

Department of Statistics & Operations Research
 College of Science
 King Saud University
 STAT-324: Probability and Statistics for Engineers
 Second Mid-Term Exam
 Second Semester 1435 – 1436



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|-----------------------------|--|--------------------|--|
| Student's Name (In Arabic): | | Section's Number: | |
| Student's Number: | | Attendance number: | |
| Teacher's Name: | | | |

Instructions:

- There are 25 multiple choice questions.
- Time allowed is 90 minutes (1.5 Hour).
- For each question, put the code of the correct answer in the following table beneath the question number.
- Please, use **capital letters**: A, B, C, and D.
- Do not copy answers from your neighbors; they have different question forms.
- Mobile Telephones are not allowed in the classroom.

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|----|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| | | | | | | | | | |

| | | | | | | | | | |
|----|----|----|----|----|----|----|----|----|----|
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| | | | | | | | | | |

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|----|----|----|----|----|
| 21 | 22 | 23 | 24 | 25 |
| | | | | |

Question (1-6):

Given the standard normal distribution, $Z \sim N(0,1)$, find:

(1) The area under the curve between $z=-1.55$ and $z=1.55$

| | | | |
|-------------------|-----------|------------|------------|
| (A) <u>0.8788</u> | (B) 0.998 | (C) 1.5396 | (D) 0.0864 |
|-------------------|-----------|------------|------------|

(2) $P(Z \geq 2.05) =$

| | | | |
|------------|-------------------|------------|------------|
| (A) 0.1088 | (B) <u>0.0202</u> | (C) 0.3645 | (D) 0.1875 |
|------------|-------------------|------------|------------|

(3) $P(0.1 < Z < 2.05) =$

| | | | |
|------------|------------|-------------------|------------|
| (A) 0.0746 | (B) 0.9950 | (C) <u>0.4400</u> | (D) 0.9750 |
|------------|------------|-------------------|------------|

(4) If $P(Z < a) = 0.879$, then the value of $a =$

| | | | |
|----------|-----------|----------|-----------------|
| (A) 2.54 | (B) -1.87 | (C) 1.64 | (D) <u>1.17</u> |
|----------|-----------|----------|-----------------|

(5) If $P(-k < Z < k) = 0.95$, then the value of $k =$

| | | | |
|----------|----------|-----------------|---------|
| (A) 2.54 | (B) 2.31 | (C) <u>1.96</u> | (D) 0.5 |
|----------|----------|-----------------|---------|

(6) $P(Z=1.89) =$

| | | | |
|------------|------------|------------|----------------|
| (A) 0.1220 | (B) 0.1660 | (C) 0.1550 | (D) <u>0.0</u> |
|------------|------------|------------|----------------|

Question (7-9):

The weight of a large number of fat persons is nicely modeled with a normal distribution with mean of 100 kg and a standard deviation of 10 kg, find the probability that an individual picked at random from this population will have a weight

(7) at most 100 kg is:

| | | | |
|----------|-----------|------------|----------------|
| (A) 0.75 | (B) 0.125 | (C) 0.0162 | (D) <u>0.5</u> |
|----------|-----------|------------|----------------|

(8) Greater than 105 kg:

| | | | |
|-------------------|------------|------------|------------|
| (A) <u>0.3085</u> | (B) 0.4388 | (C) 0.0062 | (D) 0.5278 |
|-------------------|------------|------------|------------|

(9) Between 75 and 125 kg:

| | | | |
|-------------------|------------|------------|------------|
| (A) <u>0.9876</u> | (B) 0.7135 | (C) 0.6153 | (D) 0.8995 |
|-------------------|------------|------------|------------|

Question (10-11):

Suppose that the life time of a system is a random variable T which is modeled nicely by an exponential distribution with mean of 6 years.

