

SPREADS

King Saud University
Mathematics Department | ACTU461
Exercise's Lecture (11)
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Spreads

An option spread is a combination of only calls or only puts, in which some options are bought and some others are sold. To create portfolios useful for many different objectives.

A ratio spread

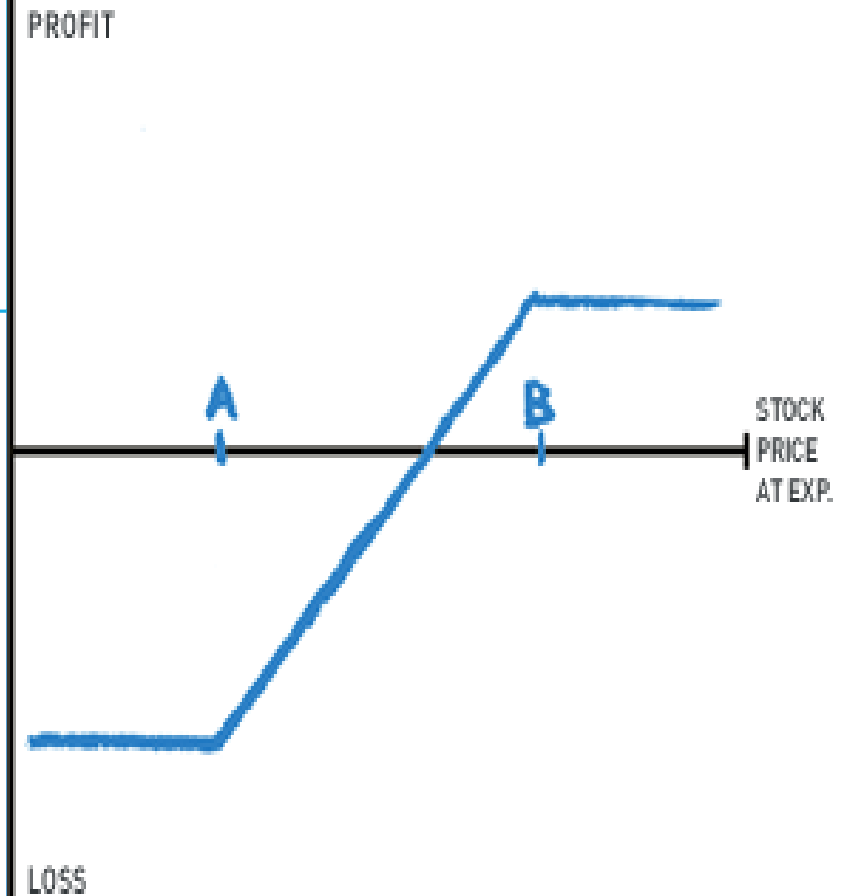
**is a combination of buying m calls at one strike price and selling n calls at a different strike price
And same expiration date.**

BULL SPREAD

Speculating on the increase of an asset price. Although investor gives up a portion of his profit on the purchased call, this is offset by the premium received for selling the call

Buying a K1–strike Call and Selling a K2–strike Call,
Or
Buying a K1–strike Put and Selling a K2–strike Put.

