

$$(1) \text{ Q23.4 } \quad |\vec{F}_{12}| = |\vec{F}_{21}| = K \frac{q_1 q_2}{r^2} = \frac{9 \times 10^9 \times (1.6 \times 10^{-19})^2}{(2 \times 10^{-15})^2}$$

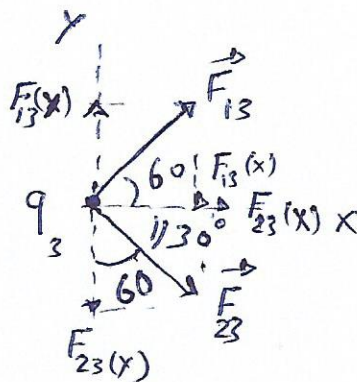
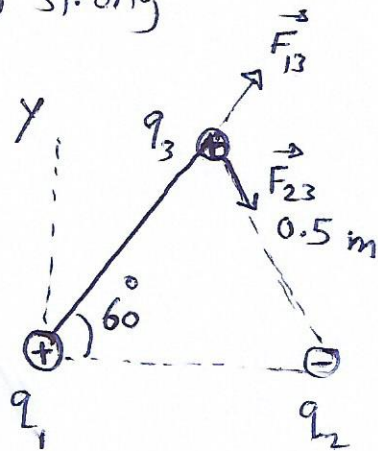
$$= 57.5 \text{ N} \quad \text{very strong}$$

$$(2) \text{ Q23.7: } \quad \vec{F}_{13} = K_e \frac{q_1 q_3}{r_{13}^2} = \frac{9 \times 10^9 \times 2 \times 10^{-6} \times 7 \times 10^{-6}}{(0.5)^2}$$

$$= 0.503 \text{ N}$$

$$\vec{F}_{23} = K_e \frac{q_2 q_3}{r_{23}^2} = \frac{9 \times 10^9 \times 4 \times 10^{-6} \times 7 \times 10^{-6}}{(0.5)^2}$$

$$= 1.01 \text{ N}$$



$$\begin{aligned} \vec{F}_x &= \vec{F}_{13}(x) + \vec{F}_{23}(x) \\ &= F_{13} \cos 60 + F_{23} \cos 30 \\ &= 0.503 \times \frac{1}{2} + 1.01 \times 0.866 \\ &= 0.755 \text{ N} \end{aligned}$$

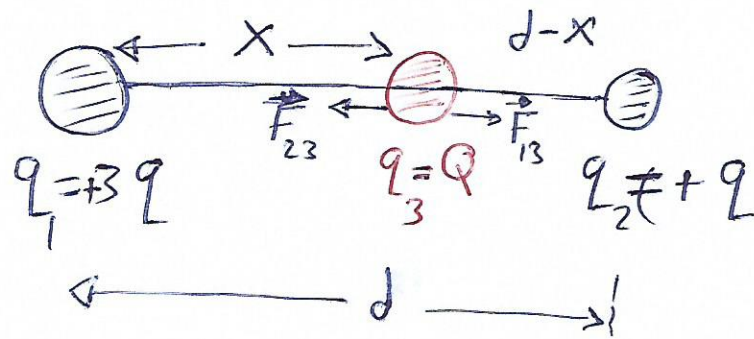
$$\begin{aligned} \vec{F}_y &= \vec{F}_{13}(y) + \vec{F}_{23}(y) \\ &= F_{13} \sin 60 - F_{23} \sin 30 \\ &= 0.503 \times 0.866 - 1.01 \times \frac{1}{2} \\ &= -0.436 \text{ N} \end{aligned}$$

$$\Rightarrow \vec{F}_3 = F_x \hat{i} + F_y \hat{j} = 0.755 \hat{i} - 0.436 \hat{j} \quad (\text{N})$$

$$|\vec{F}_3| = \sqrt{(0.755)^2 + (0.436)^2} = 0.872 \text{ N}$$

$$\phi = \tan^{-1}\left(\frac{F_y}{F_x}\right) = \tan^{-1}\left(\frac{-0.436}{0.755}\right) = -30^\circ \text{ with } x$$

(3) Q 23-10



At equilibrium

$$|\vec{F}_{23}| = |\vec{F}_{13}|$$

$$\frac{k q_2 q_3}{r_{23}^2} = \frac{k q_1 q_3}{r_{13}^2}$$

$$\frac{Q \cdot Q}{(d - X)^2} = \frac{3Q \cdot Q}{X^2}$$

$$\frac{1}{(d - X)^2} = \frac{3}{X^2}$$

$$\sqrt{\frac{1}{(d - X)^2}} = \sqrt{\frac{3}{X^2}}$$

$$\Rightarrow \frac{1}{d - X} = \frac{\sqrt{3}}{X}$$

$$\Rightarrow X = \sqrt{3} (d - X) = \sqrt{3} d - \sqrt{3} X$$

$$\Rightarrow X + \sqrt{3} X = \sqrt{3} d \Rightarrow \boxed{X = \frac{\sqrt{3} d}{1 + \sqrt{3}}}$$

