## Two sample T

1) 

The phosphorus content was measured for independent samples of skim and whole Whole: $94.95 \quad 95.15 \quad 94.8594 .55 \quad 94.55 \quad 93.40 \begin{array}{lllllllll}95.05 & 94.35 & 94.70 & 94.90\end{array}$ $\begin{array}{llllllllllllllll}\text { Skim: } & 91.25 & 91.80 & 91.50 & 91.65 & 91.15 & 90.25 & 91.90 & 91.25 & 91.65 & 91.00\end{array}$
Assuming normal populations with equal variances
a) Test whether the average phosphorus content of skim milk is less than the average phosphorus content of whole milk. Use $\alpha=0.01$

1- Test for equality of variance
$H_{0}: \sigma_{12}=\sigma_{22}$
$H_{1}: \sigma_{12} \neq \sigma_{22}$


Conclusion: As F $\ngtr \mathrm{F}$ Critical one-tail, we fail reject the null hypothesis. This is the case, $1.0849>3.1789$. Therefore, we fail to reject the null hypothesis. The variances of the two populations are equal ( $p$-value $=0.4527 \nless \alpha=0.05$ )
(2- T test two samples for means assuming equal variance By Excel)

t-Test: Two-Sample Assuming Equal Variances

|  | skim | whole |
| :--- | ---: | ---: |
| Mean | 91.34 | 94.645 |
| Variance | 0.233222 | 0.253028 |
| Observations | 10 | 10 |
| Pooled Variance | 0.243125 |  |
| Hypothesized Mean Difference | 0 |  |
| $d f$ | 18 |  |
| $t$ Stat | -14.9879 |  |
| $P(T<=t)$ one-tail | $6.53 \mathrm{E}-12$ |  |
| $t$ Critical one-tail | 2.55238 |  |
| $P(T<=t)$ two-tail | $1.31 \mathrm{E}-11$ |  |
| t Critical two-tail | 2.87844 |  |

1- Test hypothesis:
$H_{0}: \mu_{2} \geq \mu_{1}$
$H_{1}: \mu_{2}<\mu_{1}$
2- T stat $=-14.9879$
3- $\quad$ T critical one tail $=2.55238$
4- Conclusion: We do a one-tail test. If t Stat <-t Critical one-tail, we reject the null hypothesis.As $-14.9879<-2.55238$ (p-value $=0.00000653<\alpha=0.01$ ). Therefore, we reject the null hypothesis

5- Independent random samples of 17 sophomores and 13 juniors attending a large university yield the following data on grade point averages:

| Sophomores |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 3.04 | 2.92 | 2.86 | 2.56 | 3.47 | 2.65 |
| 1.71 | 3.60 | 3.49 | 2.77 | 3.26 | 3.00 |
| 3.30 | 2.28 | 3.11 | 2.70 | 3.20 | 3.39 |
| 2.88 | 2.82 | 2.13 | 3.00 | 3.19 | 2.58 |
| 2.11 | 3.03 | 3.27 | 2.98 |  |  |
| 2.60 | 3.13 |  |  |  |  |

Assuming normal population. At the 5\% significance level, do the data provide sufficient evidence to conclude that the mean GPAs of sophomores and juniors at the university different?

1- Test for equality of variance
$H_{0}: \sigma_{12}=\sigma_{22}$
$H_{1}: \sigma_{12} \neq \sigma_{22}$

F-Test TwoSample for Variances

| Juniors | Sophomores |  |
| :--- | ---: | :--- |
| 2.980769231 | 2.84 | Mean |
| 0.095641026 | 0.270225 | Variance |
| 13 | 17 | Observations |
| 12 | 16 | df |
|  | 2.825408847 | F |
|  |  | $\mathrm{P}(\mathrm{F}<=\mathrm{f})$ one- |
|  | 0.037332216 | tail |
|  | 2.598881158 | F Critical |
| one-tail |  |  |

Conclusion: As F > F Critical one-tail, we reject the null hypothesis. Therefore, reject the null hypothesis. The variances of the two populations are unequal ( p -value $=0.03733<\alpha=0.05$ )

2- T test two samples for means assuming unequal variance By Excel

t-Test: Two-Sample Assuming Unequal Variances

| Juniors | Sophomores |  |
| :--- | ---: | :--- |
| 2.980769231 | 2.84 | Mean |
| 0.095641026 | 0.270225 | Variance |
| 13 | 17 | Observations |
| 0 | Hypothesized Mean Difference |  |
| 27 | df |  |
|  | -0.923149563 | t Stat |
|  | 0.182052992 | $\mathrm{P}(\mathrm{T}<=\mathrm{t})$ one-tail |
|  | 1.703288446 | t Critical one-tail |
|  | 0.364105983 | $\mathrm{P}(\mathrm{T}<=\mathrm{t})$ two-tail |
|  | 2.051830516 | t Critical two-tail |

1. Test hypothesis:
$H_{0}: \mu_{2}=\mu_{1}$
$H_{1}: \mu_{2} \neq \mu_{1}$
2. T stat $=-0.9231$
3. T critical two tail $=2.05183$
4. Conclusion: We do a two-tail test (inequality). If t Stat < -t Critical two-tail or t Stat $>\mathrm{t}$ Critical two-tail, we reject the null hypothesis. This is not the case, -$2.05183<-0.9231<2.05183$. Therefore, we do not reject the null hypothesis (p-value $=0.3641 \nless \alpha=0.05$ )

