

Ch10

1) Assume that you have a sample of  $n_1=9$ , with the sample mean  $X_1=45$ , and a sample standard deviation of  $S_1=6$ , and you have an independent sample of  $n_2=12$  from another population with a sample mean of  $X_2=31$  and the sample standard deviation  $S_2=8$ . Complete parts (a) through (d).

a. What is the value of the pooled-variance  $t_{STAT}$  test statistic for testing  $H_0: \mu_1=\mu_2$ ?

$t_{STAT} =$

(Type an integer or a decimal rounded to four decimal places as needed.)

b. In finding the critical value  $t_{\alpha/2}$ , how many degrees of freedom are there?

degrees of freedom

c. Using a significance level of  $\alpha=0.005$ , what is the critical value for a one-tail test of the hypothesis  $H_0: \mu_1 \leq \mu_2$  against the alternative  $H_1: \mu_1 > \mu_2$ ?

The critical value is

(Type an integer or a decimal rounded to four decimal places as needed.)

d. What is your statistical decision?

- A. Reject  $H_0$  because the computed  $t_{STAT}$  test statistic is less than the upper-tail critical value.
- B. Do not reject  $H_0$  because the computed  $t_{STAT}$  test statistic is greater than the upper-tail critical value.
- C. Reject  $H_0$  because the computed  $t_{STAT}$  test statistic is greater than the upper-tail critical value.
- D. Do not reject  $H_0$  because the computed  $t_{STAT}$  test statistic is less than the upper-tail critical value.

2) Assume that you have a sample of  $n_1=8$ , with the sample mean  $X_1=42$ , and a sample standard deviation of  $S_1=4$ , and you have an independent sample of  $n_2=15$  from another population with a sample mean of  $X_2=34$  and a sample standard deviation of  $S_2=5$ . What assumptions about the two populations are necessary in order to perform the pooled-variance t test for the hypothesis  $H_0: \mu_1=\mu_2$  against the alternative  $H_1: \mu_1 > \mu_2$  and make a statistical decision?

Choose the correct answer below:

- A. It is necessary to assume that the populations from which you are sampling have unequal variances and equal sizes.
- B. It is necessary to assume that the populations from which you are sampling have negative  $t_{STAT}$  test statistics and unequal sample means.
- C. It is necessary to assume that the populations from which you are sampling have equal population means and positive standard deviations.
- D. It is necessary to assume that the populations from which you are sampling have independent normal distributions and equal variances.

3) Assume that you have a sample of  $n_1=9$ , with the sample mean  $X_1=47$ , and a sample standard deviation of  $S_1=7$ , and you have an independent sample of  $n_2=13$  from another population with a sample mean of  $X_2=30$ , and the sample standard deviation  $S_2=8$ . Construct a 95% confidence interval estimate of the population mean difference between  $\mu_1$  and  $\mu_2$ .

$\leq \mu_1 - \mu_2 \leq$

(Type an integer or decimal rounded to two decimal places as needed.)

4) A survey of 700 adults from a certain region asked, "What do you buy from your mobile device?" The results indicated that 52% of the females and 40% of the males answered clothes. The sample sizes of males and females were not provided. Suppose that of 300 females, 156 reported they buy clothing from their mobile device, while of 400 males, 160 reported they buy clothing from their mobile device. Complete parts (a) through (d) below.

a. Is there evidence of a difference between males and females in the proportion who said they buy clothing from their mobile device at the 0.1 level of significance?

\*State the null and alternative hypotheses, where  $\pi_1$  is the population proportion of females who said they buy clothing from their mobile device and  $\pi_2$

- A.  $H_0: \pi_1 = \pi_2$   $H_1: \pi_1 > \pi_2$
- B.  $H_0: \pi_1 = \pi_2$   $H_1: \pi_1 < \pi_2$
- C.  $H_0: \pi_1 = \pi_2$   $H_1: \pi_1 \neq \pi_2$
- D.  $H_0: \pi_1 \neq \pi_2$   $H_1: \pi_1 = \pi_2$
- E.  $H_0: \pi_1 \neq \pi_2$   $H_1: \pi_1 < \pi_2$
- F.  $H_0: \pi_1 \neq \pi_2$   $H_1: \pi_1 = \pi_2$

\*Determine the value of the test statistic.