(4) Q 23.14

$$Q = 24 \mu\text{C}$$

$$\vec{E} = 610 \text{ N/C}$$



$$\Rightarrow QE = mg$$

$$m = \frac{QE}{g} = \frac{24 \times 10^{-6} \times 610}{9.8} \approx 1.5 \times 10^{-3} \text{ Kg}$$

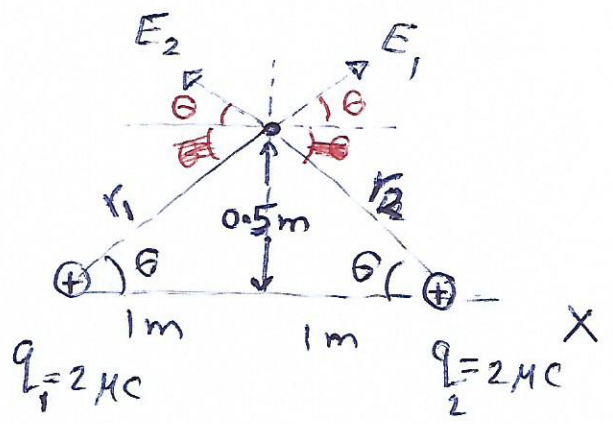
$$\approx 1.5 \text{ gm}$$

(5) Q 23.20

(a)

$$r_1 = r_2 = \sqrt{(1)^2 + (0.5)^2} = 1.12 \text{ m}$$

$$E_1 = E_2 = \frac{kq_1}{r_1^2} = \frac{kq_2}{r_2^2}$$



because $r_1 = r_2$ & $q_1 = q_2$

$$\Rightarrow E_1 = E_2 = \frac{9 \times 10^9 \times 2 \times 10^{-6}}{(1.12)^2} = 14.4 \times 10^3 \text{ N/C}$$

Field	X-Comp.	Y-Comp.
E_1	$E_1 \cos \theta$	$E_1 \sin \theta$
E_2	$-E_2 \cos \theta$	$E_2 \sin \theta$
Resultant	0	$2E_1 \sin \theta$

because $E_1 = E_2$

$$E_1 = E_2 = 14.4 \times 10^3$$

$$F = 2E \sin \theta = 2 \times 14.4 \times 10^3 \times 0.5$$

Q23.20 (b)

$$F = qE$$

$$= -3 \times 10^{-6} \times 1.29 \times 10^4$$

$$= -3.86 \times 10^{-2} \text{ N}$$

in $-y$ direction.

(6) Q23.21

(a)

$$E_1 = \frac{kq}{r_1^2} \quad (r_1 = a)$$

$$q_1 = 2q$$

$$\Rightarrow E_1 = \frac{2kq}{a^2}$$

$$E_2 = \frac{kq}{r_2^2} \quad (r_2 = a)$$

$$q_2 = 4q \Rightarrow E_2 = \frac{4kq}{a^2}$$

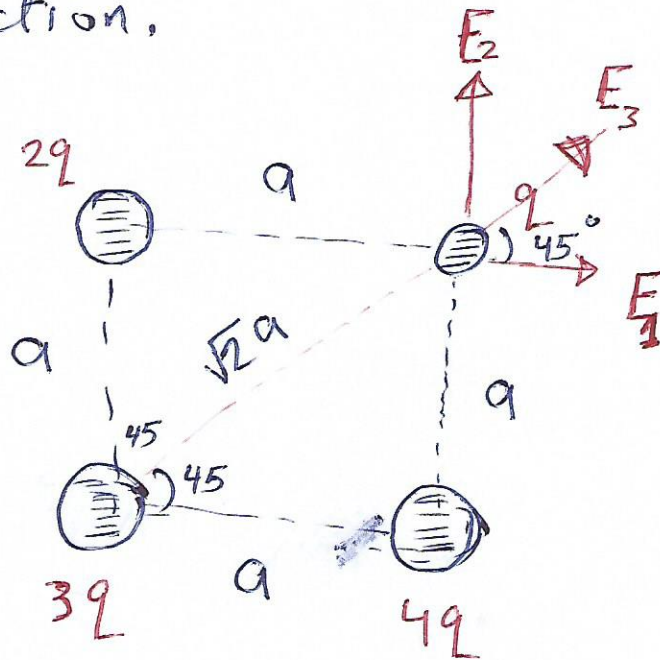
$$E_3 = \frac{kq}{r_3^2} \quad (r_3 = \sqrt{2}a)$$

$$q_3 = 3q \Rightarrow E_3 = \frac{3kq}{2a^2}$$

E_3 has two components

$$E_{3x} = E_3 \cos \theta$$

$$E_{3y} = E_3 \sin \theta$$



E	X-comp	Y-comp
E_1	$E_{1x} = E_1$	$E_{1y} = 0$
E_2	$E_{2x} = 0$	$E_{2y} = E_2$
E_3	$E_3 \cos \theta$	$E_3 \sin \theta$
\vec{E}_{net}	E_x	E_y

