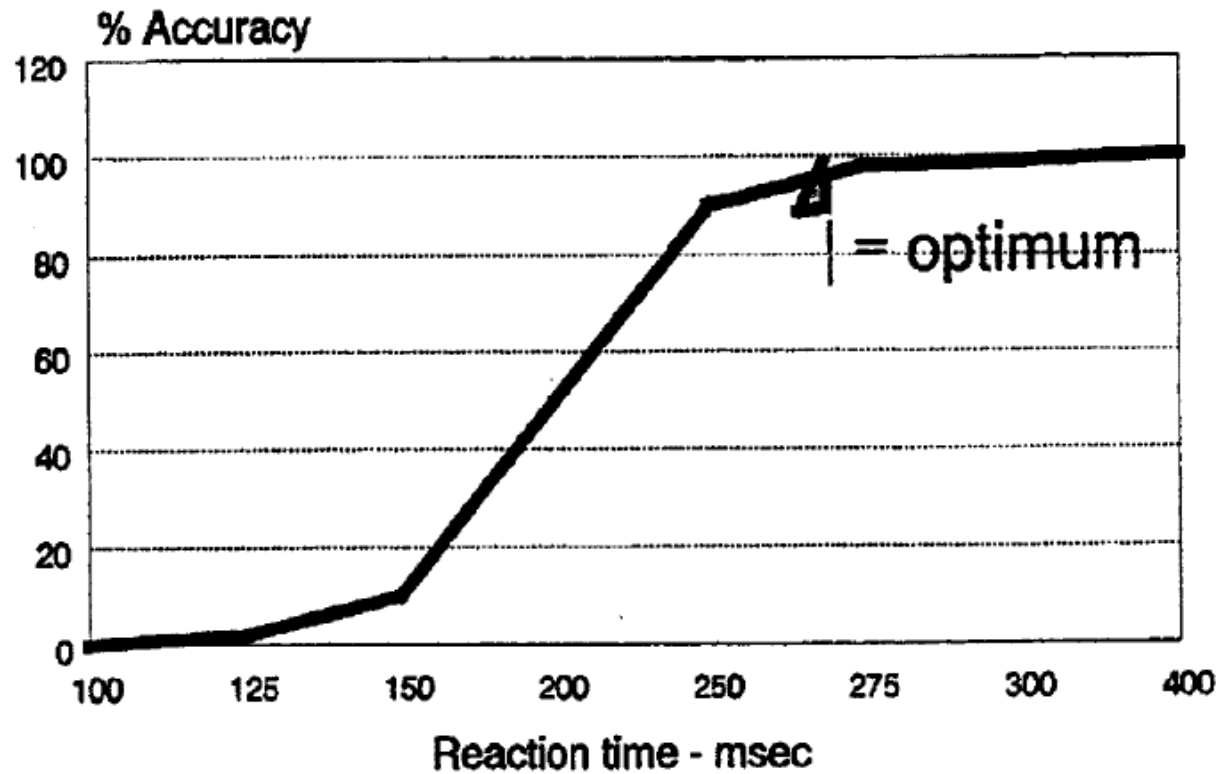
- Also, response speed proven to be affected greatly by:

- Age
- Intelligence
- Conditions (e.g. rested vs. tired, hungry or not, etc.)
- Speed-accuracy tradeoff (i.e. your aim to make less mistakes or higher speed)



