

Question 1

I. Suppose a fair die is thrown twice, then

- 1) the probability that the sum of numbers of the two dice is less than or equal to 4 is;
(A) 0.1667 (B) 0.6667 (C) 0.8333 (D) 0.1389
- 2) the probability that at least one of the die shows 4 is;
(A) 0.6667 (B) 0.3056 (C) 0.8333 (D) 0.1389
- 3) the probability that one die shows one and the sum of the two dice is four is;
(A) 0.0556 (B) 0.6667 (C) 0.3056 (D) 0.1389
- 4) the event $A = \{\text{the sum of two dice is 4}\}$ and the event $B = \{\text{exactly one die shows two}\}$ are,
(A) Independent (B) Dependent (C) Disjoint (D) None of these.

- II.
- 5) Assume that $P(A) = 0.3$, $P(B) = 0.4$, $P(A \cap B \cap C) = 0.03$, and $P(\overline{A \cap B}) = 0.88$, then the event A and B are,
(A) Independent (B) Dependent (C) Disjoint (D) None of these.
 - 6) Using question (5), $P(C|A \cap B)$ is equal to,
(A) 0.65 (B) 0.25 (C) 0.35 (D) 0.14
 - 7) If the probability that it will rain tomorrow is 0.23, then the probability that it will not rain tomorrow is:
(A) -0.23 (B) 0.77 (C) -0.77 (D) 0.23

Question 2

- I.
- The probability that a factory will open a branch in Riyadh is 0.7, probability that it will open a branch in Jeddah is 0.4, and the probability that it will open a branch in either Riyadh or Jeddah or both is 0.8, then the probability that it will open a branch:
- 8) In both cities is:
(A) 0.1 (B) 0.9 (C) 0.3 (D) 0.8
 - 9) In neither cities is:
(A) 0.4 (B) 0.7 (C) 0.3 (D) 0.2

II. The probability that a lab specimen contains high levels of contamination is 0.10. Three samples are checked, and the samples are independent, then:

10) the probability that none contains high levels of contamination is:

- (A) 0.0475 (B) 0.001 (C) 0.729 (D) 0.3

11) the probability that exactly one contains high levels of contamination is:

- (A) 0.243 (B) 0.081 (C) 0.757 (D) 0.3

Question 3

I. If in a class of 324-Stat. of 80 students, 60 are from engineering college and the rest are from computer science college, 10% of the engineering college students have taken this course before, and 5% of computer science college students have taken this course before. If one student from this class is randomly selected, then:

12) the probability that he has taken this course before is:

- (A) 0.25 (B) 0.0875 (C) 0.8021 (D) 0.75

13) If the selected student has taken this course before then the probability that he is from the computer science college is:

- (A) 0.1429 (B) 0.375 (C) 0.80 (D) 0.25

II. A random sample of 200 adults are classified according to sex and their level of education in the following table:

<i>Education</i>	<i>Male</i>	<i>Female</i>
<i>Elementary</i>	28	50
<i>Secondary</i>	38	45
<i>College</i>	22	17

If a person is selected at random from this group, then:

14) the probability that he is a male is:

- (A) 0.3182 (B) 0.44 (C) 0.28 (D) 78

15) The probability that the person is male given that the person has a secondary education is:

- (A) 0.4318 (B) 0.4578 (C) 0.19 (D) 0.44

- 16) The probability that the person does not have a college degree given that the person is a female is:
 (A) 0.8482 (B) 0.1518 (C) 0.475 (D) 0.085

III.

- 17) A man wants to paint his house in 3 colors. He can choose out of 6 colors. How many different color settings can he make?
 (A) 216 (B) 20 (C) 18 (D) 120
- 18) If continuous random variable X has a mean $\mu=16$, a variance $\sigma^2=5$, then $P(X = 16)$ is,
 (A) 0.0625 (B) 0.5 (C) 0.0 (D) None of these.
- 19) A lower bound valued according to Chebyshev's theory for $P(\mu - 2\sigma < X < \mu + 2\sigma)$ is,
 (A) 0.3175 (B) 0.750 (C) 0.965 (D) 0.250
- 20) A random variable X has a mean $\mu=12$, a variance $\sigma^2=9$, and unknown probability distribution. Using Chebyshev's theorem, $P(3 < X < 21)$ is at least equal to,
 (A) 8/9 (B) 3/4 (C) 1/4 (D) 1/16

Question 4

- I. A shipment of 7 television sets contains 2 defective sets. A hotel makes a random purchase of 3 of the sets.

- 21) If x is the number of defective sets purchased by the hotel, the probability of no defective television set, $P(X = 0)$ is,
 (A) 0.57 (B) 0.14 (C) 0.29 (D) 0
- 22) $P(0 < X \leq 2)$ is,
 (A) 0.29 (B) 0.43 (C) 0.71 (D) 1

- II. Consider the density function

$$f(x) = \begin{cases} k\sqrt{x}, & 0 < x < 1 \\ 0, & \text{elsewhere.} \end{cases}$$

- 23) The value of k is:
 (A) 1 (B) 0.5 (C) 1.5 (D) 0.667

- 24) The probability $P(0.3 < X \leq 0.6)$ is,
 (A) 0.4647 (B) 0.3004 (C) 0.1643 (D) 0.4500
- 25) The expected value of X, $E(X)$ is,
 (A) 0.6 (B) 1.5 (C) 1 (D) 0.667

Question 5

Let X be a random variable with the following probability distribution:

x	-3	6	9
f(x)	0.167	0.5	0.333

- 26) $E(X)$ is,
 (A) 4.0 (B) 5.5 (C) 6.5 (D) 6.0
- 27) $E(X^2)$ is,
 (A) 30.25 (B) 36.0 (C) 46.5 (D) 126.0
- 28) $\text{Var}(X) = \sigma_X^2$ is,
 (A) 13.25 (B) 16.25 (C) 90.25 (D) 95.75
- 29) $E[(2X + 1)]$ is,
 (A) 8 (B) 11 (C) 12 (D) 13
- 30) Variance of $(2X+1) = \sigma_{2X+1}^2$ is,
 (A) 65 (B) 66 (C) 16.25 (D) 95.75