$$E_x = E_1 + E_3 \cos \theta$$

$$= \frac{2kq}{a^2} + \frac{3kq}{2a^2} \times \left(\frac{a}{\sqrt{2}a} \right)$$

$$= \frac{4\sqrt{2}kq + 3kq}{2\sqrt{2}a^2} = 3.06 \frac{kq}{a^2}$$

$$\Rightarrow \vec{E}_{\text{net}} = \frac{3.06 \text{ Kq}}{a^2} \hat{i} + \frac{5.06 \text{ Kq}}{a^2} \hat{j}$$

$$\text{Magnitude} \Rightarrow \sqrt{\left(\frac{3.06 \text{ Kq}}{a^2}\right)^2 + \left(\frac{5.06 \text{ Kq}}{a^2}\right)^2}$$

$$= \frac{5.91 \text{ Kq}}{a^2}$$

$$\text{angle } \phi = \tan^{-1}\left(\frac{E_y}{E_x}\right) = \tan^{-1}\left(\frac{5.06 \text{ Kq}/a^2}{3.06 \text{ Kq}/a^2}\right)$$

$$\phi = \tan^{-1}\left(\frac{5.06}{3.06}\right) = 58.8^\circ$$

$$(b) \vec{F} = q\vec{E} = \frac{5.91 \text{ Kq}^2}{a^2}$$

$$\phi = 58.8^\circ$$

Q 23.42

$$F = qE \Rightarrow ma$$

$$\text{for electron} \Rightarrow \vec{a} = \frac{q\vec{E}}{m} = \frac{-1.6 \times 10^{-19} \times 520}{9.1 \times 10^{-31}} = -9.14 \times 10^{13} \text{ m/s}^2$$

$$\Rightarrow v_f = v_0 + at = 0 - 9.14 \times 10^{13} \times 48 \times 10^{-9}$$

$$= -4.39 \times 10^6 \text{ m/s}$$

opposite to the field direction

$$\text{for proton } \vec{a} = \frac{q\vec{E}}{m} = \frac{1.6 \times 10^{-19} \times 520}{1.67 \times 10^{-27}} = 4.98 \times 10^{10} \text{ m/s}^2$$

$$\Rightarrow v_f = v_0 + at = \dots$$

Q 23.45

to stop the electrons
the electric field needs to
do work on the electrons

$$W = \Delta K = \frac{1}{2} m_e (v_f^2 - v_i^2)$$

$$\vec{F} \cdot \vec{d} = \frac{1}{2} m_e (0 - v_i^2)$$

$$q E d = -\frac{1}{2} m_e v_i^2$$

$q = -e$ for electrons

$$f e E d = f \frac{1}{2} m_e v_i^2$$

$$\Rightarrow E = \frac{\frac{1}{2} m_e v_i^2}{e d} = \frac{K_i}{e d}$$

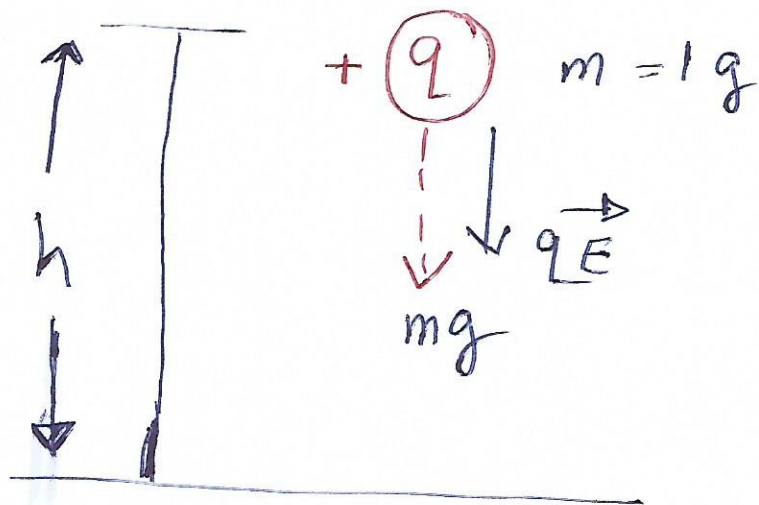
The field direction will be in the
direction of electron motion.

Q 23.46

$$m = 1 \times 10^{-3} \text{ kg.}$$

$$v_i = 0$$

$$v_f = 21 \text{ m/s}$$



in order to determine the direction of the field, ~~we need~~ we need to know about the acceleration:

$$v_f^2 = v_i^2 + 2a_y \Delta h$$

$$(21)^2 = 0 + 2a_y \times 5$$

$$\Rightarrow a_y = 44.1 \text{ m/s}^2$$

$$a_y = g + a \text{ (from the electric field)}$$

therefore the electric field must have downward direction.

$$a_{\text{electric field}} = 44.1 - 10 = 34.1 \text{ m/s}^2$$

$$= (qE) \quad a = \frac{qE}{m} \quad \text{m} = 10^{-3}$$