Cont. Reaction Time Experiments

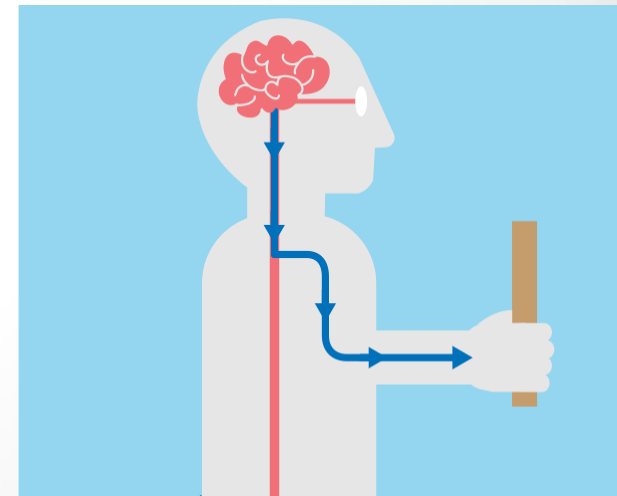
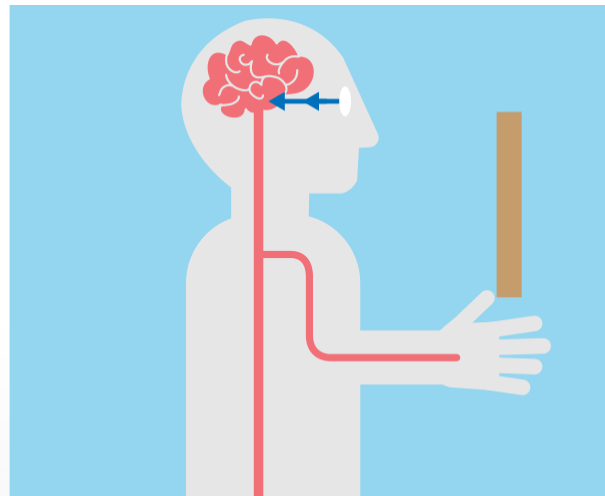
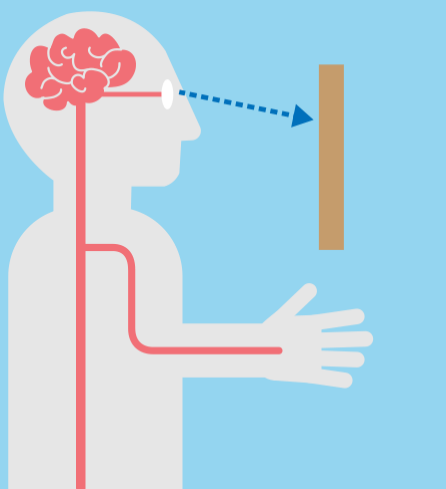
Speed-accuracy tradeoff



Cont. Reaction Time Experiments

2. Cont. Choice Response Time task (CRT)

- So what is significance of measuring CRT?
- RT is indication of time required to
 - Process/interpret information (i.e. stimuli)
 - Retrieve information from memory
 - Initiate muscle responses
 - i.e. gives good indication of time required to “think” (basic thought process)
- This is important part of “cognitive psychology” field



Hick's and Hick-Hyman Laws

3. Hick's Law

- Named after British psychologist *William E. Hick*
- Conducted experiments on CRT in 1950's
- He found (1952):

- Cognitive information capacity: is assessed as rate of gain of information
- As # of equally likely stimuli alternatives \uparrow \Rightarrow RT to stimuli \uparrow logarithmically ([next slide](#))
- i.e. RT vs. # [stimuli in Bits](#): **linear function** (amazing find!)
- Given n equally likely choices, \overline{RT} (T) required to choose among the choices is:

$$T = b \cdot \log_2(n + 1)$$

where,

b : *empirical* constant (determine from data for person)

