

Name : **Solution**

Student ID :

**Question 1** (1 + 1 marks : 1 Decision , 1 verification )

Determine whether the following matrix is in row echelon form, reduced row echelon form or neither (verify):

$$\begin{pmatrix} 1 & 2 & 3 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \end{pmatrix}$$

In any two successive rows that do not consist entirely of zeros, the leading 1 in the lower row occurs farther to the right than the leading 1 in the higher row **1 mark**

Neither **1 mark**

**Question 2** (2 marks)

Solve the following system by reducing the corresponding augmented matrix :

$$x_1 + 3x_2 - x_3 = 0$$

$$x_2 - 8x_3 = 0$$

$$4x_3 = 0$$

$$\left( \begin{array}{ccc|c} 1 & 3 & -1 & 0 \\ 0 & 1 & -8 & 0 \\ 0 & 0 & 4 & 0 \end{array} \right)$$

$$\frac{1}{4}R_3 \rightarrow R_3$$

$$-3R_2 + R_1 \rightarrow R_1$$

$$\left( \begin{array}{ccc|c} 1 & 0 & 23 & 0 \\ 0 & 1 & -8 & 0 \\ 0 & 0 & 1 & 0 \end{array} \right)$$

$$8R_3 + R_2 \rightarrow R_2$$

$$\left( \begin{array}{ccc|c} 1 & 0 & 23 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{array} \right)$$

$$-23R_3 + R_1 \rightarrow R_1$$

$$\left( \begin{array}{ccc|c} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{array} \right)$$

$$x_1 = 0$$

$$x_2 = 0$$

$$x_3 = 0$$

**2 marks****Question 3** (1 mark : 0.5 Decision , 0.5 verification )

Determine if the following statement are true or false (verify):

a) If a system have more equations than variables then it has infintely many solutions .

False , **0.5 mark** For Example the system :  $2x - y = 0$ 

$$3x - y = 1$$

$$x + y = 3 \quad \text{has a unique solution of } x = 1 \text{ and } y = 2 \quad \mathbf{0.5 mark}$$

Or (Alternatively)

If a system have more **variables than equations** then it has infintely many solutions.