(10) The variance of T is:

| | | | |
|---------|---------------|-------------|------------|
| (A) 136 | (B) <u>36</u> | (C) 0.514 2 | (D) 0.6161 |
|---------|---------------|-------------|------------|

(11) The probability that the life time of the system is greater than 10 years is

| | | | |
|------------|-------------------|------------|------------|
| (A) 0.0462 | (B) <u>0.1889</u> | (C) 0.4143 | (D) 0.2960 |
|------------|-------------------|------------|------------|

Question (12-13):

Let X be a normal random variable with mean 4 and variance 9. Then

(12) $P(X \geq 10.15) =$

| | | | |
|----------|-------------------|-------------|------------|
| (A) 0.56 | (B) <u>0.0202</u> | (C) 0.514 2 | (D) 0.6161 |
|----------|-------------------|-------------|------------|

(13) If $P(X < a) = 0.879$, then the value of a =

| | | | |
|-------|-----------------|---------|----------|
| (A) 8 | (B) <u>7.51</u> | (C) 8.9 | (D) 6.89 |
|-------|-----------------|---------|----------|

Question (14-17):

It is known that 60% of mice inoculated with a serum are protected from a certain disease (does not contract the disease). If 5 mice are inoculated, the probability that

(14) none contracts the disease:

| | | | |
|-----------|-----------|------------------|-----------|
| (A) 0.264 | (B) 0.331 | (C) <u>0.078</u> | (D) 0.159 |
|-----------|-----------|------------------|-----------|

(15) fewer than 2 contract the disease:

| | | | |
|-----------|------------------|-----------|-----------|
| (A) 1.005 | <u>(B) 0.337</u> | (C) 0.932 | (D) 0.085 |
|-----------|------------------|-----------|-----------|

(16) more than 2 contract the disease:

| | | | |
|------------|------------|------------|-------------------|
| (A) 0.2842 | (B) 0.7315 | (C) 0.4941 | <u>(D) 0.3174</u> |
|------------|------------|------------|-------------------|

(17) the standard deviation of the number of mice that contract the disease:

| | | | |
|------------------|-----------|-----------|-----------|
| <u>(A) 1.095</u> | (B) 0.951 | (C) 1.594 | (D) 0.858 |
|------------------|-----------|-----------|-----------|

Question (18-20):

A company is interested in evaluating its current inspection procedure for shipments of 10 identical items. The procedure is to take a sample of 5, without replacement. The defective proportion of shipments is 20%. The probability that in the sample

(18) none found to be defective:

| | | | |
|-----------------|-----------|-----------|-----------|
| <u>(A)0.222</u> | (B) 0.526 | (C) 0.123 | (D) 0.628 |
|-----------------|-----------|-----------|-----------|

(19) no more than 1 found to be defective:

| | | | |
|-----------|-----------|-----------|------------------|
| (A) 0.361 | (B) 0.518 | (C) 0.471 | <u>(D) 0.778</u> |
|-----------|-----------|-----------|------------------|

(20) the mean number found to be defective:

| | | | |
|-------|---------|--------------|-------|
| (A) 2 | (B) 0.5 | <u>(C) 1</u> | (D) 7 |
|-------|---------|--------------|-------|

Question (21-23):

On average, a textbook author makes two word-processing errors per page on the first draft of his textbook. Assuming that the number of errors follows Poisson distribution, the probability that:

(21) on the next page he will make no errors:

| | | | |
|-----------|-----------|-----------------|-----------|
| (A) 0.076 | (B) 0.305 | <u>(C)0.135</u> | (D) 0.215 |
|-----------|-----------|-----------------|-----------|

(22) on the next page he will make 2 or more errors:

| | | | |
|-----------|------------------|-----------|-----------|
| (A) 0.723 | <u>(B) 0.594</u> | (C) 0.151 | (D) 0.807 |
|-----------|------------------|-----------|-----------|

(23) The probability that on the next two pages he will make 1 or more errors:

| | | | |
|------------------|-----------|-----------|-----------|
| <u>(A) 0.982</u> | (B) 0.678 | (C) 0.265 | (D) 0.781 |
|------------------|-----------|-----------|-----------|

Question (24-25):

Suppose that X has the following uniform distribution:

$$f(x) = \begin{cases} \frac{1}{3}, & x = 1, 3, 4 \\ 0, & \text{otherwise} \end{cases}$$

(24) $P(X \geq 2) =$

| | | | |
|-----------|------------------|-----------|-----------|
| (A) 0.282 | <u>(B) 0.667</u> | (C) 0.155 | (D) 0.437 |
|-----------|------------------|-----------|-----------|

(25) The mean of X is:

| | | | |
|-----------|-----------|-----------|------------------|
| (A) 3.275 | (B) 1.888 | (C) 5.234 | <u>(D) 2.667</u> |
|-----------|-----------|-----------|------------------|