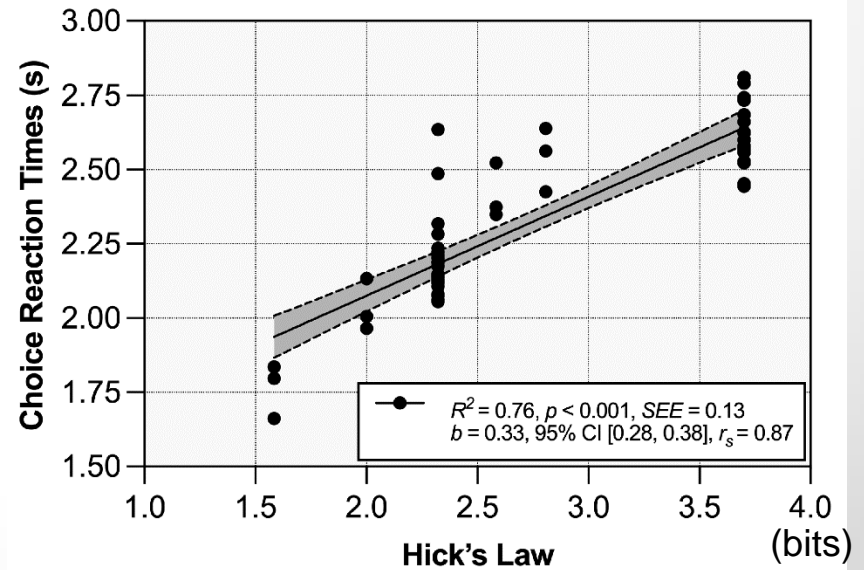
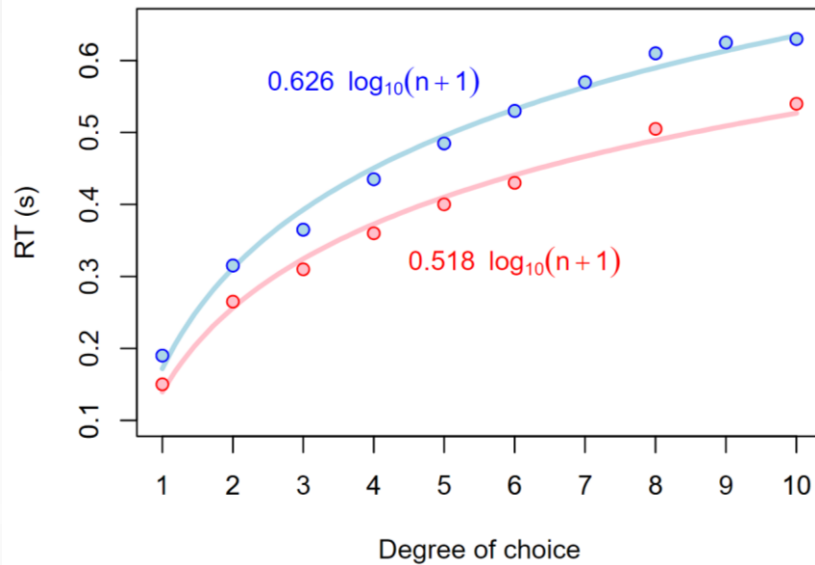
Note how \log_2 indicates how “binary” search is performed

Also, note how “+1” is used to account for 1 choice*



Hick's and Hick-Hyman Laws

3. Cont. Hick's Law



Cont. Choice Reaction Time Experiments

3. Cont. Hick's Law

- More recent research (E. Roth, 1964): RT affected by IQ

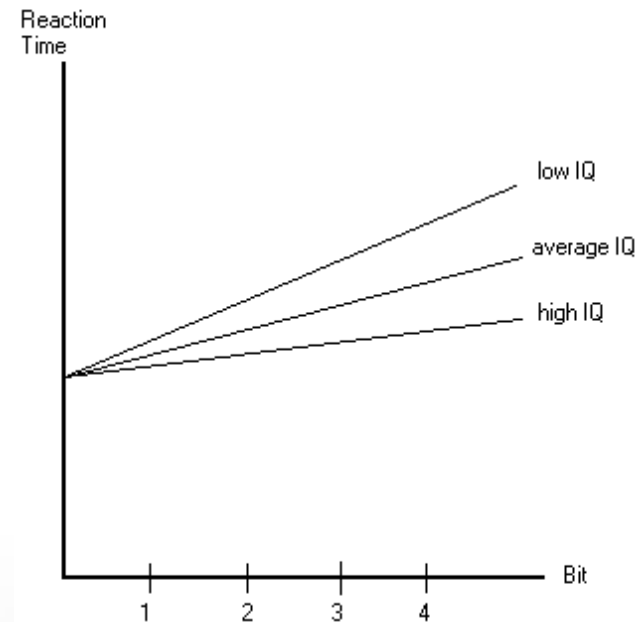
- Time (T) required to make a decision,

$$T = \log_2 n / (\text{Processing Speed})$$



- Example/summary of Hick's law is shown below
- Also, note how this indicates that we don't think equally of all alternatives

(we tend to cancel out $\frac{1}{2}$ alternatives every time we think, as indicated by eqⁿ)



