

**MODERN PHYSICS (351 PHYS)**  
**PROBLEM SET 5**

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**PROBLEM (1)**

Discuss why the following functions cannot be a wavefunction

1.  $f(x) = -x^4 + x^2 - 2$
2.  $g(x) = \sin(x/2)$  if  $x \in [-\pi, \pi]$
3.  $h(x) = \begin{cases} 1 & \text{if } -1 < x < 1 \\ 2 & \text{if } 0 < x < 2 \end{cases}$

**PROBLEM (2)**

Compute the following commutators

1.  $[x^2, p]$
2.  $[xp, 2x]$
3.  $[ix - p^2, -x^2 + 2p]$

**PROBLEM (3)**

Given the wavefunction

$$\psi(x) = N \cos(2\pi x/L)$$

Defined over  $x \in [-L/4, +L/4]$  Find the normalisation constant  $N$ , then compute  $\langle x \rangle$  and  $\langle p \rangle$ .

### PROBLEM (4)

Given the wavefunction

$$\psi(x) = Ne^{-\xi x^2/2}$$

Compute the uncertainty in position for this system  $\Delta x$

Provided that

$$\int_{-\infty}^{+\infty} x^{2n} e^{-\lambda x^2} = \frac{1 \cdot 3 \cdots (2n-1)}{(2\lambda)^n} \times \sqrt{\frac{\pi}{\lambda}}$$

### PROBLEM (5)

Compute the ground state and 1st excited state energy for an electron in an infinite well of width 1 Å. What would the energies be in the particle was a proton ?

### PROBLEM (6)

An electron trapped in an infinite well of width 4 nm, centred at  $x = 3$ .

1. What is the probability per nm of finding the electron at  $x = 1$  nm ?
2. compute  $\langle x \rangle$  and  $\langle p^2 \rangle$ .
3. find the uncertainty in momentum  $\Delta p$ .

### PROBLEM (7)

Which of the following formulas describes the shortest wavelength in the Balmer series?

1.  $4hc/E_R$
2.  $4hc/3E_R$
3.  $3hc/4E_R$
4.  $3hc/E_R$

Where  $E_R = 13,6 \text{ eV} = hc/R$