Both, - Same expiration date
- Same nominal amount
where $0 < K1 < K2$



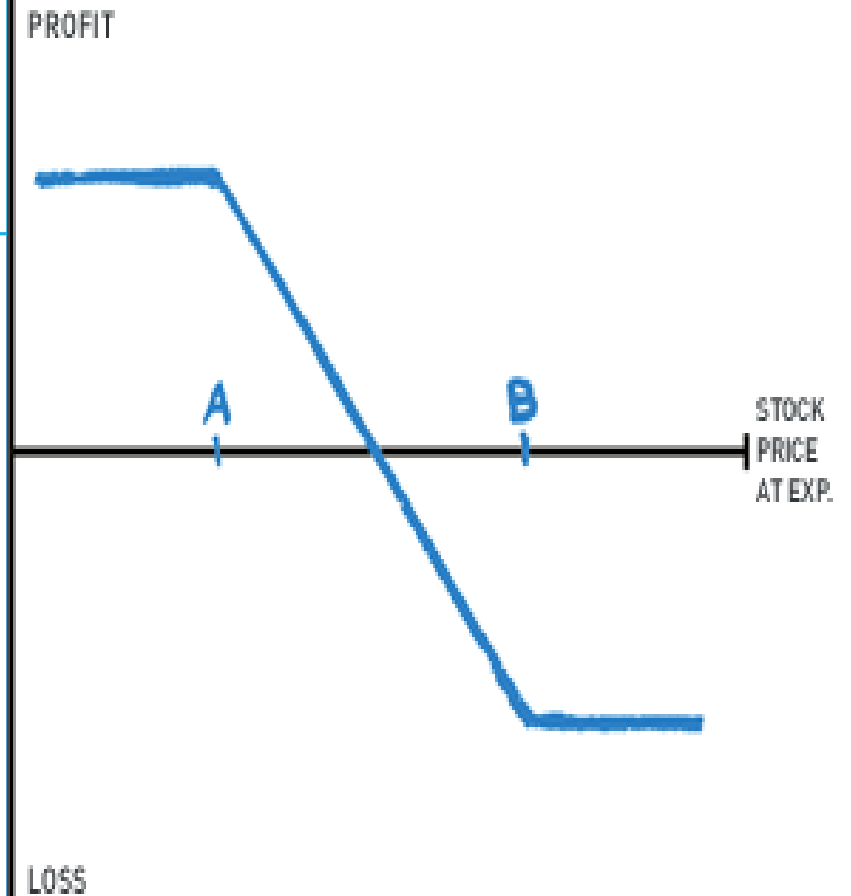
BEAR SPREAD

**Speculating on the decrease of an asset, price
Graph is reflection of that of a bull spread about
the horizontal axis**

Selling a K1–strike call and Buying a K2–strike Call,
Or
Selling a K1–strike Put and Buying a K2–strike Put.

Both, - Same expiration date
- Same nominal amount

where $0 < K1 < K2$



COLLARED STOCK

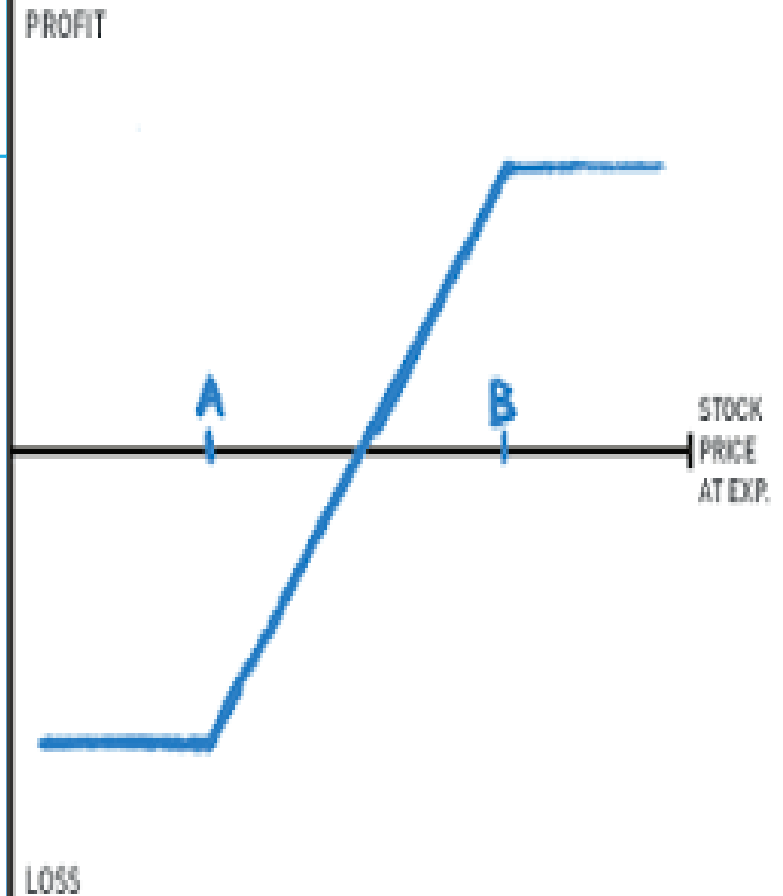
Collars are used to insure a long position on a stock.

