

Name : **SOLUTION**

Student ID : _____

Question 1 (1 mark)

You're given the following linear system :

$$3x_1 - 2x_2 = -1$$

$$4x_1 + 5x_2 = 3$$

$$7x_1 + 3x_2 = 2$$

find the augmented matrix.

$$\left(\begin{array}{cc|c} 3 & -2 & -1 \\ 4 & 5 & 3 \\ 7 & 3 & 2 \end{array} \right) \quad \mathbf{1 \text{ mark}}$$

Question 2 (1 mark)

Solve the following linear system with the corresponding augmented matrix :

$$\left(\begin{array}{ccc|c} 2 & -1 & 4 & \\ -8 & 4 & -1 & \end{array} \right)$$

By reducing the matrix:

$$4R_1 + R_2 \rightarrow R_2$$

$$\left(\begin{array}{ccc|c} 2 & -1 & 4 & \\ 0 & 0 & 15 & \end{array} \right) \quad \mathbf{0.5 \text{ mark}}$$

Back substituting :

$$2x - y = 4$$

$$0 = 15$$

The second equation is contradictory, so the given system has no solution. **0.5 mark****Question 3 (1 mark : 0.5 Decision + 0.5 verification)**

Determine whether the following matrix is in row echelon form, reduced row echelon form or neither (verify):

$$\left(\begin{array}{ccc} 1 & 2 & 3 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{array} \right)$$

The second row consists entirely of zeros and it is not at the bottom of the matrix

which validates a property of row echelon form matrices and if it is not in row echelon form **0.5 mark** then it can't be at the reduced row echelon form.Neither **0.5 mark****Question 4 (1 + 1 marks : 0.5 + 0.5 Decisions , 0.5 + 0.5 verifications)**

Determine if the following statements are true or false (verify):

a) The system:

$$\ln(x) + y = 0$$

$$2x = 0$$

is a homogeneous system of linear equations .

False **0.5 mark** . Not linear because the variable x is an argument to a function. **0.5 mark**

b) A consistent linear system has no solution .

False **0.5 mark**An Inconsistent linear system has no solution **0.5 mark**

OR (Alternative verification)

A consistent linear system has either infinitely many solutions **0.25 mark** or a unique solution **0.25 mark (Alternative)**