3-
8- In an experiment comparing 2 feeding methods for caves, eight pairs of twins were used one twin receiving Method $A$ and other twin receiving Method $B$. At the end of a given time, the calves were slaughtered and cooked, and the meat was rated for its taste ( with a higher number indicating a better taste):

| Twin pair | Method A | Method B |
| :--- | :--- | :--- |
| 1 | 27 | 23 |
| 2 | 37 | 28 |
| 3 | 31 | 30 |
| 4 | 38 | 32 |
| 5 | 29 | 27 |
| 6 | 35 | 29 |
| 7 | 41 | 36 |
| 8 | 37 | 31 |

Assuming approximate normality, test if the average taste score for calves fed by Method B is less than the average taste foe calves fed by Method A. Use $\alpha=0.05$.
(T test parried two samples for means By Excel)


| method $a$ | method $b$ |  |
| ---: | :--- | :--- |
| 34.375 | 29.5 | Mean |
| 23.69642857 | 14.57142857 | Variance |
| 8 | 8 | Observations |
|  | 0.857204246 | Pearson Correlation |
| 0 | Hypothesized Mean Difference |  |
|  | 7 | df |
|  | -5.445859126 | t Stat |
|  | 0.000480113 | $\mathrm{P}(\mathrm{T}<=\mathrm{t})$ one-tail |
|  | 1.894578605 | t Critical one-tail |
|  | 0.000960226 | $\mathrm{P}(\mathrm{T}<=\mathrm{t})$ two-tail |
|  | 2.364624252 | t Critical two-tail |

1. Test hypothesis:

$$
\begin{aligned}
& H_{0}: \mu_{b} \geq \mu_{a} \\
& H_{1}: \mu_{b}<\mu_{a}
\end{aligned}
$$

2. T stat $=-5.44585$
3. T critical one tail $=1.89457$
4. Conclusion: We do a one-tail test . If $t$ Stat <-t Critical one-tail, we reject the null hypothesis.As $-5.44585<-1.89457$ ( p -value $=0.00048<\alpha=0.05$ ) . Therefore, we reject the null hypothesis

## PEARSON CORRELATION COEFFICIENT

4) We have the table illustrates the age $X$ and blood pressure $Y$ for eight female.

| 68 | 49 | 60 | 42 | 55 | 63 | 36 | 42 | X |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 152 | 145 | 155 | 140 | 150 | 140 | 118 | 125 | Y |

Find:

|  | By Excel <br> (using $(\mathrm{fx})$ and (Data Analysis)) |
| :--- | :---: |
| Correlation=0.791832 | CORREL(M3:M10;N3:N10) |

Positive correlation between $x$ and $y$


Ten Corvettes between 1 and 6 years old were randomly selected from last year's sales records in Virginia Beach, Virginia. The following data were obtained, where x denotes age, in years, and y denotes sales price, in hundreds of dollars.

| $x$ | 6 | 6 | 6 | 4 | 2 | 5 | 4 | 5 | 1 | 2 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $y$ | 125 | 115 | 130 | 160 | 219 | 150 | 190 | 163 | 260 | 260 |

a) Determine the regression equation for the data.
b) Compute and interpret the coefficient of determination, $\mathrm{r}^{2}$.
c) Obtain a point estimate for the mean sales price of all 4-year-old Corvettes.
(Linear regression by Excel)



| SUMMARY OUTPUT |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |
| Regression Statistics |  |  |  |  |  |  |  |  |
| Multiple R | 0.967871585 |  |  |  |  |  |  |  |
| R Square | 0.936775406 |  |  |  |  |  |  |  |
| Adjusted R Square | 0.928872332 |  |  |  |  |  |  |  |
| Standard Error | 14.24652913 |  |  |  |  |  |  |  |
| Observations | 10 |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |
| ANOVA |  |  |  |  |  |  |  |  |
|  | df | SS | MS | $F$ | Significance $F$ |  |  |  |
| Regression | 1 | 24057.89126 | 24057.89 | 118.533 | $4.48427 \mathrm{E}-06$ |  |  |  |
| Residual | 8 | 1623.708738 | 202.9636 |  |  |  |  |  |
| Total | 9 | 25681.6 |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |
|  | Coefficients | Standard Error | $t$ Stat | $P$-value | Lower 95\% | Upper 95\% | Lower 95.0\% | Upper 95.0\% |
| Intercept | 291.6019417 | 11.43289905 | 25.50551 | 5.98E-09 | 265.2376293 | 317.9662542 | 265.2376293 | 317.9662542 |
| x | -27.90291262 | 2.562889198 | -10.8873 | 4.48E-06 | -33.81294571 | -21.99287953 | -33.81294571 | -21.99287953 |

a) $\hat{y}=291.6019-27.9029 x$

For every unit in $x$ we expect that $y$ to decrease by 27.9029
b) $\mathrm{R}^{2}=0.9367$
93.67\% of the variation in $y$ data is explained by $x$
c) c) $\hat{y}=291.6019-27.9029(4)=180$