A Collared Stock consists of:

Long Index + Collar

Buying the Index and Buying K1 Put , Selling a K2–
strike Call.

where $0 < K1 < K2$



WRITTEN COLLAR

Buy at-the-money Put Option with strike price K_1 + Sell out-of-the-money Call Option with strike price K_2 , where $K_2 > K_1$.

A Written Collar consists of:

Selling a K_1 –strike Put and Buying a K_2 –strike Call,

where $0 < K_1 < K_2$

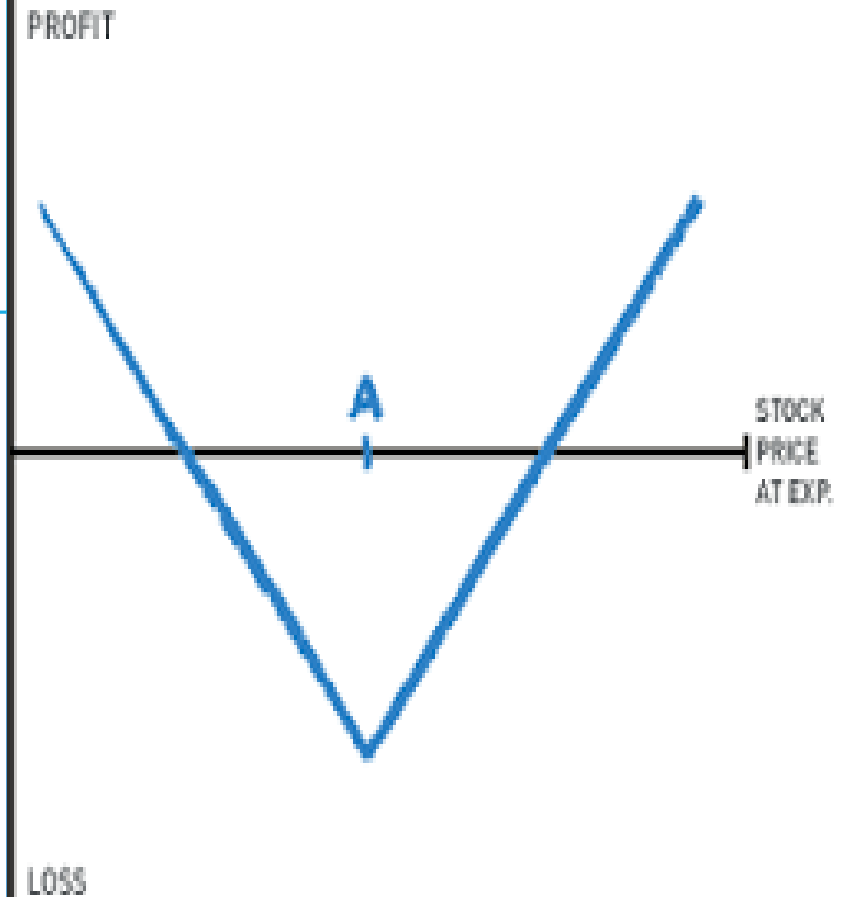
STRADDLE

A straddle is used to bet that the volatility of the market is higher than the market's assessment of volatility. Guaranteed payoff as long as ST is different than K .

A Straddle consists of:

Buying a K -strike call and a K -strike Put with

- Same strike price
- Same nominal amount



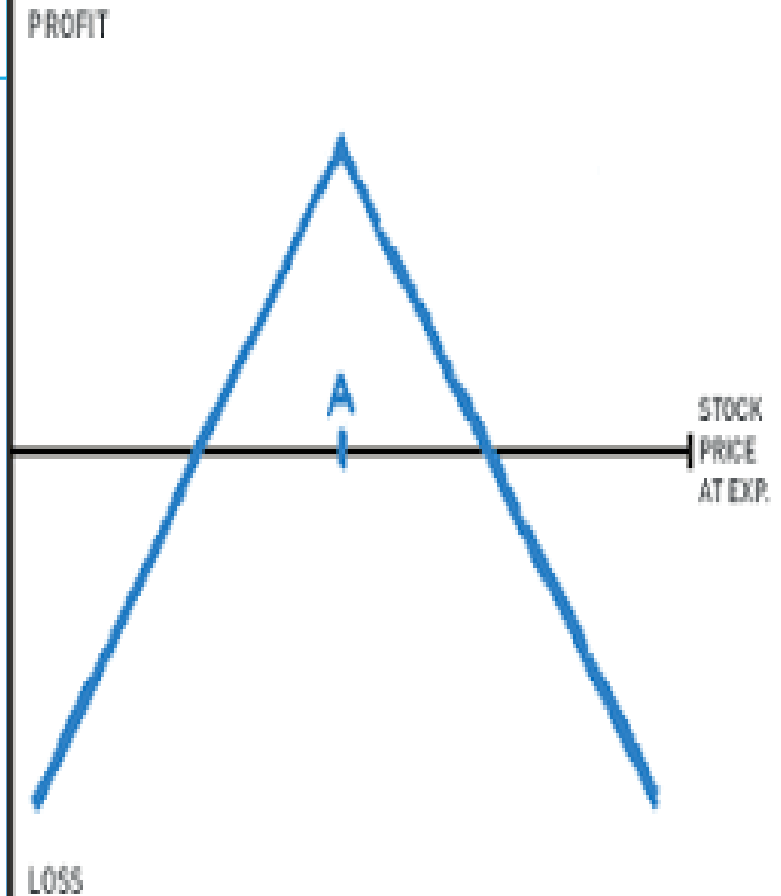
WRITTEN STRADDLE

Bet on low volatility .

A Writtin Straddle consists of:

Selling a K–strike call and a K–strike Put with

- Both, - Same strike price
- Same nominal amount



STRANGLE

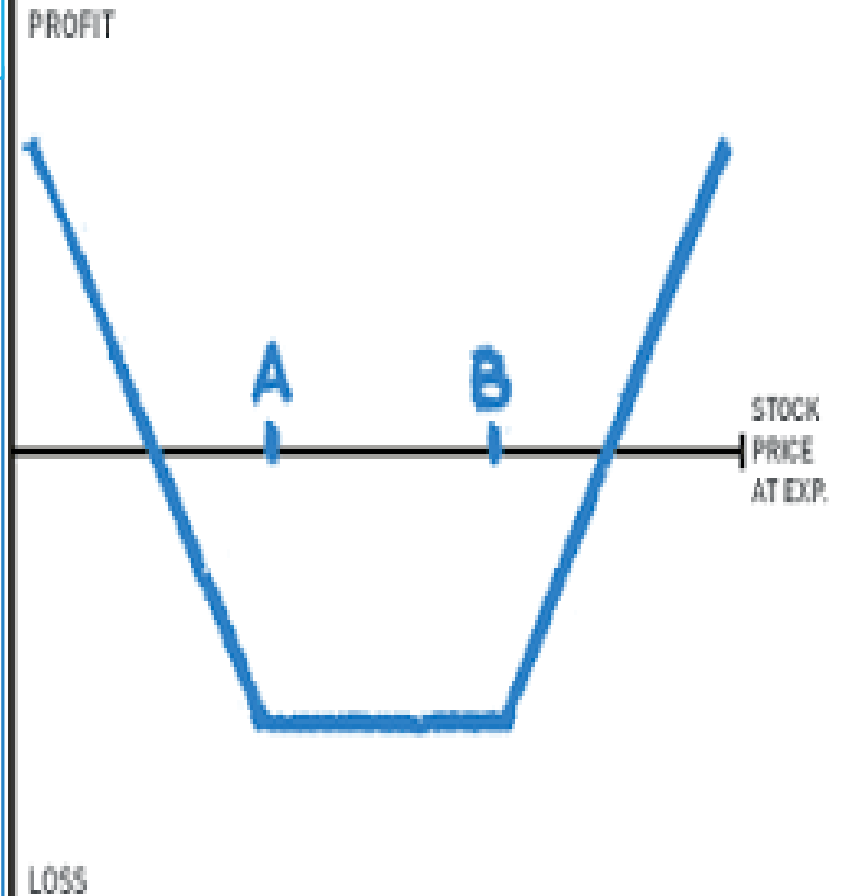
Bet on high volatility with lower cost.