Cont. Choice Reaction Time Experiments

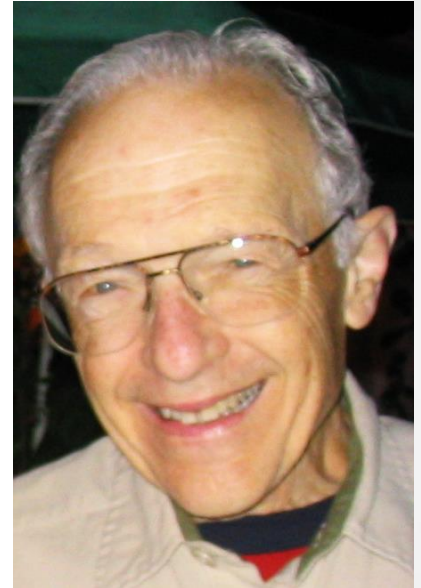
3. Hick-Hyman Law (1953):

- Hick's law further analyzed by US psychologist: *Ray Hyman*
- Kept number of stimuli (alternatives) fixed
- Varied prob. of occurrence of events/choices (e.g. size of targets)
⇒ law is generalized as follows:

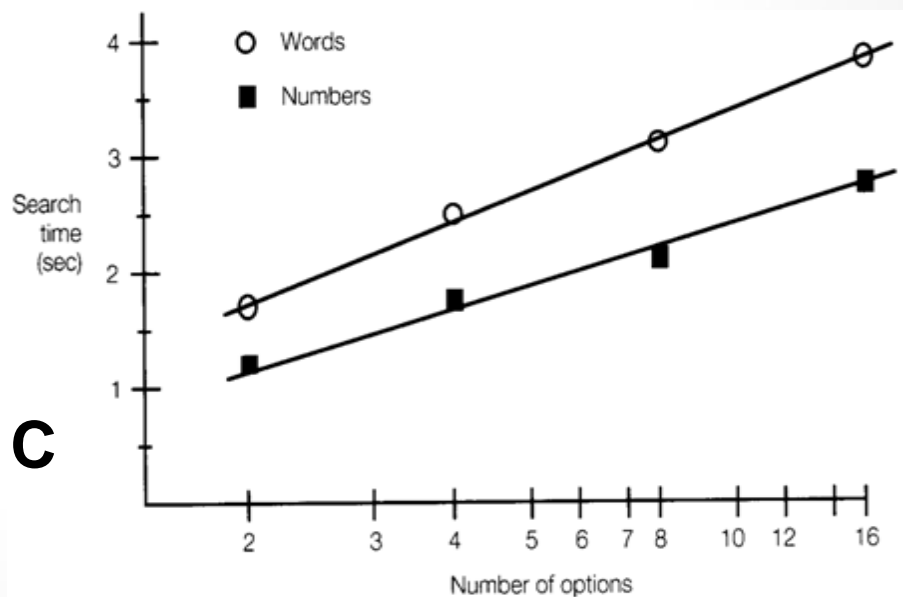
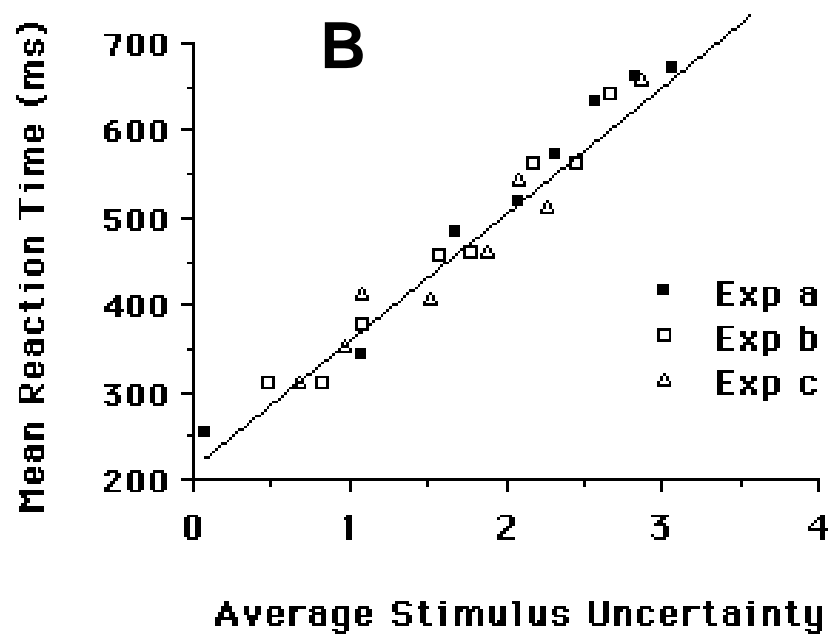
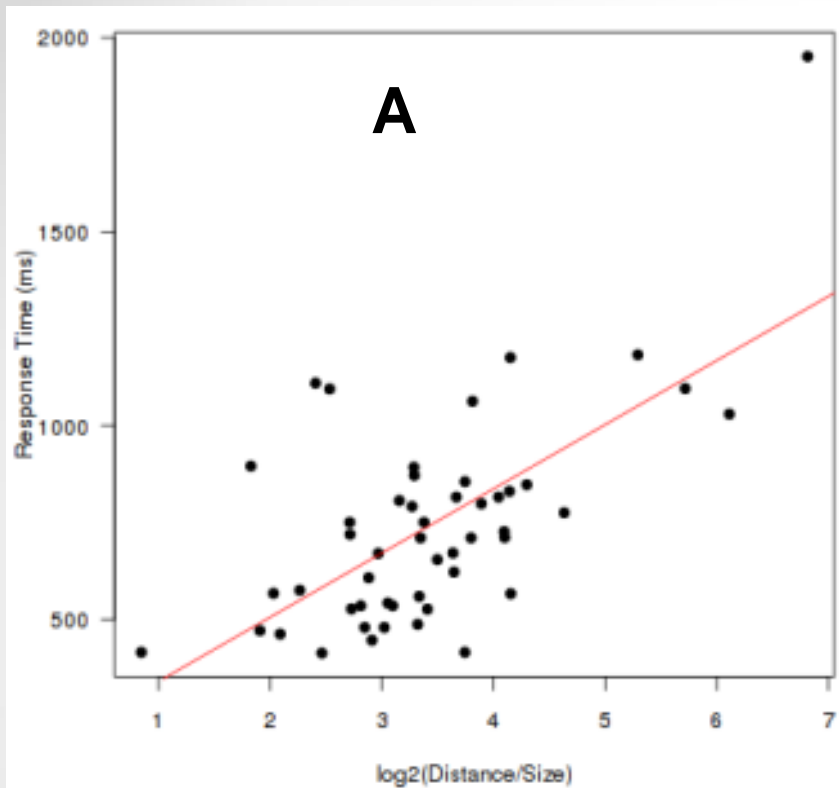
$$T = b \cdot H$$

$$H = \sum_i^n p_i \log_2 \left(\frac{1}{p_i} + 1 \right)$$

- He found: “**Hick-Hyman Law**”
 - AGAIN: Reaction time vs. Stimulus (in Bits): linear function!
- Compare *Hick*, *Hick-Hyman*, *Fitts's Laws* in next slide



SUMMARY



Videos

- Watch the following videos (applications in HCI):
 - **Hick's law:**
<https://youtu.be/ttw5nditisQ?si=BZSRb5LfZyST0anT>
 - **Hick-Hyman Law:**
https://youtu.be/558s2nkmdA4?si=E6m1hhhYGr_yWhST

References

- ***Human Factors in Engineering and Design***. Mark S. Sanders, Ernest J. McCormick. 7th Ed. McGraw: New York, 1993. ISBN: 0-07-112826-3.
- ***Simple and choice reaction time tasks***. From: PsyToolkit. Available at:
http://www.psychtoolkit.org/lessons/simple_choice_rts.html
- For more **simple reaction time tasks**:
<https://www.humanbenchmark.com/tests/reactiontime>
- ***Hick's law***. From Wikipedia, the free encyclopedia. Available at:
https://en.wikipedia.org/w/index.php?title=Hick%27s_law&redirect=no