$Z_{STAT} =$

(Type an integer or a decimal. Round to two decimal places as needed.)

\*Determine the critical value(s) for this test of hypothesis.

The critical value(s) is (are)

(Type integers or decimals. Round to two decimal places as needed. Use a comma to separate answers as needed.)

\*State the conclusion:

Reject the null hypothesis. There is sufficient evidence to support the claim that there is a difference between males and females in the proportion who said they buy clothing from their mobile device

b. Find the p-value in (a).

The p-value in part (a) is

(Type an integer or a decimal. Round to three decimal places as needed.)

c. Construct and interpret a 90% confidence interval estimate for the difference between the proportion of males and females who said they buy clothing from their mobile device .

The confidence interval is  to

(Type integers or decimals. Round to four decimal places as needed. Use ascending order.)

\*What does the confidence interval mean?

A researcher can be 90% confident that the difference in the population proportions of males and females who said they buy clothing from their device is 95%, contained in less than the lower bound of greater than the upper bound of the interval.

5) The following information is available for two samples selected from independent normally distributed populations.

Population A:  $n_1=25$        $S^2_1=36$

Population B:  $n_2=25$        $S^2_2=9$

a. Which sample variance do you place in the numerator of  $F_{STAT}$ ?

A.  $S^2_2=9$

**B.  $S^2_1=36$**

b. What is the value of  $F_{STAT}$ ?

$F_{STAT} =$

(Round to two decimal places as needed.)

6) An experiment has a single factor with six groups and two values in each group. In determining the among-group variation, there are 5 degrees of freedom. In determining the within-group variation, there are 6 degrees of freedom. In determining the total variation, there are 11 degrees of freedom.

a. If  $SSA=200$  and  $SST=248$ , what is  $SSW$ ?

$SSW =$   (Type an integer or a decimal.)

b. What is  $MSA$ ?

$MSA =$   (Type an integer or a decimal.)

c. What is  $MSW$ ?

$MSW =$   (Type an integer or a decimal.)

d. What is the value of  $F_{STAT}$ ?

$F_{STAT} =$   (Type an integer or a decimal.)

7) An experiment has a single factor with six groups and two values in each group. In determining the among-group variation, there are 5 degrees of freedom. In determining the within-group variation, there are 6 degrees of freedom. In determining the total variation, there are 11 degrees of freedom. Also, note that:  $SSA=105$ ,  $SSW=42$ ,  $SST=147$ ,  $MSA=21$ ,  $MSW=7$ , and  $F_{STAT}=3$ . Complete parts (a) through (d).

a. Construct the ANOVA summary table and fill in all values in the table.

Source	Degrees of Freedom	Sum of Squares	Mean Square (Variance)	F
Among groups	<input type="text" value="5"/>	<input type="text" value="105"/>	<input type="text" value="21"/>	<input type="text" value="3"/>
Within groups	<input type="text" value="6"/>	<input type="text" value="42"/>	<input type="text" value="7"/>	
Total	<input type="text" value="11"/>	<input type="text" value="147"/>		

(Simplify your answers.)

b. At the 0.025 level of significance, what is the upper-tail critical value from the F distribution?

$F_{0.025} =$

(Round to two decimal places as needed.)

c. State the decision rule for testing the null hypothesis that all six groups have equal population means. Reject  $H_0$  if  $F_{STAT} > 5.99$

d. What is your statistical decision?

Since  $F_{STAT}$  is **less than** the upper-tail critical value, **do not reject  $H_0$** . There is **insufficient** evidence to conclude there is a difference in the population means for the six groups.