A strangle consists on:

Buying a K_1 -strike Put and a K_2 -strike Call

Both, - same expiration date

where $0 < K_1 < K_2$



WRITTEN STRANGLE

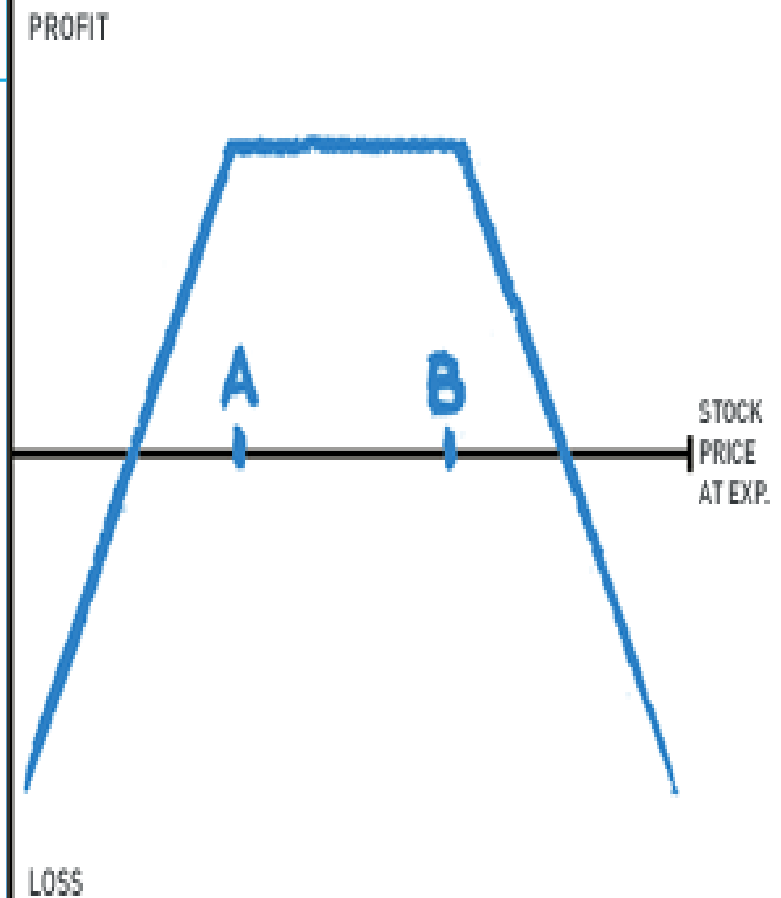
A written strangle is a bet on low volatility

A written strangle consists on:

Selling a K_1 -strike Call and a K_2 -strike Put

Both, - same expiration date

where $0 < K_1 < K_2$



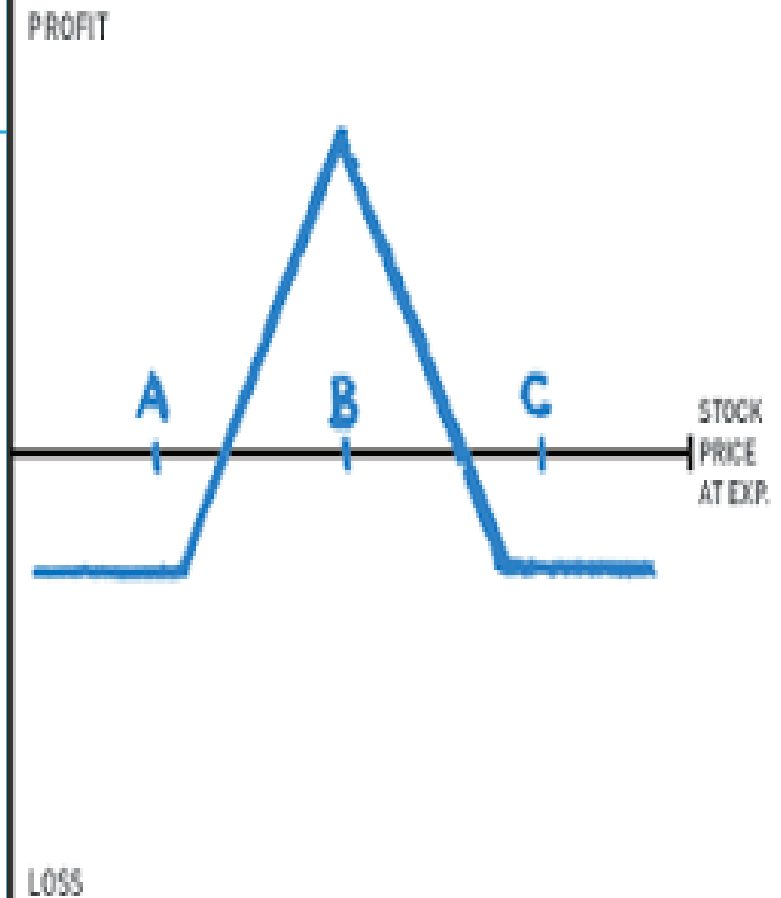
BUTTERFLY SPREAD

Bet on low volatility with lower cost. The upper and lower strike prices are equal distance from the middle.

A butterfly spread consists on:
Write a **straddle** and buy strangle

Selling a K_2 -strike Call and a K_2 -strike Put,
Buying a K_1 -strike Call and a K_3 -strike Put.

where $0 < K_1 < K_2 < K_3$



BOX SPREAD

Guarantees cash flow into the future. Purely a means of borrowing or lending money

A box spread consists of:

Creating a **synthetic long forward** in k_1 strike price,

And a **synthetic short forward** in k_2 strike price.

Buying a k_1 -strike Call and selling k_1 -strike Put,

And Buying a k_2 -Strike Put and selling a k_2 -strike Call.

At time T , a payment of $K_1 - K_2$ per share is obtained.

If $k_1 < k_2$, a box spread is a way to lend money.

If $k_1 > k_2$, a box spread is a way to borrow money

Joe believes that the volatility of a stock is higher than indicated by market prices for options on that stock. He wants to speculate on that belief by buying or selling at-the-money options.

Determine which of the following strategies would achieve Joe's goal.

- (A) Buy a strangle
- (B) Buy a straddle
- (C) Sell a straddle
- (D) Buy a butterfly spread
- (E) Sell a butterfly spread

The current price of a non-dividend paying stock is 40 and the continuously compounded risk-free interest rate is 8%. The following table shows call and put option premiums for three-month European of various exercise prices:

Exercise Price	Call Premium	Put Premium
35	6.13	0.44
40	2.78	1.99
45	0.97	5.08

A trader interested in speculating on volatility in the stock price is considering two investment strategies. The first is a 40-strike straddle. The second is a strangle consisting of a 35-strike put and a 45-strike call.

Determine the range of stock prices in 3 months for which the strangle outperforms the straddle.

Determine which of the following strategies creates a ratio spread, assuming all options are European.

- (A) Buy a one-year call, and sell a three-year call with the same strike price.
- (B) Buy a one-year call, and sell a three-year call with a different strike price.
- (C) Buy a one-year call, and buy three one-year calls with a different strike price
- (D) Buy a one-year call, and sell three one-year puts with a different strike price.
- (E) Buy a one-year call, and sell three one-year calls with a different strike price.

You are given:

- i) An investor short-sells a non-dividend paying stock that has a current price of 44 per share.
- ii) This investor also writes a collar on this stock consisting of a 40-strike European put option and a 50-strike European call option, Both options expire in one year.
- iii) The prices of the options on this stock are:

Strike Price	Call option	Put option
40	8.42	2.47
50	3.86	7.42

- iv) The continuously compounded risk-free interest rate is 5%.
Calculate the maximum profit for the overall position at expiration.

- (A) 2.61
- (B) 3.37
- (C) 4.79
- (D) 5.21

Box spreads are used to guarantee a fixed cash flow in the future. Thus, they are purely a means of borrowing or lending money, and have no stock price risk. Consider a box spread based on two distinct strike prices (K, L) that is used to lend money, so that there is a positive cost to this transaction up front, but a guaranteed positive payoff at expiration.

Determine which of the following sets of transactions is equivalent to this type of box spread.

- (A) A long position in a (K, L) bull spread using calls and a long position in a (K, L) bear spread using puts.
- (B) A long position in a (K, L) bull spread using calls and a short position in a (K, L) bear spread using puts.
- (C) A long position in a (K, L) bull spread using calls and a long position in a (K, L) bull spread using puts.
- (D) A short position in a (K, L) bull spread using calls and a short position in a (K, L) bear spread using puts.
- (E) A short position in a (K, L) bull spread using calls and a short position in a (K, L) bull spread using puts.

The current price of a stock is 40. The continuously compounded risk-free rate and dividend rate are $r = 0.03$ and $\text{Delta} = 0.01$. The price of an at-the-money 3-month call is 2.48. An investor buys the at-the-money 3-month call and put.

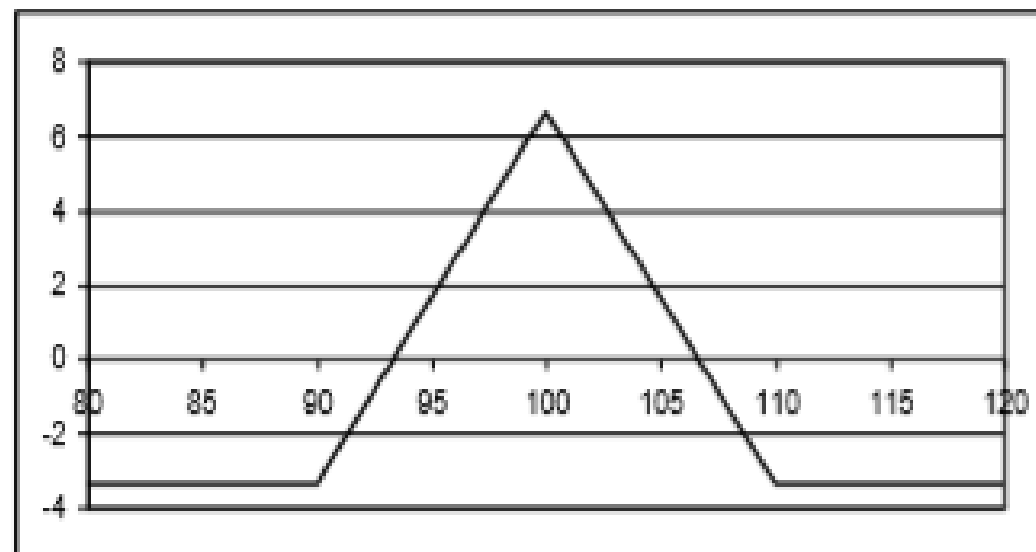
- a) Give the name of this combined position and the graph.
- b) What is the minimum profit?

9.

Stock ABC has the following characteristics:

- The current price to buy one share is 100.
- The stock does not pay dividends.
- European options on one share expiring in one year have the following prices:

Strike Price	Call option price	Put option price
90	14.63	0.24
100	6.80	1.93
110	2.17	6.81



A butterfly spread on this stock has the following profit diagram.

The continuously compounded risk-free interest rate is 5%.

Determine which of the following will NOT produce this profit diagram.

- (A) Buy a 90 put, buy a 110 put, sell two 100 puts
- (B) Buy a 90 call, buy a 110 call, sell two 100 calls
- (C) Buy a 90 put, sell a 100 put, sell a 100 call, buy a 110 call
- (D) Buy one share of the stock, buy a 90 call, buy a 110 put, sell two 100 puts

The current price of a stock index is 1000. The following table shows call and put option premiums for six months European options of various exercise prices:

Exercise Price	Call Premium	Put Premium
950	120.41	51.78
1000	93.81	74.20
1050	71.80	101.21

Strategy 1 is to sell the 950-strike put and to buy 1,050-strike call

Strategy 2 is to buy the 950-strike put and to sell 1,050-strike call

Strategy 3 is to buy the 950-strike call and to sell 1,050-strike call

Strategy 4 is to buy 950-strike call, sell the 1,000 -strike call, sell the 950-strike put and buy the 1,000-strike put.

Determine which, if any, of these strategies will have greater payoffs in six months for higher prices of the stock index than for relatively lower prices.